



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

Ram-pressure stripping of a kicked Hill sphere

Citation for published version:

McKernan, B, Ford, KES, Bartos, I, Graham, MJ, Lyra, W, Marka, S, Marka, Z, Ross, NP, Stern, D & Yang, Y 2019, 'Ram-pressure stripping of a kicked Hill sphere: Prompt electromagnetic emission from the merger of stellar mass black holes in an AGN accretion disk', *Astrophysical Journal Letters*, vol. 884, no. 2. <https://doi.org/10.3847/2041-8213/ab4886>

Digital Object Identifier (DOI):

[10.3847/2041-8213/ab4886](https://doi.org/10.3847/2041-8213/ab4886)

Link:

[Link to publication record in Edinburgh Research Explorer](#)

Document Version:

Peer reviewed version

Published In:

Astrophysical Journal Letters

General rights

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.



Ram-pressure Stripping of a Kicked Hill Sphere: Prompt Electromagnetic Emission from the Merger of Stellar Mass Black Holes in an AGN Accretion Disk

B. MCKERNAN,^{1,2,3} K.E.S. FORD,^{1,2,3} I. BARTOS,⁴ M.J. GRAHAM,⁵ W. LYRA,^{6,7} S. MARKA,⁸ Z. MARKA,⁸ N.P. ROSS,⁹
D. STERN,⁷ AND Y. YANG⁴

¹*Department of Astrophysics, American Museum of Natural History, Central Park West at 79th Street, New York, NY 10024*

²*Department of Science, Borough of Manhattan Community College, City University of New York, New York, NY 10007*

³*Physics Program, The Graduate Center, City University of New York, New York, NY 10016*

⁴*Department of Physics, University of Florida, Gainesville, FL 32611*

⁵*Cahill Center for Astronomy & Astrophysics, California Institute of Technology, 1200 E California Blvd, Pasadena, CA 91125*

⁶*Department of Physics and Astronomy, California State University Northridge, 18111 Nordhoff Street, Northridge, CA 91330*

⁷*Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Drive, Pasadena, CA 91109*

⁸*Columbia Astrophysics Laboratory, Columbia University, New York, NY 10027*

⁹*Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK*

Submitted to ApJL

ABSTRACT

Accretion disks around supermassive black holes (SMBH) are promising sites for stellar mass black hole (BH) mergers due to mass segregation and merger acceleration by disk gas torques. Here we show that a GW-kick at BH merger causes ram-pressure stripping of gas within the BH Hill sphere. If $R_H \geq H$, the disk height, an off-center UV flare at $a_{\text{BH}} \sim 10^3 r_g$ emerges within $t_{\text{UV}} \sim O(2\text{days})(a_{\text{BH}}/10^3 r_g)(M_{\text{SMBH}}/10^8 M_\odot)(v_{\text{kick}}/10^2 \text{km/s})$ post-merger and lasts $O(R_H/v_{\text{kick}}) \sim O(5t_{\text{UV}})$. The flare emerges with luminosity $O(10^{42} \text{erg/s})(t_{\text{UV}}/2\text{days})^{-1}(M_{\text{Hill}}/1M_\odot)(v_{\text{kick}}/10^2 \text{km/s})^2$. AGN optical/UV photometry alters and asymmetric broad emission line profiles can develop after weeks. If $R_H < H$, detectability depends on disk optical depth. Follow-up by large optical sky surveys is optimized for small GW error volumes and for LIGO/Virgo triggers $> 50M_\odot$.

