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A Generic Framework and Library for Exploration of Small Multiples through Interactive Piling

Fritz Lekschas, Xinyi Zhou, Wei Chen, Nils Gehlenborg, Benjamin Bach, and Hanspeter Pfister

Fig. 1. Exploring Small Multiples through Visual Piling. (A) An example of thousands of necklace sketches from Google Quickdraw [25] displayed as small multiples. The interactive arrangement, grouping, and aggregation of small multiples into piles support the discovery and comparison of recurring patterns. (B) Other types of small multiple visualizations grouped and aggregated into piles, including (from left to right) natural and immunofluorescence microscopy images, matrices, area charts, and scatterplots.

Abstract—Small multiples are miniature representations of visual information used generically across many domains. Handling large numbers of small multiples imposes challenges on many analytic tasks like inspection, comparison, navigation, or annotation. To address these challenges, we developed a framework and implemented a library called PILING.JS for designing interactive piling interfaces. Based on the piling metaphor, such interfaces afford flexible organization, exploration, and comparison of large numbers of small multiples by interactively aggregating visual objects into piles. Based on a systematic analysis of previous work, we present a structured design space to guide the design of visual piling interfaces. To enable designers to efficiently build their own visual piling interfaces, PILING.JS provides a declarative interface to avoid having to write low-level code and implements common aspects of the design space. An accompanying GUI additionally supports the dynamic configuration of the piling interface. We demonstrate the expressiveness of PILING.JS with examples from machine learning, immunofluorescence microscopy, genomics, and public health.

Index Terms—Information visualization, small multiples, interactive piling, visual aggregation, spatial organization.

1 INTRODUCTION

In many disciplines, datasets consist of large numbers of elements, pattern instances, or dimensions. For instance, in supervised machine learning, researchers compile sets of photos to train and validate machine learning models; in genomics, computational biologists study visual patterns that act as proxies for biological features; in public health, medical experts try to correlate different measurements to health conditions of their patient cohort.

Small multiples [45] are a widely used visualization technique to display such datasets through a series of miniature visualizations that show different facets or subsets of the data. However, as the number of small multiples grows, comparison and exploration can become inefficient due to the decreasing availability of screen real estate per visualization and the increasing efforts for sequential scanning. Subsampling or filtering can help to limit the number of small multiples but might obscure important characteristics of the dataset. Summary visualizations can alleviate this problem by aggregating subsets of the data into a single visualization. However, the analyst needs to know upfront how to organize the dataset into subsets. Without interactive features, exploration with summary visualizations can be limited when there are many potentially interesting facets or subsets to explore.

We propose a generic framework for exploring large numbers of small multiples through interactive visual piling. Inspired by how physical piles enable casual organization [35] of paper documents, piling in visualization affords spatial grouping of visual elements into piles that can be arranged, browsed, and aggregated interactively. By combining the benefits of small multiples and visual aggregations with interactive browsing, piling can be an effective technique for exploring small multiples. For instance, in Fig. 1A, we demonstrate how piling enables the discovery and comparison of shared concepts of necklace sketches through interactive arrangements, groupings, aggregation, and browsing. Currently, piling has been applied to matrix visualizations by ad-hoc domain-specific methods to explore set typed data [45], dynamic
networks [3], and matrix patterns [31]. But there are many more scenarios where interactive visual piling can be useful for exploration, as shown in Fig. 1. However, developing a new piling system for every use case would be time-consuming. Moreover, many concepts of piling are independent of the domain, data type, and visual encoding.

We present the first overview of interactive visual piling as a method for the exploration of small multiples. Based on a systematic analysis of previous work, we define a design space according to five analytical tasks that any piling interface should support: grouping, arrangement, previewing, browsing, and aggregation. We focus on analytical tasks to study how different visual encoding and interaction approaches support the exploration of small multiples. Our design space provides guidance for the design of future piling interfaces. To streamline the implementation of piling interfaces, we developed PILING.JS—a JavaScript-based library that provides solutions for many common aspects of our design space. PILING.JS is built around a data-type independent rendering pipeline and a declarative view specification to avoid having to write low-level code for handling the interactive piling interface. Using PILING.JS, we demonstrate the generality of interactive piling for exploring small multiples and the expressiveness of our library with examples from machine learning, immunofluorescence microscopy, geographic information systems, proteomics, and genomics code of PILING.JS is freely available under a permissive open source license at https://github.com/flekschas/piling.js and features extensive documentation and examples at https://piling.js.org.

2 RELATED WORK

Small Multiples. Small multiples [46] are a series of miniature visualizations that show different facets or subsets of a dataset or different instances of a pattern type. Small multiples afford direct visual comparison and are, for example, used for multifaceted exploration [7,21], analyzing temporal data [10,40], parameterization [24,36], or as a general exploration method for visual analytics [47]. Small multiple designs are conceptually similar to glyph design [41] as the reduced availability of screen real estate render glyphs useful. Typically, small multiples are positioned in a grid or data-driven layout [44,49] that the user cannot manipulate directly. With visual piling, the goal is to enhance small multiples to support interactive grouping and aggregation of large numbers of small multiples for scenarios that require comparisons across a multitude of facets and subsets of the data.

