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3D plane labeling stereo matching with content aware adaptive windows

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Abstract: In this paper, we present an algorithm that exploits both the underlying 3D structure and image entropy to generate an adaptive matching window. The presented algorithm estimates real valued disparity maps by smartly exploring a 3D search space using a novel hypothesis generation approach that acts like a propagation scheduler. The proposed approach is among the top performing results when evaluated in the Middlebury, KITTI 2015 benchmarks.

1 INTRODUCTION

The problem of 3D plane labeling to estimate depth from two or more images has become the focus area of modern stereo matching algorithms. The core issue in 3D plane labeling using two images (left I₁ and right I₂ views of a scene) is finding the correspondences for each pixel from image I₁ to I₂ by assigning a 3D plane that produces a real valued disparity. This process is better modeled as an optimization problem where the objective is to compute the disparity assignment that minimizes eq.1.

\[ E(D) = \arg \min_D \sum_p^{\text{NumP}} \{ C_p(D_p) + \sum_{q \in N(p)} V_{pq}(D_p, D_q) \} \]  

(1)

\[ E(D) \] is the cost of the disparity assignment (energy), D is a set of planes and D_p encodes a plane at pixel p, that gives the disparity of the pixel at p with respect to another image. D_p(q) is the disparity estimated using plane D_p evaluated at pixel q. The plane D_p has two parameters: a 3D unit normal vector \( \hat{n}_p = (n_x^p, n_y^p, n_z^p) \) and disparity \( d_p \). The disparity of pixel \( q = (x_q, y_q) \) using \( D_p \) is given by:

\[ D_p(q) = a \cdot x_q + b \cdot y_q + c \]  

(2)

where \( a = -n_x^p/n_z^p, b = -n_y^p/n_z^p \) and \( c = (n_x^p \cdot x_q + n_y^p \cdot y_q + n_z^p \cdot d_p) / n_z^p \) as in (Bleyer et al., 2011). \( C_p \) is a function that measures the similarity/dissimilarity of two pixels (e.g. \( I_1(p) \) and \( I_2(p + D_p(p)) \)), and \( \text{NumP} \) is the number of pixels in the image. \( N(p) \)

1 The displacement along a search area is known as disparity.

2 RELATED WORK

The idea of assigning planes per pixel to estimate sub-pixel disparity has been previously used in (Klaus et al., 2006; Woodford et al., 2007; Bleyer et al., 2011; Besse et al., 2012; Olsson et al., 2013; Heise et al., 2013; Taniai et al., 2014; Sinha et al., 2014; Yamaguchi et al., 2014). These algorithms can be classified in two categories: fixed plane inference (FPI) and dynamic plane inference (DPI). FPI algorithms make an initial disparity estimation and then extract the planes, which are then used during the inference process to estimate disparity. By contrast DPI algorithms assign one or more planes to each pixel, and then propagate “good” planes (i.e. low/high scores depending on the cost function) to neighbors/regions under the assumption that neighbors/regions are likely to have the same plane. Then in a refinement stage the
planes are improved, thus the planes are dynamically updated. DPI algorithms in particular have become the state of the art (e.g. (Bleyer et al., 2011; Besse et al., 2012; Heise et al., 2013; Taniai et al., 2014)).

Common issues in DPI algorithms include the use of large adaptive windows (commonly using (Yoon and Kweon, 2006)) or segment (Li et al., 2015) based similarity cost to compute the similarity/dissimilarity cost, which can result in a strong bias towards large planes. A possible solution to this issue is to change the window size, which requires either some assumption about the 3D structure or image content. However, changing the window size can result in poor performance in textureless areas and thus requires additional assumptions such as the uniqueness constraint or occlusion penalties. Another issue in DPI algorithms such as (Bleyer et al., 2011; Besse et al., 2012) is that the hypothesis generation and propagation is done sequentially.

2.1 Contributions

To address some of the issues described the proposed approach makes the following contributions:

- Content aware adaptive window aggregation: Reduces error and loss of details.
- Use of a cost function that imposes a local hypothesis uniqueness, unlike (Klaus et al., 2006; Woodford et al., 2007; Olsson et al., 2013; Yamaguchi et al., 2014; Sinha et al., 2014; Bleyer et al., 2011; Besse et al., 2012; Taniai et al., 2014): Helps to handle textureless surfaces, and does not require higher order interactions (unlike (Vogel et al., 2015)) in a MRF.
- Use of a cost function that penalizes disparity values outside a defined search range: Prevents invalid disparity values assignment.
- Use of a single global hypothesis per disparity plane: Eliminates the need to update multiple hypotheses.
- Use of a hypothesis generator that acts as a propagation scheduler: Helps to do a search in a 3D space.

3 PROPOSED ALGORITHM

The proposed approach to estimate a 3D plane labeling per pixel has the following components:

- Content aware slanted windows to compute the data term (pixel similarity measure).
- Uniqueness and out of range terms.
- Adaptive search range.
- Smoothness term that adapts to image content.
- Hypothesis generation/update that acts as a propagation scheduler.