Keywords: accretion – accretion disks – galaxies: active – gravitational waves – black hole physics

1. INTRODUCTION

Advanced LIGO (Aasi et al. 2015) and Advanced Virgo (Acernese et al. 2015) are revealing a surprisingly numerous population of merging stellar mass black holes (BHs; LIGO 2018), including a previously undetected population of black holes with masses $> 20M_\odot$. In the local Universe, BH density seems greatest in our own Galactic nucleus (Hailey et al. 2018; Generozov et al. 2018), consistent with previous conjectures (Morris 1993; Miralda-Escudé & Gould 2000). Thus, a promising channel for the LIGO/Virgo BH mergers are active galactic nucleus (AGN) disks. This is because a fraction of the orbiting nuclear population (including BHs), are geometrically coincident with the AGN disk and an-

other fraction is ground-down into the disk (Syer et al. 1991; Artymowicz et al. 1993; Goodman & Tan 2004). Torques from AGN disk gas drive binary formation, migration, and mergers in these populations (McKernan et al. 2012, 2014; Bellovary et al. 2016; Bartos et al. 2017; Stone et al. 2017; McKernan et al. 2018; Secunda et al. 2019; McKernan et al. 2019). Here we show there can be a prompt, bright UV/optical counterpart from AGN disks after a kicked BH merger. Follow-up by wide-area optical photometric surveys (e.g. ZTF) is optimized for LIGO/Virgo triggers $> 50M_\odot$ with small error volumes. Detection of such signatures would assign specific galactic counterparts to GW sources and probe AGN disk interior conditions for the first time.

2. HILL SPHERE REACTION POST-MERGER

Mass is lost in a BH merger during chirp and ringdown as gravitational waves (GWs) carry away energy and

angular momentum. The final mass M_f is (Tichy & Marronetti 2008)

$$M_f = M_b [1 - 0.2\nu - 0.208\nu^2(a_1 + a_2)] \quad (1)$$

where $\nu \equiv \mu/M_b = q_b/(1 + q_b)^2$ is the symmetric mass ratio of binary $M_b \equiv M_1 + M_2$ where $q_b \equiv M_2/M_1$, and $a_{1,2}$ are the spin magnitudes of masses $M_{1,2}$. Typically $\Delta M \equiv (M_b - M_f)/M_b \sim 0.05$ for $q_b \sim 1$ and small a_1, a_2 . The sphere of influence of a binary BH system of mass M_b in orbit around a super-massive black hole of mass M_{SMBH} is given by the Hill radius ($R_H \equiv r(q/3)^{1/3}$), where r is the semi-major axis of the binary center-of-mass around the SMBH and $q \equiv M_b/M_{\text{SMBH}}$. Post-merger R_H decreases at light speed by

$$\Delta R_H \approx r \left(\frac{M_b}{3M_{\text{SMBH}}} \right)^{1/3} \left(\frac{\Delta M}{3M_b} \right) \approx R_H \left(\frac{\Delta M}{3M_b} \right) \quad (2)$$

for small ΔM . Several effects result. First, gas within the Hill sphere that is orbiting too fast for new mass M_f moves outward, self-colliding. Second, gas formerly inside R_H now collides with gas orbiting the SMBH. Third, the post-merger BH accretes the low angular-momentum component of self-shocked Hill sphere gas in a burst. A jet or beamed outflow adds luminosity $\eta \dot{M}_f c^2$ to the emerging, observable hot-spot outlined below, where η is the accretion efficiency onto M_f .

Separately, a GW-kick at merger (e.g. Baker et al. 2008; Zlochower et al. 2011) causes ram-pressure stripping of the original Hill sphere gas as it collides with a comparable mass of disk gas. Many of these effects have been studied in the context of SMBH mergers in gas disks (e.g. Bogdanović et al. 2008; Kocsis & Loeb 2008; Shields & Bonning 2008; Megevand et al. 2009; O’Neill et al. 2009; Bode et al. 2010). However the physics of the kicked Hill sphere colliding with surrounding gas has no direct analogy in circumbinary disks for SMBH mergers.