Piling for Document Organization. Piling is a technique for the spatial visualization of documents. Based on studying physical piling, Thomas Malone [34] suggests that piling is cognitively easier than filing as it only involves loose classification of documents. In a study conducted by Whittaker and Hirschberg [51], physical piling resulted in more frequently-browsed data collections compared to a folder-based exploration approach. Mander et al. [35] introduced piling as a technique for casual organization of documents in a virtual desktop environment. To address the scalability issues of piling, they experimented with automatic piling strategies and different modes of visually encoding and interacting with piles to aid document retrieval and browsing. In follow-up work [42], they show how automatic piling-based grouping and aggregation can enhance content-aware browsing of virtual document collections. Kim et al. [28] employed visual piling for browsing photos and found automatic piling to be as efficient for search as manually sorting and more efficient compared to automatically ordering. In this work, we are expanding the piling approach for casual document organization into a generic technique for interactive visual aggregation.

Interacting with Visual Piles. In the human computer interaction community, several projects explored interaction techniques for interactive browsing of document-based piles. For instance, using a 3D virtual desktop environment called BumpTop [1], Agarawala et al. studied and implemented several pen-based interaction techniques for a tabletop display. BumpTop explores leafing through items like one would leaf through pages of a book, partially dispersing piles to see individual items better, or temporarily dispersing piles into a grid of items to avoid any overlap. Alikakseyeu et al. [2] have further studied pen-based interaction techniques for browsing piles and found dispersing to be most effective. Other work explored the space of tangible interactions with piles in a mixed-reality environment such as digital tabletops [27] or bendable e-ink displays [19].

Additionally, Bauer et al. [50] have explored spatial arrangement techniques for piling in Dynapad, where a pile is more loosely defined as a spatially-constrained set of visual items. Items must not necessarily overlap, which allows for continual exposure of items but requires more space and does not support aggregation. Another interaction technique for spatially organized items, called Bubble Clusters [50], is built on the implicit formation of groups based on their spatial proximity. WallTop [8] implements a similar approach, where overlapping windows feature an outline that allows for group-based spatial positioning via drag-and-drop. We analyzed this work to identify common gestures for interaction, which we implemented in PILING.JS.

Piling for Information Visualizations. In information visualization, visual piling is used for comparison. Tominski et al. [45] developed a generic interactive technique for pairwise comparison of information visualizations inspired by how people compare physical sheets of paper. Their technique is similar to piling for pairwise comparisons, but it does not visually or interactively scale to more than two items. Beyond this work, piling has mainly been applied to matrices for visual aggregation. For example, the Onset [43] technique implements a piling interface to interactively aggregate binary matrices for comparison. Bach et al. extended this approach to dynamic networks in Small Multiples [3] for detecting states over time. Importantly, Bach et al. introduced the notion of a preview representation for items, which they implement as one-dimensional aggregates of the 2D matrix to aid browsing. In HiPiler [31], the idea of piling is further generalized to support one-, two-, and multi-dimensional arrangements. Vogogias et al. [48] and Fernandez et al. [17] have applied similar matrix-based visual piling ideas to other applications in biology and software evolution. Finally, Lekschas et al. [30] use piling to guide navigation in multiscale visualizations by aggregating overlapping patterns into piles and displaying them as insets.

In general, visual piling is an approach to reduce clutter [15] through interactive aggregation. In this paper we demonstrate the usefulness of piling and generalize the piling approach beyond matrix visualizations.

3 THE VISUAL PILING APPROACH

Visual piling is an interactive approach for organizing, exploring, and comparing small multiples. Piling is centered around the act of spatially positioning items on top of each other, which together form a pile, and arranging these piles meaningfully to support effective comparison.

3.1 Elements and Properties of a Visual Pile

Inspired by physical piles of paper documents, we define a pile as a group of partially-occluded small multiples that results from piling up individual items, illustrated in Fig. 2. Given the partial overlap, only a single item is shown in its entirety, which we call the pile cover. As the remaining items are only partially visible, we refer to them as previews. While there are many ways of visually representing a pile, we distinguish piles from other forms of spatially-arranged small multiples by the following set of properties, which builds upon the description of a physical pile from Bauer et al. [6].

Occlusion & Connectedness. Items that comprise a pile should occlude each other partially to form a single mutually-connected unit. However, piles can temporarily be dispersed for exploration.

Identity. A pile must differentiate itself visually from a single item. There are different visual encodings to identify a pile, like a label indicating the number of items on a pile, superimposed semi-transparent images, or items that are offset relative to each other.

Cohesion. Items on a pile should act as a single element during the exploration. Cohesive behavior does not mean that access to individual items is lost upon grouping items into a pile. However, a pile should reflect the notion of a group when interacting with the piling interface.