The novel content aware windows exploit both intensity and 3D structure (if available) to adapt the window size and similarity function. It’s important to note that the proposed hypothesis generation provides an alternative to sequential algorithms (e.g. (Bleyer et al., 2011; Besse et al., 2012)) and does not impose restrictions to the pairwise interactions like (Taniai et al., 2014).

3.1 Content aware adaptive similarity function

DPI algorithms commonly use the adaptive window (eq.4) from (Yoon and Kweon, 2006), which has the following issues: bias towards large planes (good quality in textureless areas), center pixel bias for large windows (results in loss of detail, e.g. fig.1), and noisy results for small windows. The center pixel bias can be reduced by using the windows from (Zhang et al., 2009), which adapts better to local image changes, but can give poor results if the windows are poorly estimated or window size is not large (particularly in textureless areas). To compensate for the center pixel bias while keeping good performance in textureless areas, a texture measure $L_p$ (eq.3) is used to balance the influence of eq.4 and eq.5 (fixed size modified version of (Zhang et al., 2009)) in eq.7.

$$ L_p = \left\{ e^{-\frac{\|D_p\|}{\sigma}} \right\} T_p = \frac{1}{Z} \sum_{q \in N(p)} e^{-\frac{\|D_q\|}{\sigma}} h(p) \right\} $$

$$ AW_p(D_p) = \frac{1}{Z} \sum_{q \in N(p)} e^{-\frac{\|D_q\|}{\sigma}} c_q(D_p) $$

$$ CW_q(D_p) = \frac{1}{Z} \sum_{q \in N(q)} e^{-\frac{\|D_q\|}{\sigma}} CW_q(D_p) $$

$$ CW_q(D_p) = \frac{1}{Z} \sum_{q \in N(q)} e^{-\frac{\|D_q\|}{\sigma}} c_q(D_p) $$

$$ C_p(D_p) = L_p \cdot AW_p(D_p) + (1 - L_p) \cdot CW_q(D_p) $$

where $Z$, $Z_0$, $Z_c$ are normalization constants such that the weights in the neighbourhood add up to one, $h(p)$ is a $5 \times 5$ entropy filter, $|I_p - I_q|$ is the L1 distance in RGB space, $N(p)$ is the neighborhood around p ($n \times n$ window), $N_h(p)$ and $N_v(q)$ are the horizontal ($1 \times n$) and vertical ($n \times 1$) neighborhoods around p and q. Eq.3 is the adaptively filtered version of $h(p)$, which is done to clean the noisy measure, and better balance $AW_p$ and $CW_q$ close to edges.

The adaptive window from (Zhang et al., 2009) was modified as follows: Use of range terms for vertical and horizontal directions. Only horizontal arms are computed, while the vertical arm remains of a
map gradient is first measured along the pixels in the segment perimeter (eq.11), then a segment difference measure is computed using the median disparity of neighbouring segments (eq.12), and later propagated per pixel (eq.13) to reduce the effect of noise from the initial disparity map. Thus window size at each pixel $p$ is computed using $n = \Omega(p)$ in eq.14.

$$w_p = \frac{1}{K|\hat{N}(p)|} \sum_{q \in \hat{N}(p)} \left| d_p - d_q \right| \geq 2\frac{K_w}{3}$$  \hspace{1cm} (11)$$

$$w_p = \begin{cases} 
\frac{1}{K|\hat{N}(p)|} \sum_{q \in \hat{N}(p)} \min(|d_p - \hat{d}_q|, K_w) : \hat{w}_p > \tau_w \\
0 : \text{otherwise}
\end{cases} \hspace{1cm} (12)$$

$$W_p = \frac{1}{Z} \sum_{q \in \hat{N}(p)} e^{-\frac{|d_p - \hat{d}_q|}{\sigma}} w_p \hspace{0.5cm} Z = \sum_{q \in \hat{N}(p)} e^{-\frac{|d_p - \hat{d}_q|}{\sigma}} \hspace{1cm} (13)$$

$$\Omega(p) = \begin{cases} 
\omega_1 : W_p > \tau_{nn} \text{ and } T_p > \tau_L \\
\omega_2 : \text{otherwise}
\end{cases} \hspace{1cm} (14)$$

where, $\hat{d}_p$ and $\hat{d}_q$ are the median disparities (to compensate for noise in the initial estimate) of the segments where pixels $p$ and $q$ come from. $\hat{N}(p)$ is the perimeter of the segment where $p$ comes from. Notice that eq.12 computes a value per segment, while eq.13 does it per pixel by aggregating neighboring values based on intensity similarity. $\tau_{nn}$ is dynamically computed from $W_p$ using Otsu threshold. Eq.11 measures the number of pixels that can be considered for being above a threshold.