2.1. Collisions involving Hill sphere gas

Post-mass loss, parcels of gas within the Hill sphere are at the pericenter of a new, eccentric orbit. The Hill sphere gas will self-collide on timescales $> O(t_{\text{orb}})$ (O’Neill et al. 2009). Supersonic collisions occur deepest in the Hill sphere ($r = R_1 < R_H$), where the collisional Mach number (\mathcal{M}) is

$$\mathcal{M} \approx \frac{1}{2} \frac{1}{(r/R_H)^{1/2}} \frac{q^{1/3}}{r(r_g)^{1/2}} \left(\frac{c}{c_s} \right) \left(\frac{\Delta M}{M_b} \right) \quad (3)$$

where c_s is the gas sound speed and $\Delta v/v_{\text{K,Hill}} \approx \Delta M/2M_b$ where $v_{\text{K,Hill}}(r) = c/\sqrt{r_{g,b}}$ is the gas Keplerian velocity with $r_{g,b} = GM_b/c^2$. For $q \geq 10^{-4}$, supersonic collisions can extend to $R_1 \sim R_H$. If

$\mathcal{M} \gg 1$, ($r \ll R_1$) the post-shock temperature is $T \sim (5/16)\mathcal{M}^2 T_{\text{disk}}$ from Rankine-Hugoniot jump conditions, where T_{disk} is the model disk temperature at the merger radius. If $\mathcal{M} \sim 1 + \epsilon$, ($r \sim R_1$), then $T \sim (1 + \epsilon)T_{\text{disk}}$. The collisions at $R_1 < R_H$ generate energy $E_1 \approx (3/2)M_{\text{Hill}}(R_1/R_H)^3(k_B/m_H)T_{\text{disk}}$ on orbital timescales around M_f .

In the sub-sonic collision zone ($R_1 < r < R_H - \Delta R_H$), $\mathcal{M} < 1$ and the average gas temperature is $T \sim (1/3)(m_H/k_B)(\Delta M \Delta v_2/M_b)^2$, where Δv_2 is the velocity difference between $[R_1, R_H]$. Subsonic collisions contribute $E_2 \approx (1/2)M_{\text{Hill}}(\Delta M \Delta v_2/M_b)^2$. Gas between $R_H - \Delta R_H$ and R_H , with total mass ΔM_{Hill} , collides with gas orbiting the SMBH at velocity differential $\Delta v(r) \approx (c/2r(r_g)^{1/2})(q/3)^{1/3}$, yielding a average uniform temperature of $T = (1/3)(m_H/k_B)(\Delta v(r))^2$ and energy $E_3 \approx (1/2)\Delta M_{\text{Hill}}\Delta v(r)^2$.

The luminosity of the self-collisions above are limited by the timescales on which the gas collides, which could be $\gg t_{\text{orb}}$ (O’Neill et al. 2009). The most luminous EM contribution post-merger occurs as the kicked BH remnant attempts to carry its original Hill sphere gas with it. This is because: 1) it involves most of M_{Hill} and 2) the timescale of the disk response is short (R_H/v_{kick}) compared to most self-collision timescales. Physically, once the Hill sphere gas collides with an equivalent mass of disk gas (in time R_H/v_{kick}), much of the original Hill sphere gas is lost via ram pressure stripping. As a result, energy $E_{\text{kick}} = 1/2 M_H v_{\text{kick}}^2 \sim 10^{47} \text{erg} (M_{\text{Hill}}/1M_\odot)(v_{\text{kick}}/10^2 \text{km/s})^2$ is dissipated via shocks at temperature $T \sim O(10^5) \text{K} (v_{\text{kick}}/10^2 \text{km/s})^2$ over a duration $O(R_H/v_{\text{kick}})$. Here we assume an adiabatic shock; however, the timescales for large mass SMBH, especially for merging binaries on large orbits, imply non-adiabatic processes will be important. For such circumstances, our estimates represent upper limits.