Transience. Piling should be seen as a dynamic process where the piling state can change frequently. In contrast to other aggregation techniques, the goal of piling is to compose and disperse piles interactively...
While symbol-based cluster plots are highly scalable, they do not reveal A common approach to uncover similarities within large and high-
dimensional data collections is to arrange ($T_2$) the items as a two-
dimensional embedding for cluster analysis (Fig. 1A2). We arranged
multiples (Fig. 1A1 left) allows us to assess and compare individual
items implicitly form groups perceptually. However, implicit grouping
uses the Gestalt principle of “proximity,” which states that nearby
items are treated as parallel or sequential, is swiping [31], where the user moves
two or more items to be piled up at the same time. While multi-select grouping does not result
in intermediate groupings, the sequence of selected items can still be
reflected, given the order of selected items. In contrast, parallel
grouping techniques allow two or more items to be piled up at the same time.
For instance, many piling interfaces support region-based grouping via
lasso techniques [1, 31]. Parallel grouping does not afford temporal
organization as the order in which multiple items are grouped together
is not explicitly defined. A special form of grouping, which can be
treated as parallel or sequential, is swiping [31], where the user moves
the mouse cursor or pen over each item to be grouped. Swiping enables
more precise selections in dense arrangements like cluster plots.

4.2 Arrangement
For arrangements (T2), we consider the relative positioning of items
on a pile and the absolute positioning of piles (Fig. 3 Arrangement).

3.2 Goals and Tasks
Even though the application-specific goals differ, we identify two over-
arching goals for interactive visual piling interfaces from related work.
(G1) Visual piling is a tool for organizing data collections into subsets
to reduce complexity. This includes, for example, to sort items into
groups, categorize groups based on their content, or filter out subsets
of items for quality control. (G2) Beyond organization, visual piles are
a means to explore and compare individual items and groups of items
to each other. Specifically, one might want to determine the primary
topic of a group, identify outliers, or discover trends.

To identify the common tasks needed to support organization, ex-
ploration, and comparison, we systematically reviewed related work.
Following an open-coding approach, the first two authors coded all
17 piling-related papers from Sect. 2 according to their application-
specific tasks independently. We focused our coding efforts on the role
of interactive piling to not confuse piling-specific with unrelated tasks.
After coding the papers, the first two authors resolved disagreements.
Subsequently, we generalized the assigned codes into five high-level
analytic tasks that any interactive visual piling interface should support.

T1 Grouping: manually or automatically sort items into piles.
T2 Arrangement: position items and piles relative to each other in
an orderly, randomized, gridded, or unconstrained layout.
T3 Previewing: identify and locate items on a pile using in-place,
gallery, foreshortened, combining, and indicating previews.
T4 Browsing: search, explore, and navigate within and between piles
through in-place, dispersive, layered, and hierarchical browsing.
T5 Aggregation: summarize a pile into a synthesized, representative,
or abstract representation.

To study how different visual encoding and interaction approaches
support the exploration of small multiples, we use these five analytical
tasks to structure the design space exploration [Sect. 4] and to guide
future piling designs.

3.3 Usage Scenario
To exemplify how visual piling enhances the exploration of small
multiples, we describe a typical usage scenario following the example
of necklace sketches from Google Quickdraw [23] (Fig. 1A), which we
also demonstrate in the supplementary video. One goal in analyzing
large collections of visual objects is to identify and compare trends
within the dataset. Inspired by Forma Fluenta [37], we are trying to
find recurring pattern concepts. Visualizing the sketches as small
multiples (Fig. 1A1 left) allows us to assess and compare individual
sketches, but it does not support the discovery of shared concepts.
A common approach to uncover similarities within large and high-
dimensional data collections is to arrange (T2) the items as a two-
dimensional embedding for cluster analysis (Fig. 1A2). We arranged
the items by a UMAP [38] embedding of image features that were
learned with a convolutional autoencoder. In the resulting cluster plot,
items can be represented as a symbol (e.g., a dot) or a small thumbnail.
While symbol-based cluster plots are highly scalable, they do not reveal
the visual details of a cluster. On the other hand, thumbnail-based

cluster plots do not scale to large datasets due to overplotting issues.
Visual piling provides a trade-off by grouping (T1) spatial clusters, i.e., clusters formed by items in relative proximity (Fig. 1A3). By
aggregating (T5) all sketches into an average and showing this average
as the pile cover, we can discover and browse overarching concepts
effectively. For instance, after manually refining the grouping and
arrangement of four piles (Supplementary Figure S1), we can see
that people are sketching a necklace as an open beaded necklace, a
necklace worn around a neck, an open pendant necklace, or a closed
pendant necklace (Fig. 1A4). Visual piling also affords the encoding
of additional information beyond the individual items. For instance, in
Fig. 1A4, we visualize the relative distribution of geographic regions
across a pile using small bar charts below each pile.

4 A DESIGN SPACE FOR VISUAL PILING
This is the first design space (Fig. 3) for visual piling. For each of the
five analytical tasks (Sect. 3.2), we derived general approaches and
common solutions from previous work through multiple discussions
among the co-authors. The resulting subcategories cover overarching
approaches of each task. We generalize these approaches to highlight
categorical differences. Multiple approaches can be combined to offer
different ways of organizing and exploring small multiples. In our
design space, we cover the relevant visual encodings and interactions.
We also describe common gestures for triggering interactions but do
not attempt to provide a complete overview of all possible gestures.

4.1 Grouping
We distinguish between manual and automatic grouping (T1), as ex-
emplified in Fig. 2 Grouping. Manual grouping requires the user to
interactively determine which items should be grouped and, potentially,
in which order. Automatic grouping follows a specific procedure to
group multiple items at once.