### 3.2 Uniqueness and out of range terms

The Similarity function described above only takes into consideration intensity to compute a matching score. However, this has the implicit assumption that each pixel has a unique match, which in general is not necessarily true (e.g.,2), especially in occluded areas and textureless regions that are prone to have multiple matches (see red boxes in fig.3). Eq.15 penalizes each pixel that has multiple matches (similar to (Kolmogorov and Zabih, 2001)).

$$U(D_p) = \begin{cases} 
\tau_{unique} : L(D_p) \\
0 : \text{otherwise}
\end{cases} \hspace{1cm} (15)$$

where $L(D_p)$ is true when a pixel $p$ is mapped to $d + D_p$ which has more than one match. This is done per hypotheses, which means it’s a local uniqueness terms, unlike (Kolmogorov and Zabih, 2001) and (Vogel et al., 2015) where it’s represented as part of the MRF.

A plane $D_p$ evaluated at a different pixel $q$ in the image could have disparity values that lie outside

---

2In particular adaptive windows have a tendency to lose thin vertical details.
Figure 2: Example of uniqueness constraint violation; two pixels (red arrows) in left image scanline map to a single pixel in right image (red pixel).

a defined search range of disparities. Eq.16 penalizes disparity values that lie outside a defined search range.

\[
O(D_p) = \begin{cases} 
1 - \exp\left(-\left|D_p - \text{min}D\right|/\sigma_d\right) & : D_p < \text{min}D \\
1 - \exp\left(-\left|D_p - \text{max}D\right|/\sigma_d\right) & : D_p > \text{max}D \\
0 & : \text{otherwise}
\end{cases}
\] (16)

where minD and maxD are the minimum and maximum of the disparity search range, while \(\sigma_d\) is the maximum deviation allowed for values outside the search range. Eq.7 is updated to include eq.15 and eq.16, which then becomes:

\[
\hat{C}_p(D_p) = C_p(D_p) + U(D_p) + O(D_p)
\]

Note that the proposed uniqueness term requires to keep track of its current value after inference to update the current cost (eq.17) and prevent energy from oscillating in later iterations.

3.3 Search range detection

To detect spurious disparities the probability distribution (from the normalized disparity histogram) of each disparity present in both the left and right disparity maps is computed using an initial search range [\(\text{min}D, \text{max}D\)], and an n-point (n is 18% of the initial disparity search range) Parzen window is applied to smooth the probability distribution.

Finally, a search finds the lowest (\(\text{min}D\)) and largest disparities (\(\text{max}D\)) that are above a threshold \(\tau_{\text{max}D}\) and \(\tau_{\text{min}D} = \frac{2}{3}\tau_{\text{max}D}\). It’s possible that \(\text{min}D\) is over estimated and \(\text{max}D\) under estimated, which is addressed by \(\text{min}D = \text{max}(\text{min}D, \text{min}D - \Delta\text{min}D), \) and \(\text{max}D = \text{min}(\text{max}D, \text{max}D + \Delta\text{max}D).\) The estimated bounds on the disparities are used to eliminate or penalize unrealistic disparities. \(\text{max}D\) is used during the inference process, and \(\text{min}D\) during the post-processing stage.

3.4 Smoothness term

The assumption made by the proposed edge model is that possible depth discontinuities are allowed small variations, while areas with a similar intensity are allowed to have larger changes, by contrast in (Besse et al., 2012; Taniai et al., 2014) the maximum variation is constant.

\[
V_{pq}(D_p, D_q) = \begin{cases} 
w_{pq}\lambda_0(D_p - D_q, K2) & : |F_p - F_q| < \tau_{\text{diff}} \\
w_{pq}\lambda_0(D_p, D_q, K1) & : \text{otherwise}
\end{cases}
\]

(18)

\[
w_{pq} = \left\{ \frac{1}{Z_n} e^{-\left|I_{\omega}(p) - I_{\omega}(q)\right|} \right\} Z_n = \sum_{q \in N(p)} e^{-\left|I_{\omega}(p) - I_{\omega}(q)\right|}
\]

(19)

where \(K1 < K2, I_{\omega}\) is a gray level image after applying the quick shift segmentation\(^3\) (Vedaldi and Soatto, 2008; Vedaldi and Fulkerson, 2008), \(w_{pq}\) and \(\lambda\) are weights, \(F_p\) and \(F_q\) come from a local cue map \(F\), and \(\tau_{\text{diff}}\) is a threshold, which means the growth limit of the smoothness term adapts based on the local cue map \(F\) (eq.22), while \(\omega(D_p, D_q, K)\) is given by:

\[
\omega(D_p, D_q, K) = \text{min}(\{D_p(p) - D_q(q)\} + |D_q(q) - D_p(p)|)), K
\]

(20)