2.2. Disk opacity

Photons liberated by gas shock heating can be scattered inside the disk before escape. If the merger occurs where gas pressure dominates then the disk atmospheric density is $\rho(z) = \rho_0 \exp(-z^2/2H^2)$ where ρ_0 is the mid-plane density, z is the vertical distance, and H is the disk height. The mean free path length of photons in the disk is $\ell = 1/(\kappa\rho)$, where κ is the disk opacity. Total path length L travelled by photons to the disk surface is $L = N\ell$ where $N = H^2/\ell^2$ is the average number of steps. Therefore, $L = H^2/\ell$ and the mean photon travel time is $t_{\text{Hill}} = L/c$. Assuming constant dissipation per unit optical depth, the disk surface temperature (T_{eff}) is $T_{\text{eff}} \approx ((3/8)\tau + 1/(4\tau))^{-1/4} T_0$ where $\tau = \kappa\Sigma/2$

and T_0 is the midplane temperature (Sirko & Goodman 2003). Now we consider two illustrative AGN disk models where $R_H \geq H$ and $R_H < H$. This allows us to quantify EM signatures at the order-of-magnitude level.

2.3. $R_H \geq H$: prompt UV flare

Consider a kicked $M_b = 65 M_\odot$ binary located at $r = 10^3 r_g$ from a $M_{\text{SMBH}} = 10^9 M_\odot$ SMBH, so $R_H \sim 3r_g$. For a Thompson et al. (2005) disk model at radius $r = 10^3 r_g$, $H/r \sim 10^{-3}$, so $H \sim r_g$ and $R_H > H$ in this example. The volume of gas in the Hill sphere is

$$V_{\text{gas}} = \frac{4}{3}\pi R_H^3 - \frac{2}{3}\pi(R_H - H)^2[3R_H - (R_H - H)]. \quad (4)$$

Here, $V_{\text{gas}}/V_{\text{Hill}} \sim 0.5$, so $M_{\text{Hill}} = V_{\text{gas}}\rho \sim 0.8M_\odot$.

The ram-pressure stripping of the kicked Hill sphere gas releases shock energy $E_{\text{kick}} = 1/2 M_{\text{Hill}} v_{\text{kick}}^2 \sim 10^{47} \text{erg} (M_{\text{Hill}}/1M_\odot) (v_{\text{kick}}/10^2 \text{km/s})^2 \sim O(10^5) (v_{\text{kick}}/10^2 \text{km/s}) \text{K}$ over timescale $O(R_H/v_{\text{kick}}) \sim 6 \text{mo}$, yielding a UV luminosity $\sim 10^{41} \text{erg/s}$. If disks similar to the Thompson et al. (2005) model are found around smaller mass SMBH, the timescale R_H/v_{kick} drops considerably and the luminosity can reach $\sim 10^{42} \text{erg/s}$ around $M_{\text{SMBH}} \sim 10^6 M_\odot$ (see below).

2.4. $R_H < H$: delayed, weak flare

A $M_b = 65 M_\odot$ binary located at $r = 10^3 r_g$ from a $M_{\text{SMBH}} = 10^8 M_\odot$ SMBH has a Hill sphere of radius $R_H \sim 6r_g$. In a Sirko & Goodman (2003) disk model at $r = 10^3 r_g$, $H/r \sim 10^{-2}$ so $H \sim 10r_g$ and $R_H < H$. Therefore $V_{\text{gas}} = V_{\text{Hill}}$ and $M_{\text{Hill}} = V_{\text{Hill}}\rho \sim 1.5M_\odot$. The photon diffusion length in the disk is $\langle L \rangle = \langle H \rangle^2/\ell$ where $\langle H \rangle$ spans $[H - R_H, H]$, or $[2.1, 10]r_g$ in this example. For an exponential atmosphere with $z \sim H$, $\langle L \rangle = \langle H \rangle^2/\ell \sim [0.4, 22] \times 10^{17} \text{cm}$ and the photon travel time spans $t_{\text{Hill}} = \langle L \rangle/c$ or $t_{\text{Hill}} \sim [15 \text{day}, 2.3 \text{yr}]$. For $\tau_0 \sim 10^4$, $T_{\text{eff}} \sim 0.1T_0$. So, while UV/optical photons emerge from the kick-shock on a timescale $O(\text{month})$ post-merger, the reprocessed optical signature is smeared out over several months with luminosity $\leq 10^{41} \text{erg s}^{-1}$. Upper limits on follow-up of LIGO/Virgo search volumes therefore constrains (H, ρ) in AGN disks.