Manual. Sequential grouping is the simplest form of manual
grouping. It requires the user to group items interactively, one at a time. This
is typically achieved with a drag-and-drop gesture [13, 31, 35, 36, 50].
While sequential grouping requires more time, it enables temporal
organization. For instance, the most recently added elements can be
located on top of the pile. For efficiency, one can also form a group from
multiple selected items. While multi-select grouping does not result
in intermediate groupings, the sequence of selected items can still be
reflected, given the order of selected items. In contrast, parallel
grouping techniques allow two or more items to be piled up at the same time.
For instance, many piling interfaces support region-based grouping via
lasso techniques [1, 31]. Parallel grouping does not afford temporal
organization as the order in which multiple items are grouped together
is not explicitly defined. A special form of grouping, which can be
treated as parallel or sequential, is swiping [31], where the user moves
the mouse cursor or pen over each item to be grouped. Swiping enables
more precise selections in dense arrangements like cluster plots.

Automatic. Many piling interfaces support automatic grouping to
improve scalability. Layout-driven grouping is based on an explicitly-
or implicitly-defined layout. Items that are located within the same
unit of the layout can then be grouped. Such units can, for instance,
be the rows, columns, or grid cells [31]. Proximity-based grouping
uses the Gestalt principle of “proximity,” which states that nearby
items implicitly form groups perceptually. However, implicit grouping
can cause uncertainty in subsequent pile interactions [35] as it is not
always possible to infer the grouping state as perceived by the user [6].
Therefore, most piling interfaces only use proximity to trigger explicit
grouping, e.g., by outlining the pile bounds [35, 50] or merging nearby
items [50]. Finally, in similarity-based grouping, items are merged
automatically based on some notion of similarity. While there are many
different ways of measuring similarity, fundamentally, the similarity
can be derived from the items [28, 31, 42] or related metadata [31].

Elements and Properties of Visual Piles. To illustrate key
properties of piles, we differentiate between individual items and piles.

Fig. 2. Elements and Properties of Visual Piles. To illustrate key
properties of piles, we differentiate between individual items and piles.

rather than to just consume a static grouping state. However, this does
not mean that piles cannot persist.

While sequential grouping requires more time, it enables temporal orga-
ning techniques allow two or more items to be piled up at the same time.
In contrast, multi-select grouping does not result


**Item arrangement.** A random item arrangement is characterized by non-deterministic offsets and rotations of the items. Such arrangements make the visual pile closely resemble a physical pile, which can be useful to distinguish between automatically- and manually-composed piles [33]. Random item arrangements can also encode access patterns, such as the frequency of file access [14]. Finally, a pseudo-random item arrangement can be the result of sequential grouping. Since it is unlikely that the user will stack items in a pixel-precise manner, the resulting offset can appear random. Nevertheless, the offset can provide meaningful cues to the pile creator [34] for browsing (T4). In contrast, orderly item arrangements are the result of automatic and deterministic positioning. Such arrangements enable controlling how much each item is overlapped, which is useful for comparing items [3, 31]. When the item offset follows a single direction, in-place browsing can be efficient as the cursor movement is minimal. Also, orderly arrangements typically follow the Gestalt principle of “continuation” to foster perceptual grouping.

**Pile Arrangement.** Dividing the canvas into rows and columns of a specific size leads to a gridded pile arrangement. Gridded arrangements are useful for comparing piles due to the alignment. Imposing a specific ordering onto the pile can highlight temporal or sequential patterns. The simplest form of a gridded pile arrangement is a one-dimensional timeline [6, 28] but two-dimensional grid layouts are more common to make use of the entire screen [13, 31]. Finally, as precise pile arrangements, we summarize manual, layout-driven, or data-driven arrangements that require a pixel-precise positioning on the canvas. In this regards, automatic arrangements can incorporate one-dimensional [6], two-dimensional [31], or multidimensional [31] scatterplots. The position can also be inherent to the items themselves, which is, for example, the case for exploring annotated pattern instances [30].

4.3 Previewing

To afford content-awareness, visual piles can implement different layout types to support previewing items (T3), as shown in Fig. 3 which is key to support effective exploration and navigation (T4). Partial. Inspired by physical piling, partial previewing of items arises naturally and is implemented in many piling interfaces [1, 2, 5, 27, 28]. The effectiveness depends on the data type and the size of the partial previews.

Gallery. When the partial overlap severely limits the perception of the item’s content, one can opt for a gallery preview where a small number of items or aggregates [30] is shown in a regular grid. This approach can be useful for datasets in combination with a representative aggregation approach (Sect. 4.5).

Foreshortened. To limit the size of a pile while still providing item-specific previews, previews can be foreshortened along one axis. Such previews can be implemented with perspective distortion [1], compression, or aggregation along one dimension [3, 17, 30, 31, 38]. While the first option can provide cues for search and navigation (T4), the latter enables more effective comparison between alignable items.

Combining. When working with items that have a sparse visual representation and shared axes, like scatterplots, line charts, or bar charts, multiple items can be combined to provide an overview. A combined preview can be the result of superimposing items with a transparent background or through dedicated aggregation [43]. While this approach is space-efficient, the relationship between the overview and individual items might get lost without employing other means of previewing items.