\(F_p\) is computed using the intensity gradient of the reference image, and is used to locate possible depth discontinuities. Using the image gradient can lead to problems in areas where the gradient is noisy (e.g. image or texture is noisy). This issue can be partially addressed by filtering both the image and gradient, which can provide a two-fold advantage. First, the gray level of the reference image is filtered (eq.21) to remove potential sources of noise (e.g. noisy edges or sensor noise). Second, a filter is applied to the gradient magnitude (eq.22) to remove false edges (e.g. small letters on a wall).

\[
\hat{I}_g(p) = \left\{ \frac{1}{Z} \sum_{q \in N(p)} e^{\frac{-\left|\nabla I(p)\right|}{\sigma}} \right\} Z = \sum_{q \in N(p)} e^{\frac{-\left|\nabla I(p)\right|}{\sigma}}
\]

(21)

\[
F_p = \left\{ \frac{1}{Z} \sum_{q \in N(p)} e^{\frac{-\left|\nabla I(p)\right|}{\sigma}} \right\} Z = \sum_{q \in N(p)} e^{\frac{-\left|\nabla I(p)\right|}{\sigma}}
\]

(22)

where \(I\) is the color image, \(|\nabla \hat{I}_g(p)\| = |\nabla \hat{I}_g(p)| + |\nabla \hat{I}_g(q)|, \) and \(\nabla \hat{I}_g(p)\) and \(\nabla \hat{I}_g(q)\) are obtained using the Sobel gradient operator.

4 HYPOTHESIS GENERATION AND PROPAGATION

The model described so far makes the assumption that each pixel has associated a set of planes from which a single optimal plane assignment (\(D\)) is found using TRW-S. The proposed hypothesis generation algorithm will give each pixel \(p\) a set \(GH_p = D_p \cup H_p \cup \)
\[ DS_p \cup V_p \]  
\[ D_p \] is the current solution, \( H_p \) is generated from pixel coordinates using \((r, sampling)\), \( DS_p \) is generated from the pixels that belong to the same segment\(^4\) \((P, sampling)\), \( V_p \) is generated from pixels coming from another view \((V, sampling)\). Using these disparity planes at each pixel allows the following:

1. Pixels can keep their current plane assignment \( D_p \).
2. Pixels propagate their planes to close and distant pixels via \( r, sampling \).
3. Segments help to propagate large disparity planes to distant pixels via \( P, sampling \).
4. Views propagate their planes via \( V, sampling \).

Note that hypothesis generation is done from a single disparity plane assignment \( D \) for both left and right views, and the hypothesis generation is effectively acting as a propagation scheduler once inference is done.

### 4.1 \( r, sampling \)

Algorithms that use plane propagation commonly assume that neighboring pixels are likely to have the same plane (Bleyer et al., 2011; Besse et al., 2012) or that planes are shared within a certain area (Taniai et al., 2014). The proposed \( r, sampling \) tries to generate hypotheses that are shared in a region (similar to (Taniai et al., 2014)), but also include a few planes from a distant region. The pixel coordinates used for sampling are \((X, Y) = \{ [divs \times (x+i)/divs] + r + i, [divs \times (y+j)/divs] + r + j \mid (j,i) \in [-r,r] \times [-r,r] \}\), which come from a window of width \( 2r + 1 \). \((x,y)\) are the coordinates of pixel \( p \), and \( divs = 2r + 1 \). The \( r, sampled \) plane at pixel \( p \) sampled with \((i, j)\) is given by:

\[ \hat{D}_p^{ij} = D_p^{ij} \tag{23} \]

This sampling is repeated for each \((i, j) \in [-r, r] \times [-r, r]\) generated by a window centered at \( p \), which means each pixel has a set of hypotheses:

\[ H_p = \bigcup_{i=-r}^{r} \bigcup_{j=-r}^{r} \hat{D}_p^{ij} \tag{24} \]

The purpose of this sampling strategy is to include the planes from all neighbors in the \( divs \times divs \) window centered at \( p \) and also neighbors that come from distant \( divs \times divs \) windows. Fig.4 shows how a \( 3 \times 3 \) window (i.e. \( r = 1 \)) would generate several hypotheses, where each colored box is a different plane. For illustration purposes we will center our attention around the “red plane” and its eight neighbors. \( H_1...H_8 \) represent the hypothesis generated by using \( i \) and \( j \) according to eq.24. In particular fig.4 demonstrates how each of the non-purple planes are transformed into a hypothesis. Also note that the planes from the purple pixels are used as well (although they are not necessarily the same!). This is meant to allow the propagation of distant neighbors. This hypothesis generation strategy is similar to that of (Taniai et al., 2014), but ours does not impose a sub-modular requirement to the pairwise interaction in the generated hypothesis.