2.5. New thermal emission from kicked hot spot

The temperature of an unperturbed thin AGN disk is $T(r) = T_{\text{max}} r^{-3/4}$, where $T_{\text{max}} \sim 6 \times 10^5 (M_{\text{SMBH}}/10^8 M_\odot)^{1/4} (\dot{m}/\dot{M}_{\text{Edd}})^{1/4} \text{K}$ and \dot{M}_{Edd} is the Eddington accretion rate. For $R_H > H$, T_{eff} can be $> T_{\text{max}}$ if τ_0 is small. The emitting area of the kicked Hill sphere is $(R_H/R_{\text{disk}})^2 \sim 5 \times 10^{-7}$ smaller than the

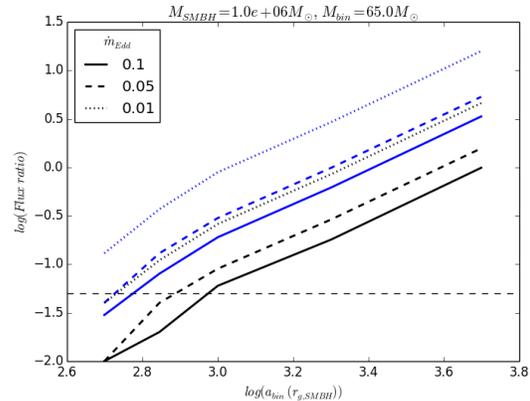


Figure 1. Ratio of optical (ZTF g -band) flux (black curves) and NUV (*GALEX* band) flux (blue curves) from kicked Hill sphere hot spot to (ZTF g -band, *GALEX* NUV) flux from a unperturbed AGN disk around a $M_{\text{SMBH}} = 10^6 M_\odot$ SMBH, as a function of binary distance (a_{bin}) from SMBH. We assume $M_b = 65 M_\odot$, $\Delta M \sim 0.05$ & $v_{\text{kick}} = 10^2 \text{km/s}$. Horizontal dashed line corresponds to a flux increase of $\sim 5\%$. Curves correspond to M_{SMBH} accreting at fractions 0.1 (solid), 0.05 (dashed), 0.01 (dotted) of the Eddington rate. At $a_b \geq 10^3 r_g$, the change in optical/NUV flux is detectable for $R_H > H$.

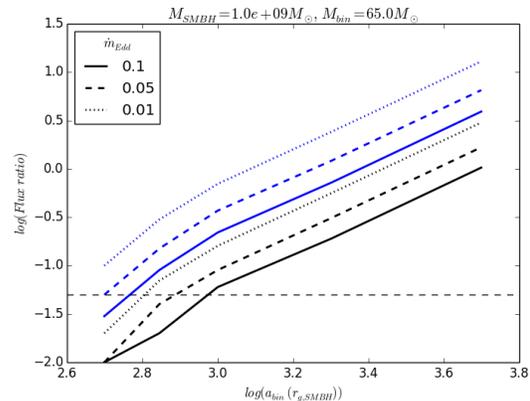


Figure 2. As Fig. 1 except for $M_{\text{SMBH}} = 10^9 M_\odot$.

disk (if $R_{\text{disk}} \sim 10^4 r_g$). The kicked hot spot has a temperature dependent only on v_{kick}^2 . Thus, a kicked merger in a AGN disk around a small mass SMBH can generate a short-lived luminous hot spot which could dominate continuum emission in the UV or optical bands.