Indicating. To maximize space efficiency while still hinting at an item’s content, one can provide abstract indicators as item previews. Most common indicators are implemented as tabs [23, 43], but the indicator can be more abstract, e.g., a small dot. While indicators do not directly preview the content, they afford browsing (Sect. 4.4) and can encode metadata like the distribution of items.

4.4 Browsing

In the context of visual piling, we regard browsing (T4) as the act of inspecting the visual details of piled items (Fig. 3 Browsing). Since browsing requires interaction, the applicability of different browsing approaches depends on the type of preview.

In-Place. Inspecting the visual details of an item in-place is a fast browsing approach as the arrangement of items remains unchanged. To show an item in its entirety, the ordering of items is altered temporarily such that the browsed item is shown on top [1, 2, 23]. A variation of in-place browsing shows the browsed item next to the pile as an inset [35]. Another in-place browsing technique called “leafing” [1, 5, 30, 31] involves interacting with foreshortened previews. Upon interaction, foreshortened previews can either be expanded to their full extent or shown on top of the pile, similar to flipping through the pages of a book. Typically, in-place browsing is triggered by moving the pointing device over the preview item to be shown in its full extent [1, 2, 23, 30, 31, 35].

Dispersive. Dispersive pile browsing techniques temporarily disperse a pile such that the overlap between items is resolved partially or entirely, allowing for subsequent comparison of the items. To aid maintaining a mental map of the items on a pile, many dispersive techniques use the same type of layout for positioning the dispersed items and only increase the spacing between items [1, 2, 50]. A more disruptive approach arranges the dispersed items into a regular grid [1, 26]. Pile dispersion is often triggered by a double click or tap [2, 3, 31, 50], but many gestures have been explored too including horizontally moving a pointer device back and forth [35], hovering over a pile [1], and context-menu induced dragging gestures [1]. Finally, an indirect way...
of dispersive browsing employs a zoom gesture in combination with automatic proximity-based grouping [30][39]. Thereby, piles gradually disperse as the user zooms into a specific region.

Layered. Increasing numbers of small multiples limit the available space for visual browsing. Layered browsing techniques temporarily hide other items and, thus, give more space to the browsed piles. Layering can be combined with dispersive browsing to support flexible pile exploration and sub-piling [31].

Hierarchical. Finally, for piles of many items, it can be ineffective to browse all items at once. Instead, hierarchical clustering can be employed to enable hierarchical browsing such that the pile only disperses into a subset of piles from the next hierarchical level.

4.5 Aggregation

Aggregation (T5) is the act of summarizing piled items into a concise form (Fig. 3 Aggregation). The goal of aggregation is to improve the content awareness when previewing a pile and aid comparison between groups of items. Therefore, the choice of the aggregation method depends on the layout type for previewing.

Synthesized. We call aggregation techniques that create a single image from a group of items synthesized aggregations. Hereby, the resolution or granularity of the aggregate is identical to the items. Summary statistics are commonly used for synthesized aggregations [3][30][31][43][48] but other methods are possible. When the aggregate presents new or unseen information, it is useful to provide some means of previewing individual items [3][31][43] to enable item-specific comparisons.

Representative. For data types where individual items do not align well, such as natural images, synthesized aggregations are typically ineffective. Instead, the pile can be summarized by a single or multiple representative items which are typically visualized as gallery previews [30]. Through careful sampling, the selection of representative items can provide enough information to inform the user about a pile’s primary content.

Abstract. Finally, for non-alignable but well-defined data, one can employ abstract aggregation techniques. The goal of such techniques is to provide a simplistic or schematic representation of the pile’s content where the resolution or granularity is reduced compared to the items. Simplistic aggregations provide limited content awareness. However, the aggregation can, nevertheless, hint at the category or type of items on a pile, which can be useful for navigation (T4).

4.6 Additional Pile Encodings

Several additional style properties (Fig. 4) can be employed to encode related information such as the pile or item size, item access patterns, or categorical information.

Coloring. To highlight trends within a group of piled items, one can adjust the lightness [35] or apply other color filters. While potentially effective at encoding additional information, extreme color adjustments can harm content awareness and should be used with caution.

Scaling. Scaling the visual pile size in the x,y [30] or z-direction is another approach to encode additional information. Z-scaling requires that items are represented as three-dimensional objects. If applied, z-scaling can also afford edge browsing, which is an in-place browsing technique for physical piles [35].
Fig. 6. Rendering Regimes. Static renderers are easy to set up but offer limited support for aggregation. Dynamic renderers can be complex but support dynamic updates (e.g., color scaling) and aggregation.

asyncronous executions in JavaScript. The texture resources must be one of the following media types: an image, canvas, or video element. Since many web-based visualizations render SVGs, PILING.JS provides a predefined SVG renderer that accepts an SVG string or element as input. Using the SVG renderer, it is easy to render any static D3 visualization in PILING.JS. PILING.JS also includes a predefined matrix renderer and supports PixiJS [20] WebGL programs as a renderer for dynamic re-rendering (Fig. 6 right). To support gallery previews, PILING.JS implements meta renderers, which compose multiple images into a single image. These renderers rely on a representative aggregation approach. For convenience, PILING.JS provides a built-in renderer that composes multiple items into a gallery (Fig. 7). In general, each built-in renderer can be replaced or configured for customization.