### 4.2 \( P, sampling \)

One assumption commonly used in stereo matching is that pixels with similar intensity have a similar disparity value or disparity plane. An easy way to group pixels is to use super-pixels or segments (e.g. SLIC(Achanta et al., 2012) in this paper), which are then initialized with a plane. The disparity plane \( D_{sp} \) is assigned to a segment \( s_p \) by randomly selecting a plane from the planes associated with the pixels that belong to the segment:

\[ D_{sp} = D\phi(p) \tag{25} \]

\( D_{sp} \) denotes a plane at pixel \( p \) that was assigned by function \( D\phi(p) \) which randomly selects a plane such that it belongs to the same segment as pixel \( p \). This criteria will only generate one hypothesis per pixel, although there may be other planes in the same segment. This is done under the assumption that one

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\(^4\)A segment will be a set of pixels that are grouped using some logical criteria e.g. spatial distance and color similarity.
of planes selected may be correct without the need of fitting one plane to the entire segment. Although each $D_{s_p}$ is assigned to several pixels (depending on the super-pixel algorithm used), it may be desirable to create additional hypotheses from the segments that surround $s_p$. To sample the neighboring segments the centroid of each $s_p$ is computed, all neighboring $s_p$ centroid segments are sorted by their polar angle with respect to $s_p$, and finally only the first $P$ elements are selected.

$$DS_p = \left\{ D_{s_p} \cup \left( \bigcup_{j=1}^{P} D_{s_{qi}} \right) \Theta(s_{qi},s_p) < ... < \Theta(s_{qP},s_p) \right\}$$

where $s_{qi} \in N(s_p)$ and $\Theta(s_{qi},s_p)$ is the function that evaluates the polar angle with respect to the centroid of $s_p$.

### 4.3 V-sampling

The hypotheses $H_p$ and $DS_p$ so far are generated from only one view. Since left and right sets of disparity planes are computed it’s possible that one them contains planes which could be used to generate a better set of hypothesis. The additional set of hypotheses is computed by mapping the planes $H_p \cup DS_p$ from the other view to the current image. This process will be referred to as V-sampling and can be expressed by $V_p = Dw_p \cup Hw_p \cup DS_{wp}$, where $Dw_p$ is the current solution of the other view, $Hw_p$ and $DS_{wp}$ are the mapped versions of r-sampling and P-sampling hypotheses from the other view. Note that this doubles the number of hypotheses. For instance: assume two views are used, then for $r = 2$ and $P = 6$ the number of hypotheses generated would be 32 for one view, but after doing V-sampling the number of hypotheses would be 64. Note that (Bleyer et al., 2011) follows a similar approach (i.e. mapping the planes from one view to the other), but only generates one hypothesis.

### 5 REFINEMENT

Using the algorithms from the previous section, hypotheses are generated and a unique disparity plane is assigned to each pixel (i.e $D_p$). The solution is then refined by generating a new set of hypotheses $Gre_f_p = D_p \cup Hre_f_p \cup DS_{ref_p}$ with perturbations(Bleyer et al., 2011) added to the plane parameters (normal vector $\hat{n}_p$ and disparity $d_p$), and the doing inference once again. The hypothesis refinement process is:

1. Given the current disparity map $D_{curr}$, $\Delta n_1 = \kappa$, $\Delta d_1 = Sr \times \kappa$ as input.
2. For $t = 1$ to $s$ steps do:

   (a) compute pixel hypothesis re-sampling ($H_{ref_p}$), see sec.5.1.
   (b) compute segment hypothesis re-sampling ($DS_{ref_p}$), see sec.5.2.
   (c) compute $Gre_f_p = D_p \cup Hre_f_p \cup DS_{ref_p}$ and obtain a new solution $\hat{D}_{curr}$.
   (d) set $D_{curr} = \hat{D}_{curr}$, $\Delta n_t = \Delta n_{t-1}/2$ and $\Delta d_t = \Delta d_{t-1}/2$.

This means that for each pixel in the disparity map three situations can happen: a plane is propagated from a neighbor, a plane is refined and propagated from a neighbor, or a plane stays the same. Propagation is done simultaneously during the hypothesis refinement process, which happens due to the way hypotheses are generated. Also note that V-sampling is not used. To the best of our knowledge no other algorithm performs simultaneous propagation and refinement, which could have the potential to reduce the space needed to store hypotheses. The refinement process doubles the number of hypotheses. For instance: if r-sampling ($r = 2$) and P-sampling($P = 6$) generate 32 hypotheses, then refinement would add 32 additional hypotheses (with perturbations added).
5.1 Pixel hypothesis re-sampling

To overcome local minima of the current disparity plane assignment, and obtain a refined version of r-sampling, each pixel is updated by randomly adding a perturbation selected from \([-\Delta n, \Delta n]\) (uniform distribution) and \([-\Delta d, \Delta d]\) (uniform distribution) which are initially set to \(\Delta n = \kappa\) (the new normal vector has to be normalized) and \(\Delta d = Sr \times \kappa\). \((Sr\) search range in disparity units), with \(\kappa = 0.2\) as recommended in (Besse et al., 2012). This process is repeated several times. After each step \(\Delta n\) and \(\Delta d\) are updated by setting them to \(\Delta n = \Delta n_{-1}/2\) and \(\Delta d = \Delta d_{-1}/2\). This process generates a new set of hypotheses \(H_{ref} = H_p \cup H_n,\) where \(H_n\) is generated using \(r\)-sampling from \(D_p\) after perturbations have been added.