Fig. 1 shows (black curves) the ratio of rest-frame g -band optical flux from the hot-spot to that emitted by the AGN disk and (blue curves) the corresponding *GALEX* NUV flux ratio. The curves assume a

kicked $M_b = 65 M_\odot$ BH merger ($v_{\text{kick}} \sim 10^2 \text{ km/s}$) in a disk around a $M_{\text{SMBH}} = 10^6 M_\odot$ SMBH accreting at $[0.01, 0.1] \dot{M}_{\text{Edd}}$, with $R_H > H$ so flux escapes. Fig. 2 is as Fig. 1, but for $M_{\text{SMBH}} = 10^9 M_\odot$. Horizontal dashed lines show the detectability threshold of a 5% flux change. Figs. (1) and (2) show the post-merger Hill sphere kick can be a substantial fraction of (or even dominate) g -band/NUV emission from the AGN disk if $a_b \geq 10^3 r_g$. ZTF and LSST can easily detect such changes ($> 5\%$) in g -band for well-detected sources. If $R_H < H$, the hot-spot is obscured. The curves in Figs. 1 and 2 drop by a factor $O(T_0/T_{\text{eff}})$ or -1.2 in log flux ratio for $T_0/T_{\text{eff}} \sim 2$. Mergers in lower accretion rate AGN disks with $R_H < H$ may be detectable for small T_0/T_{eff} if $\dot{M}_{\text{Edd}} = 0.01$.

2.5.1. Asymmetry in BLR line profiles

The broad line region (BLR) in AGN is modelled as a distribution of clumpy clouds at median radius R_{BLR} (Krolik, McKee & Tarter 1981; Netzer & Marziani 2010). The hot-spot on the disk photosphere emerges in days ($R_H > H$), whereupon the BLR is asymmetrically illuminated in time R_{BLR}/c (a few weeks). Off-center illumination generates a uniform asymmetry in all broad line components, unlike central AGN variability. If the hot spot persists, the asymmetric illumination washes over the BLR in several months.

3. STRATEGY FOR FOLLOW-UP OF A LIGO/VIRGO GW DETECTION VOLUME

LIGO–Virgo are detecting BH mergers at a rate 1/wk in the third observing run (O3)¹. If BH mergers are preferentially associated with AGN, we must optimize searches for the EM signatures above. If LIGO/Virgo releases binary mass estimates ($> 50 M_\odot$) with GW triggers, we increase the likelihood that $R_H > H$ so an EM counterpart is detectable.

Optimal search involves rapid wide-field UV/optical follow-up of small LIGO/Virgo error boxes when $M_b > 50 M_\odot$. UV is preferred since the fractional signature is more pronounced (Figs. 1 and 2), though such capabilities are currently lacking. Candidates displaying photometric jumps may have $R_H > H$ and optical spectroscopic follow-up can search for broad line asymme-

tries, indicating an off-center hot-spot. If $R_H < H$ then the disk hot-spot shows up weeks/months post-GW trigger. Optical surveys can detect photometric changes if $R_H > H$ and $a_b > 2000$ (4000) r_g in AGN disks accreting at 0.01 (0.1) \dot{M}_{Edd} .

A vetted AGN catalog is a good starting point for optical/UV follow-up. Assef et al. (2018) provides a catalog consisting of 4.5 million AGN candidates across the full extragalactic sky (≈ 150 candidates deg^{-2}) with 90% reliability (their ‘‘R90’’ catalog), as well as a lower reliability catalog of 21 million AGN candidates across the full extragalactic sky (≈ 700 candidates deg^{-2}) with 75% completeness; their ‘‘C75’’ catalog). Both catalogs derive from the AllWISE Data Release (Wright et al. 2010), and are currently the widest area published lists of AGN candidates across the full sky.