Aggregators. To support foreshortened item previewing or pile aggregations, the designer needs to specify an aggregator function for items or piles. The aggregator either receives as input a single item or multiple items and returns a single data source that is subsequently passed to the related renderer. By decoupling renderers and aggregators, both can be reused without having to adjust them. Also, not all types of item previews require aggregation. For synthesizing aggregation, PILING.JS provides a set of predefined matrix aggregators that supports common summary statistics (mean, variance, and standard deviation). For representative aggregation, PILING.JS implements a generic cluster-based approach that employs k-means clustering as the computation is fast enough to not cause noticeable delays. We pick the k items that are closest to the k centroids from k-means as the representative images.

5.2 Pile Encoding via View Properties
PILING.JS offers many view properties to specify the arrangement, previewing, and visual encoding of piles (Supplementary Figure S2). For a complete overview of all view properties, please refer to https://piling.js.org. View properties are set via PILING.JS’s set method, which receives as input the property name and value. In general, there are three types of view properties in PILING.JS, which related to our data model (Sect. 5.1), global, pile-specific, and item-specific view properties. Global properties relate to the entire piling interface and do not change during interactive grouping. For instance, set(‘columns’, 10) sets the number of columns to 10. In contrast, pile- and item-specific properties can depend on the grouping on the pile, i.e., the state of grouping, and therefore support dynamic specifier functions (Fig. 8). For instance, the pile border size could be a function of the number of elements on a pile. Inspired by D3 [9], PILING.JS implements a declarative data-driven interface to dynamic properties by passing the specific items and piles to the specifier function. Using this approach, the designer only needs to specify how to translate the data object into a property value, while PILING.JS visually renders the property. Dynamic pile-specific properties are invoked for every pile. They receive the current pile object and return a corresponding property value. Item-specific property specifiers are invoked for every item on a pile as the pile’s composition changes. The specifier function receives an item’s data object, index, and corresponding pile object, and returns the property value (Fig. 8 bottom-right).

5.3 Pile Interactions
While visual piling is agnostic to the input device (e.g., mouse, pen, or touch), PILING.JS currently focuses on mouse interactions and implements general mouse gestures found across several related works (Sect. 4) for manual grouping, arrangement, browsing, as well as methods for automatic grouping and arrangement.

Gestures for Manual Interactions. PILING.JS implements common gestures for grouping and arrangement (Sect. 4). Piles can be arranged manually via a drag-and-drop gesture. For sequential grouping, an item or pile needs to be dropped onto another item or pile (Fig. 9 top-left). To group multiple items at once, PILING.JS offers a lasso tool. The lasso is initiated by clicking into an empty region of the canvas. Subsequently, a circle will appear (Fig. 9 bottom-left). By clicking into this circle and holding down the primary mouse button, the user can start the lasso selection. All items located within the lasso area are grouped upon releasing the primary mouse button. For browsing (Sect. 4.4), PILING.JS implements gestures for in-place, dispersive, layered, and hierarchical browsing. In-place browsing is triggered by a click on a pile and moving the mouse cursor over the previews. Double-clicking on a pile will temporarily disperse a pile into a regular grid, as shown in Fig. 9 top-right. To browse a pile in layers, the user can activate the pile’s context menu (Fig. 9 top-right) and select “browse separately.” The browsed pile is additionally dispersed on the next layer to support rapid sub-piling.

Automatic Grouping and Arrangements. To support automatic grouping and arrangement, PILING.JS features a groupBy, splitBy and arrangeBy method. The groupBy method enables layout-, proximity-, and data-driven groupings, as described in Sect. 4.1. As a complement, the splitBy method can split piles based on their position and data properties of items. Finally, the arrangeBy method enables automatic pile-specific arrangements. All these methods rely on a type and an objective. The type determines the subroutine to be used and the objective provides the necessary data to execute this subroutine.
For an example, see Supplementary Figure S3. Currently, groupBy supports proximity-based (distance and overlap), layout-driven (grid, column, and row), and similarity-based (category and cluster) grouping. For instance, groupBy(‘category’, ‘country’) will group all items of the same country, assuming that the items contain a property called country. We chose this API style to keep the number of public API methods small. The splitBy method supports the same proximity- and similarity-based subroutines for splitting piles. The arrangeBy offers coordinate-based (xy, ij, uv, and index) and data-driven (data) layouts, e.g., arrangeBy(‘data’, ‘size’) will order items by a property called country. Finally, the proximity-based groupBy subroutines can be re-evaluated automatically upon zooming, as the proximity between items might have changed. Similarly, the arrangeBy subroutines can be re-evaluated automatically after grouping piles.

5.4 Adjust and Explore the Piling Interface via a GUI

PILING.js provides a mid-level API, which hides the state and rendering aspects of visual piling but relies on the designer to implement the rendering pipeline programmatically. As we worked on the use cases (Sect. 6), we realized that switching between a text editor and the browser to parameterize view specification can be time-consuming since the visual feedback is delayed until the browser refreshes. Therefore, as shown in Fig. 10 we provide a simple yet effective GUI to allow the designer to adjust various view properties dynamically.

Currently, the GUI features elements for adjusting static property values such as Boolean flags, single or multiple selections, or numerical values. The GUI also has support for triggering groupings and arrange- ment operations. Finally, given the breadth of view properties, it is infeasible to cover every possible setting. Therefore, PILING.js allows the designer to specify custom settings (Fig. 10 bottom-right).