5.2 Segment hypothesis re-sampling

Refined versions of the disparity planes image segment are obtained by creating variants of the current set of disparity planes per image segment. First, for each segment in the current image random disparity planes \((DS_{r})\) are generated using \(P\)-sampling and then noise is added. This generates a new set of hypotheses \(DSU_{p} = \Psi(DS_{r} \cup DS_{rn}),\) where \(DS_{rn}\) was generated via \(P\)-sampling, \(DS_{r}\) is the perturbed version of \(DS_{r},\) and \(\Psi\) is a function that takes each pair of planes \(DS_{r}\) and \(DS_{rn}\) and returns the one whose cost locally minimizes eq.1, with respect to the current solution. This leaves \(P\) plane hypotheses per segment. Another set of hypotheses \(DSU_{p}\) is then generated, in which each segment \(S_{b_j}\) has a number from \([1...n].\) These numbers are used as multipliers to control the random interval \([-\Delta d, \Delta d]\), such that \(\Delta d = 1 \times \Delta d.\) Thus each element of \(DSU_{p}\) is the \(\Delta d\) perturbed version of a plane generated by \(Db(p)\) to allow large jumps of disparity that can change an entire segment. This re-sampling produces a set of hypotheses \(DS_{ref} = DSU_{p} \cup DSU_{n}p.\)

6 OVERALL DISPARITY ESTIMATION PROCESS

The disparity estimation process can now be summarized as follows:
1. Initialize solution \(D_{left}\) and \(D_{right}\) to either a random plane per pixel or initialize from a pre-computed disparity map.
2. For \(t = 1\) to \(s\) steps do:
   a. Generate hypotheses \(GH_{left}p\) and \(GH_{right}p,\) see sec.4.
   (b) Do inference and compute new solutions \(\hat{D}_{left}\) and \(\hat{D}_{right}.
   (c) Refine the new solutions \(\hat{D}_{left}\) and \(\hat{D}_{right},\) see sec.5.
   (d) set \(D_{left} = \hat{D}_{left}\) and \(D_{right} = \hat{D}_{right}.

Random initialization is done by selecting a random uniform disparity. The normal \(\hat{n}\) is selected from the uniform distribution of a unit sphere. \(\Delta d\) and \(\Delta \hat{n}\) are selected in the same way. Fig.5 shows intermediate stages for the teddy image, using the proposed algorithm with random initialization. It can be observed that our approach is effectively propagating the planes and also minimizing eq.1. Notice that in the first propagation the outline of the underlying 3D surface can already be seen. When using a pre-computed disparity map\(^5\) to initialize the current solution, the normal vectors are computed at five scales, averaging, and creating a plane per pixel by estimating the parameters of eq.2 using the normal vectors and current disparity.

Finally, the proposed algorithm is extended to multi-scale:
1. Precompute disparity maps \(D_{left},\) \(D_{right,pre}\) (e.g. using SGM or random initialization).
2. Estimate window size from \(D_{left,pre}\) and \(D_{right,pre}\) (if disparity map was precomputed).
3. Compute initial solution \(D_{left}\) and \(D_{right}\) by downsampling \(D_{left,pre}\) and \(D_{right,pre}\) to one quarter size and solving.
4. Compute updated solution at half-size by initializing with current \(D_{left}\) and \(D_{right}\).
5. Compute updated solution at full-size by combining \(D_{left,pre}\) and \(D_{right,pre}\) with current \(D_{left}\) and \(D_{right}\), i.e compute \(GH_{pre}p \cup GH_{p}\) for left and right, then do inference to update current solutions, and update maxD (sec.3.3).
6. Compute updated solution at full-size by initializing with current \(D_{left}\) and \(D_{right}\).
7. Compute occlusion detection and post-processing.

The post-processing is done by computing occluded, and mismatched areas as in (Zbontar and LeCun, 2015). Then masks containing non-occluded areas, and depth edges\(^6\) are eroded and marked as occluded to reduce the fattening effect. Then \(minD\) is updated (sec.3.3), and disparities lower than \(minD\) are marked as occluded. The occluded areas are then filled in using simple background interpolation and

\(^5\)The pre-computed disparity map is obtained using SGM, see support material.

\(^6\)Detected using Canny edge detector.
filtered by applying a weighted median filter. The non-occluded areas are NOT post-processed.