4. CONCLUSIONS

A merging BH binary in an AGN disk generates a prompt set of EM signatures if the Hill sphere radius is greater than the AGN disk height ($R_H > H$). The GW-kick causes ram pressure stripping of the Hill sphere. The resulting shock dominates the EM response & has no analog in SMBH mergers. Searches, including non-detections, constrain (H, ρ) in AGN disks. If $R_H < H$, detectability depends heavily on disk opacity. UV searches are optimal, but small LIGO/Virgo error boxes can be efficiently searched by large optical surveys with photo-z selected AGN catalogs. LIGO/Virgo triggers should include ‘large mass’ ($M_b > 50 M_\odot$) estimates to optimize EM follow-up.

5. ACKNOWLEDGEMENTS

BM dedicates this paper to the memory of his mother, Treasa McKernan. BM & KESF are supported by NSF 1831412. The work of DS was carried out at the Jet Propulsion Laboratory, California Institute of Technology, under a contract with NASA. Thanks to the referee for highlighting the GW kick & participants in the 1st workshop on stellar mass BH mergers in AGN disks, held March 11-13, 2019 and sponsored by the CCA at the Flatiron Institute in New York City.

REFERENCES

- Aasi, J. et al., 2015, CQG, 32 074001
 Abbott B.P. et al., 2016, ApJ, 833, L1
 Abbott B.P. et al., 2017, Phy.Rev.Lett., 118, 1101
 Acernese, F. et al., 2015, CQG, 32 024001
 Artymowicz P. et al., 1993, ApJ, 409, 592
 Assef R.J. et al., 2018, ApJS, 234, 23
 Baker J.G. et al., 2008, ApJ, 682, L29

¹ <https://gracedb.ligo.org/latest/>

- Bartos I. et al., 2017, *ApJ*, 835, 165
- Baruteau C., Cuadra J. & Lin D.N.C., 2011, *ApJ*, 726, 28
- Bellovary J. et al., 2016, *ApJ*, 819, L17
- Bode T. et al., 2010, *ApJ*, 715, 1117
- Bogdanović T. et al., 2008, *ApJS*, 174, 455
- Generozov A., Stone N.C., Metzger B.D. & Ostriker J.P., 2018, *MNRAS*, 478, 4030
- Goodman J. & Tan J.C., 2004, *ApJ*, 608, 108
- Hailey C.J. et al., 2018, *Nature*, 556, 70
- Krolik J.H., McKee C.F. & Tarter C.B., 1981, *ApJ*, 249, 422
- Kocsis B. & Loeb A., 2008, *PhRvL*, 101, 1101
- LIGO & VIRGO Scientific Collaborations, 2018, *ApJ*, arXiv:1811.12940
- McKernan B. et al., 2012, *MNRAS*, 425, 460
- McKernan B. et al., 2014, 441, 900
- McKernan B. et al., 2018, *ApJ*, 866, 66
- McKernan B. et al., 2019, *MNRAS* (submitted), arXiv:1907.04356
- Megevand M. et al., 2009, *PhRvD*, 80, 4012
- Miralda-Escudé J. & Gould A., 2000, *ApJ*, 545, 847
- Morris M., 1993, *ApJ*, 408, 496
- Netzer H. & Marziani P., 2010, *ApJ*, 724, 318
- O'Neill S.M., 2009, *ApJ*, 700, 859
- Secunda A. et al., 2018, *ApJ*, 878, 85
- Shields G.A. & Bonning E.W., 2008, *ApJ*, 682, 758
- Sigurdsson S. & Phinney E.S., 1993, *ApJ*, 415, 631
- Sirko E. & Goodman J., 2003, *MNRAS*, 341, 501
- Stone N.C. et al., 2017, *ApJ*, 464, 946
- Subr L. & Karas V., 2005, *A&A*, 433, 405
- Syer D., Clarke C. & Rees M.J., 1991, *MNRAS*, 250, 505
- Tichy W. & Marronetti P., 2008, *Phys. Rev. D*, 78, 1501
- Thompson T.A., Quataert E. & Murray N., 2005, *ApJ*, 630, 167
- Wright E.J. et al., 2010, *AJ*, 140, 1868
- Zlochower Y. et al., 2011, *CQGra*, 28, 4015