5.5 Implementation

PILING.js is implemented in JavaScript using PixiJS for WebGL rendering. We chose PixiJS for its highly-optimized 2D texture rendering and flexible mid-level API, which greatly simplifies the development of WebGL programs. The source code of PILING.js is free and open-source available at `https://github.com/flekshaas/piling.js` and features extensive documentation for all available view configurations.

5.6 Performance Evaluation

PILING.js is designed to support datasets of up to a few thousand items. In the following, we evaluate the initialization time and frame rate (Fig. 11). The initialization time includes the library’s startup time, data rendering, and item creation. We compare the time for loading items of the following media types: images, canvas-derived textures, and WebGL programs. For the frame rate, we compare navigation, arrangement, and grouping animations (i.e., animated transitions of the piling state triggered by scripted interactions) using the example from Fig. 1. Specifically, we examine scrolling, pan-and-zoom, automatic arrangements of all items, and lasso-based grouping, which cover the essential core interactions. We repeated each animation ten times and measured the duration in seconds and frame per second (FPS) in Chromium (v80) on a 2016 MacBook Pro.

![Frame Rates](image1.png)

Fig. 11. Performance Evaluation. Construction time (smaller is better) and frame rate (higher is better; 60 FPS is the best) as a function of the number of items for different media and interaction types. Loading 5,000 dynamic WebGL renderers (‘X’) was not feasible as the browser timed out. Error bars show standard deviation.

As shown in Fig. 11, the initialization time increases with the number of items but remains acceptable until 1,000 items. The media type and size of the items greatly influences the initialization time. Especially the custom WebGL programs take longer to initialize. The frame rates for scrolling and pan-and-zoom interactions with datasets of up to 1,000 items is smooth but starts to degrade significantly for datasets larger than 2,000 items. As the arrangement and grouping animations are more involved, their frame rates are lower but remain acceptable for up to 2,000 items.

6 USE CASES

In the following section, we present several use cases to demonstrate the generality of the visual piling approach and the expressiveness of our PILING.js library for exploring large collections of small multiples. The use cases are also available online at `https://piling.js.org`.

Compiling Training Data for Machine Learning.

A critical aspect of machine learning research, especially deep learning, is the composition of training and validation datasets to probe machine learning models. For instance, in computer vision research, this involves collecting, sorting, and selecting images. While several collections of annotated images exist for comparison and benchmarking, subsets are often used during the initial development of the model for exploration. Creating these subsets is not trivial as nuanced image features might not have been extracted, and formal categorization of every potential interesting feature is prohibitive. Visual piling can address this issue by allowing users to sort existing datasets into subsets (T1) for rapid hypothesis testing. For example, in Fig. 12, we sampled 2,000 images of cars in context from the Microsoft COCO dataset that can be used to train car detector models. Browsing all images provides a first overview. Using the given object approach, the designers can easily adjust view properties such as sorting, filtering, and grouping.

![Compiling Natural Images from the COCO dataset](image2.png)

Fig. 12. Compiling Natural Images from the COCO dataset. All images (1) contain car annotations, but only a subset of them show a car prominently. (2) Arranging the images by their primary annotation type and relative annotation size improves the explorability.
annations, we can arrange (T2) the images in a two-dimensional grid by their primary category (x-axis) and relative size of the annotation in pixels (y-axis). Google Facets [21] allows for similar arrangements but requires zooming as the number of items increases. With PILING.JS, we can instead group all items that are located within the same grid cell into piles, which provides visual cues about the groups’ content and the ability to compose new groups manually.

**Exploring Instance Annotations in Large Images.** One aspect of analyzing large image data involves the exploration of instance annotations. For example, in cell biology, researchers annotate cell boundaries in immunofluorescence microscopy data of tissues or cell cultures. The goal of visual exploration is to compare and organize cells to each other for quality control and stratification (T1). Using a conventional small-multiples approach can be limiting when there are several potentially-interesting arrangements. In Fig. 13, we show an exploration of a microscopy image from Codeluppi et al. [12]. Since the cells were clustered based on their gene expression profiles, we arranged cells by the gene expression data reported in the original paper (T2). As the cell bodies do not align well, we show a gallery preview of representative images (Fig. 13.2 and 3) as the pile cover to highlight the diversity of cell images across the pile (T5). Additionally, we preview individual cell annotations as one-dimensional heatmaps (T3) above the cover, which show the cells’ gene expression profiles. This enables us to correlate the cell morphology to the gene expression data.

**Comparing Repeated One-Dimensional Measurements.** Comparing one-dimensional repeated measurements with small multiples typically involves the alignment of items along a shared axis to discover patterns (T2). For large numbers of repeated measurements, it can be beneficial to explicitly group measurements to emphasize trends and to interactively change the grouping to highlight different patterns between subsets of the data. For example, in Fig. 14, we loaded the global surface temperature anomaly dataset from NASA [13]. This dataset contains surface temperature measurements for each month across 14 decades (the 1880s to 2010s) that is normalized by the mean temperature of 1951-1980. We plotted the mean temperature deviations from -1.5 to +1.5 degrees Celsius for each month of the 14 decades (Fig. 14.1). Grouping the plots by decades or months, and arranging them by a vertical offset enables us to dynamically create ridge plot-like piles. Positioning the piles next to each other makes it easy to compare decennial (Fig. 14.2) and monthly trends (Fig. 14.3). We can now immediately see how the temperature increased over the last 140 years.