All experimental results were carried out using the multi-scale approach with pre-computed initialization. The proposed algorithm uses the following parameters for all scales: aggregation window sizes of $w_1 = 41 \times 41$, $w_2 = 25 \times 25$, $\tau_{grad} = 3/255$, $\tau_{cen} = 9/25$, $\sigma_r = 10/255$, $\sigma_d = 0.5$, $\tau_w = 2.5$, $\tau_{diff} = 0.07$, $\alpha = 30$, $K_1 = 1$, $K_2 = 6$, $r = 2$, $P = 6$, $\tau_b = 2$, $\tau_u = 0.5$, $K_w = 8$. For quarter and half size $\lambda = 0.06$, and $\lambda = 0.12$ for full size. The disparity estimation is iterated 4 times at quarter size, 1 time at half-size and 4 times at full size. The refinement iterations are set to 5 times each scale. These parameters were obtained by using the Middlebury training data, and every fifth image from KITTI 2015 and 2012 training data.

7 PROPOSED APPROACH VS. STATE OF THE ART

The approach presented in this paper was validated in three stages. First, the proposed content aware adaptive windows are compared to the traditional approach, as well as the tolerance to noise and evaluation of $r-$sampling performance. Then the proposed algorithm is extensively validated on three data sets: The new Middlebury (15 images) data set (Scharstein et al., 2014), KITTI 2015(Menze and Geiger, 2015) and 2012(Geiger et al., 2012) (up to 200 images). The only parameters that are set differently are $\Delta min D$ (10 for Middlebury and 5 for KITTI), $\Delta max D$ (60 for Middlebury and 20 for KITTI) and $\tau_{max D}$ (0.0028 for Middlebury and 0.0003 for KITTI).

To test the performance of the proposed similarity function three competing functions are compared (tab.1): $AW$ is the traditional approach (eq.4) with the enabled out of range term, but no uniqueness term. $AW + CW$ is the proposed adaptive window (eq.7) with the enabled out of range term, but no uniqueness term. $AW + CW + U$ is the proposed adaptive window with the out of range and local uniqueness terms (eq.17). Our innovations (eq.17) clearly improve on the popular adaptive windows(Yoon and Kweon, 2006) commonly used in DPI algorithms.

Table 2: Evaluation of $r$-sampling and proposed approach (all stages enabled) tolerance to noise in initial disparity map, using every fifth image from KITTI 2015 training data. ns0 no noise, and added disparity noise $[-1,1]$ (ns1), $[-2,2]$ (ns2), $[-3,3]$ (ns3).

To evaluate the effectiveness of $r$-sampling we replace it with the pixel shared hypotheses LSL from (Taniai et al., 2014). In tab.2 our sampling strategy (ns0) in general matches the performance of LSL, and even gives improved performance for foreground objects $D1 – fg$, which is caused by the larger number of hypotheses 25 for $r$-sampling vs. 16 for LSL due to different hypothesis generation strategies. The performance of our approach in tab.2 shows that the proposed approach ns0 is robust to several levels of uni-
form real valued noise added to the initial disparity map.

The main competitors to our algorithm are MCNCC (Zbontar and LeCun, 2015) and MDP (Li et al., 2016a), since they were evaluated using the same data sets (see tab.3 and tab.4). To compare to the state of the art, from all data sets competitors were selected by choosing the best performing convolutional neural network algorithms and the best performing algorithm not using convolutional neural networks. For the KITTI 2015 and 2012 results, algorithms must appear in both data sets evaluation tables. The proposed algorithm is among top performers in the Middlebury (tab.3) and KITTI 2015/2012 (tab.4 and tab.5). In tab.3 the disparity map is evaluated only in non-occluded areas, integer and sub-pixel scores are computed using an error pixel threshold of 2.0 (rank 9th out of 44) and 0.5 (rank 8th out of 44) respectively.

Table 3: Comparative table of results (on non-occluded pixels) on the new Middlebury data set. Only non-anonymous entries are used for comparison: PMSC (Li et al., 2016b), Mesh and MeshE (Zhang et al., 2015), APAP (Park and Yoon, 2016), MCNCC (Zbontar and LeCun, 2015), MDP (Li et al., 2016a).

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>%bad &gt; 2.0</th>
<th>%bad &gt; 0.5</th>
<th>avg. error</th>
<th>rms</th>
</tr>
</thead>
<tbody>
<tr>
<td>Our</td>
<td>10.50&lt;sup&gt;st&lt;/sup&gt;</td>
<td>43.2&lt;sup&gt;st&lt;/sup&gt;</td>
<td>3.17</td>
<td>15.6</td>
</tr>
<tr>
<td>PMSC&lt;sup&gt;8&lt;/sup&gt;</td>
<td>6.87&lt;sup&gt;1st&lt;/sup&gt;</td>
<td>39.1&lt;sup&gt;1st&lt;/sup&gt;</td>
<td>2.27</td>
<td>12.9</td>
</tr>
<tr>
<td>MeshE&lt;sup&gt;9&lt;/sup&gt;</td>
<td>7.29&lt;sup&gt;2nd&lt;/sup&gt;</td>
<td>40.1&lt;sup&gt;2nd&lt;/sup&gt;</td>
<td>2.50</td>
<td>15.4</td>
</tr>
<tr>
<td>APAP&lt;sup&gt;10&lt;/sup&gt;</td>
<td>7.46&lt;sup&gt;3rd&lt;/sup&gt;</td>
<td>50.9&lt;sup&gt;3rd&lt;/sup&gt;</td>
<td>3.89</td>
<td>21.1</td>
</tr>
<tr>
<td>MCNCC</td>
<td>8.29&lt;sup&gt;5th&lt;/sup&gt;</td>
<td>40.7&lt;sup&gt;5th&lt;/sup&gt;</td>
<td>3.82</td>
<td>21.3</td>
</tr>
<tr>
<td>MDP</td>
<td>12.6&lt;sup&gt;8th&lt;/sup&gt;</td>
<td>61.8&lt;sup&gt;8th&lt;/sup&gt;</td>
<td>5.28</td>
<td>23.1</td>
</tr>
<tr>
<td>Mesh</td>
<td>13.4&lt;sup&gt;11th&lt;/sup&gt;</td>
<td>51.2&lt;sup&gt;11th&lt;/sup&gt;</td>
<td>4.63</td>
<td>20.1</td>
</tr>
</tbody>
</table>

In the KITTI benchmark, our algorithm ranks 8<sup>th</sup> (out of 38), and 14<sup>th</sup> (out of 83) for KITTI 2015 and 2012 respectively. The evaluation on KITTI 2012 proved more challenging (tab.5) mostly in the presence of reflective regions, and color image misalignment (the gray images are colored, and not properly aligned to the ground truth shape image). The top performing algorithms (for KITTI 2015 and 2012) currently achieve high performance by: exploiting scene specific content to solve ambiguities (e.g. cars in Disp.v2), training specifically for the data set (e.g. MCNCC), or using multiple image pairs to estimate disparity (e.g. PRSM, OSF). By contrast the proposed algorithm achieves top performing results in multiple data set by: using only one image pair, solving at different scales, not using scene specific features (e.g. cars), and generating a set of hypothesis from a single initial hypothesis.

Table 4: Comparative table of results (all pixels evaluated) on the KITTI 2015 data set. Only non-anonymous entries are used for comparison: Disp v2 (Guney and Geiger, 2015), PRSM (Vogel et al., 2015), OSF (Menze and Geiger, 2015).

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>%bad</th>
<th>%bad</th>
<th>avg.</th>
<th>avg.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Our</td>
<td>3.55</td>
<td>12.30</td>
<td>5.01</td>
<td></td>
</tr>
<tr>
<td>Disp.v2</td>
<td>3.00</td>
<td>5.56</td>
<td>3.43</td>
<td></td>
</tr>
<tr>
<td>MCNCC</td>
<td>2.89</td>
<td>8.88</td>
<td>3.89</td>
<td></td>
</tr>
<tr>
<td>PRSM</td>
<td>3.02</td>
<td>10.52</td>
<td>4.27</td>
<td></td>
</tr>
<tr>
<td>MDP</td>
<td>4.19</td>
<td>11.25</td>
<td>5.36</td>
<td></td>
</tr>
<tr>
<td>OSF</td>
<td>4.54</td>
<td>12.03</td>
<td>5.79</td>
<td></td>
</tr>
</tbody>
</table>

Table 5: Comparative table of results (all pixels evaluated) on the KITTI 2012 (Geiger et al., 2012) data set. Only non-anonymous entries are used for comparison.

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>%bad noc</th>
<th>%bad occ</th>
<th>avg. noc</th>
<th>avg. occ</th>
</tr>
</thead>
<tbody>
<tr>
<td>Our</td>
<td>3.22</td>
<td>4.27</td>
<td>0.80</td>
<td>1.00</td>
</tr>
<tr>
<td>Disp. v2</td>
<td>2.37</td>
<td>3.09</td>
<td>0.70</td>
<td>0.80</td>
</tr>
<tr>
<td>MCNCC</td>
<td>2.43</td>
<td>3.63</td>
<td>0.70</td>
<td>0.90</td>
</tr>
<tr>
<td>PRSM</td>
<td>2.78</td>
<td>3.00</td>
<td>0.70</td>
<td>0.70</td>
</tr>
<tr>
<td>OSF</td>
<td>3.28</td>
<td>4.07</td>
<td>0.80</td>
<td>0.90</td>
</tr>
</tbody>
</table>

8 CONCLUSIONS

The proposed algorithm delivers top performing results even though only one global hypothesis is used (eliminating the need to update multiple hypotheses), and no convolutional neural network (e.g. Zhang et al., 2015; Zbontar and LeCun, 2015; Guney and Geiger, 2015) or prior 3D models (e.g. cars) are used. The use of r-sampling and P-sampling are novel, simple and effective ways of simulating a propagation scheduler, which can be executed in parallel, unlike those from (Bleyer et al., 2011; Besse et al., 2012; Zhang et al., 2015). The proposed similarity function is also capable of reducing some of the loss of detail and error caused by the popular adaptive window approach.
REFERENCES