**Movie Analysis.** When analyzing movies, it can be insightful to study the visual similarity of scenes. To compare the similarity between frames, Bach et al. [4] folded a linear curve, called a time curve, in 2D space using a dimensionality reduction technique. In Fig. 15.1, we loaded 365 frames from a movie showing the annual precipitation cycle of the United States [11] (one frame per day). Based on the similarity between each frame, we embedded the frames into a two-dimensional space with UMAP [38] (Fig. 15.2). After arranging the frames by their embedding (T2), we can highlight the annual precipitation cycle and several clusters of highly similar frames. Visualizing the frames as thumbnails shows what these clusters represent. As the high number of frames makes it hard to compare individual frames, we grouped overlapping frames into piles to simplify the view (T1), which highlights nine visually distinct precipitation patterns (Fig. 15.3). Additionally, we encode the frame order via the border color (which ranges from light gray (January) to black (December)) and connect the piles with a line visualization to foster the connection to the underlying sequence of the movie. This line visualization is realized with D3 [9] and linked to the pile interface.

**Time Series Analysis.** When dealing with time series, an important task is to identify overall trends and variations. To see and make sense of any trends, one must be able to compare individual items. Visual piling can address this challenge through content-aware browsing (T4). In Fig. 16, we plot the fertility rate (x-axis) against life expectancy (y-axis) from Worldbank [52] from 1960 to 2017 as small multiples, resolved by country and colored according to the geographic region. After grouping (T1) European countries (Fig. 16.2), we can see that, over time, the fertility rate lowers while the life expectancy increases, as shown by color gradient going from bright (1960) to dark (2017). To support comparing individual years without having to split the groups,
we render small rectangles next to a pile as indicating previews (T3) of the years. By leafing through the rectangles (T4), the year’s corresponding scatterplot is revealed, which allows us to trace the temporal development (Fig. 16.3 top). Upon manually grouping scatterplots, we aggregate (T5) the data into a combined and connected scatterplot (Fig. 16.3 bottom), which is shown as the pile cover, to allow tracing the development of individual countries. By piling up the years 1960 and 2017 of North America and East Asia, we can see the alignment of countries in both regions (Fig. 16.3 bottom).

Pattern-Driven Navigation in Multiscale Visualization. A common challenge in exploring local patterns in multiscale visualization is the lack of visual details at an overview. These details are often needed to decide which region to explore in detail. Lens techniques can be applied to magnify a selected region, but many lens techniques do not scale well to large numbers of local patterns. As shown in Scalable Insets [30], the scalability issue can be addressed by displaying local patterns as insets and grouping those insets into piles upon zooming out. In Fig. 17.1, we show area charts of COVID-19 infection rates as small multiples. By arranging the small multiples according to their geolocation (T2) we can gain an overview of the global spread (Fig. 17.2). To avoid issues of overplotting, we group (T1) overlapping items into piles (Fig. 17.3). Piles are visually represented by a stacked area chart to show the overall regional spread of the virus (T5). The combination of grouping and aggregating provides guidance without introducing severe occlusion. Browsing individual countries (T4), states, or counties is realized by navigating to a specific area. Upon zooming in, piles are automatically split when the items do not overlap anymore, given their original position (Fig. 17.4).

Matrix Pattern Comparison. A common task in analyzing network data involves the detection and assessment of reoccurring pattern instances, known as motifs. When the data is visualized as a matrix, these motifs can be represented as small multiples. In analyzing motifs, single instances provide only limited insight. Instead, the analyst typically needs to compare individual motifs to groups of motifs. Using a piling interface, this comparison can be achieved by interactively grouping and aggregating the patterns into piles. For example, Fig. 18 shows pattern instances from Rao et al. [39], which should show a dark dot in the center and act as proxies for specific biological events. As these instances are retrieved computationally, the goal is to verify if the expected pattern is truly exhibited. Scanning over the small multiples sequentially is time-consuming but highlights differences (Fig. 18.1). Ordering the small multiples (Fig. 18.2) helps to find instances with the expected pattern (T2). By aggregating (T5) all instances and showing the average as the pile cover, we can confirm that, on average, the algorithm works as desired (Fig. 18.3). However, by additionally showing one-dimensional previews on top of the cover, we can identify many outliers, which should be removed prior to subsequent analyses (Fig. 18.3 asterisk). Interactive grouping also enables us to stratify (T1) the pattern collection for more efficient data cleaning (Fig. 18.4).

Fig. 17. Worldmap of COVID-19 Infection Rates. Small multiples of area charts (1) show the number of infected people over time. Arranging the charts geographically (2) and grouping them by overlap (3) highlights infection hot spots without overplotting issues. Upon zooming in, piles are automatically split (3-5).

Fig. 18. Comparison of Matrix Patterns. Small multiples of matrix patterns (1) that are supposed to show a dark dot in the center. Ordering (2), aggregating (3), and grouping (4) through visual piling enables us to discover overall trends and outliers (*).


