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Accelerated Structure-Aware Sparse Bayesian Learning for 3D Electrical Impedance Tomography

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Abstract—In this work, we consider the reconstruction of three-dimensional (3D) conductivity distribution using electrical impedance tomography (EIT) technique. A high-resolution and efficient algorithm is developed to solve the EIT inverse problem. The presented algorithm is extended upon a recently proposed novel EIT reconstruction approach based on structure-aware sparse Bayesian learning (SA-SBL). The correlation between proximal layers in the 3D geometry are incorporated into the structure prior to improve the reconstruction accuracy. In addition, an efficient approach based on approximate message passing is developed to accelerate the large-scale 3D learning process. To validate the algorithm, numerical experiments using real recorded data are conducted. The visual and quantitative comparisons show that the proposed method outperforms the existing methods in terms of reconstruction accuracy and computational complexity in all test cases. The SA-SBL based reconstruction approach can preserve the 3D structure of medical volume, reduce the systematic artifacts, and improve the computational efficiency.

Index Terms—Inverse problem, electrical impedance tomography (EIT), sparse Bayesian learning (SBL), image reconstruction, three-dimensional geometry.

I. INTRODUCTION

NON-DESTRUCTIVE examination and visualization of the internal industrial/biological process within a certain object is frequently and increasingly demanded in practice. Compared with other popular imaging modalities, such as ultrasound [1] and computed tomography (CT) [2], electrical impedance tomography (EIT) possesses the merits of higher temporal resolution, lower cost, wider applicability, and etc. However, EIT reconstruction is inherently unstable and suffers from the fundamental ill-posedness of the underlying inverse problem. The susceptibility of EIT solution to the measurement, numerical, and modeling errors necessitates regularization, and numerous such methods has been developed over the years. While the majority of EIT reconstruction algorithms has been designed for two-dimensional (2D) geometries (cf. literature review in [3]), a single cross-sectional slice of the volume can only reveal partial information of the realistic three-dimensional (3D) objects and thus limit the capacity of EIT. On the other hand, EIT is intrinsically a 3D problem [4], for it is well known that the path of the electric currents spread all over the 3D domain. As such, off-plane conductivity changes generally affect the solutions of the electrode plane and create considerable distortions in the resulting 2D images [5]. These severe limitations to 2D EIT thus encourage the development of 3D reconstruction. It is worth mentioning that, most 2D reconstruction methods are also applicable in 3D situations with minor modifications, and methods for both situations have been occasionally discussed together indiscriminately.

Fully 3D EIT has been investigated since 1980s. Calderón’s pioneer work [6] outlined a linearized method for the reconstruction of the multidimensional conductivity in a bounded domain, which laid the mathematical foundation for 3D EIT. Thenceforth many algorithms have been developed, including double constraint iterative algorithm [7], variants of Newton’s One-Step Error Reconstruction (NOSER) [8]–[10], Markov chain Monte Carlo (MCMC) based Bayesian approach [11], and etc. Apart from the linear approaches, various nonlinear solvers have also been produced. However, these were either facilitating a Newton-type strategy, which is highly computational intensive for large-scale problems, or employing the Krylov-subspace approach, which suffers from poor convergence rate [12]. In [13], a fully iterative regularized Gauss-Newton method was applied to 3D tank data adopting the complete electrode model (CEM) [14], which is the most accurate model for real-world EIT. In this paper, we also work exclusively with CEM. Readers are also referred to important articles [4], [15], where various commonly used conventional 3D reconstruction algorithms, such as regularised Gauss-Newton and conjugate-gradient based algorithms, were evaluated using simulated and real experimental data. The results of the study suggested that 3D EIT algorithms do have value and require further development.

Studies of 3D EIT in the early period was restrained by the prohibitive consumption of computing and storage resources, which partly explains why 2D assumptions were constantly made. Later, advances in electronic devices made the true 3D EIT reconstruction technically more feasible. The release of software EIDORS [16] marked another significant milestone in the progress of 3D EIT. Since then, other more...
recent approaches, including topology optimization approach [17], direct reconstruction using scattering transforms [18], iterative soft shrinkage algorithm [19], Bayesian approach with edge-prefering priors [20], TV regularization [21], nonlinear approach [22], and 3D-Laplacian and sparsity joint regularization algorithm [23] have been proposed. Despite considerable effort for nearly three decades, existing 3D EIT reconstruction algorithms fail to efficiently and reliably produce images with sufficiently high spatial resolution. Moreover, many algorithms (perhaps the majority) are ad hoc and require tweaking of parameters that prevents repeatability in experimentation. Specifically in the field of bioengineering, 3D EIT has yet to make the transition from theoretical studies to practical use.

The quality of reconstructed images and the efficiency of the reconstruction process are two major concerns for 3D EIT. One most recent publication [3] has proposed a novel structure-aware sparse Bayesian learning (SA-SBL) algorithm for 2D EIT reconstruction, with which an enhanced spatial resolution was achieved. The underlying structural dependency of signals can be readily incorporated within the Bayesian framework. Several challenging problems in industrial applications have been successfully tackled on this account. Specifically in the field of bioengineering, 3D EIT has yet to make the transition from theoretical studies to practical use.

In this work, we consider an inverse problem of linearized time-difference EIT of the form [3]

$$\mathbf{v} = \mathbf{J} \sigma + \mathbf{n},$$

(1)

where

- $\mathbf{v} \in \mathbb{R}^{M \times 1}$ represents the time-difference vector of the voltage measurements, and $M$ denotes the length of the measurement vector.
- $\mathbf{J} \in \mathbb{R}^{M \times N}$ is the sensitivity matrix, and $N$ denotes the number of simplices in the 3D domain.
- $\sigma \in \mathbb{R}^{N \times 1}$ represents the 3D time-difference conductivity distribution to be reconstructed.
- $\mathbf{n} \in \mathbb{R}^{M \times 1}$ denotes the measurement noise vector, which is assumed to be Gaussian, i.e., $\mathbf{n} \sim \mathcal{N}(0, \gamma_0 \mathbf{I}).$

Similar to [3], [26], we let $g = N - h + 1$ be the total number of groups. For $\forall i = 1, 2, \ldots, g$, $\sigma$ is factorized as (2) to facilitate the utilization of SA-SBL framework. Substituting (2) into (1), we then obtain the following stretched linear model

$$\mathbf{v} = \Phi \mathbf{x} + \mathbf{n},$$

(3)

where $\Phi \triangleq \mathbf{J} \Psi \in \mathbb{R}^{M \times gh}$. We follow the standard Bayesian formulation and assume that both of the priors of the weights $\mathbf{x}$ and the noise vector $\mathbf{n}$ follow parameterized Gaussian distributions, i.e., $\mathbf{x} \sim \mathcal{N}(0, \Sigma_0)$, $\mathbf{n} \sim \mathcal{N}(0, \gamma_0 \mathbf{I})$, where the stretched covariance matrix is expressed as $\Sigma_0 = \text{diag}(\gamma_i, \mathbf{B}_i) \in \mathbb{R}^{gh \times gh}$. The positive definite matrix $\mathbf{B}_i$ determines the correlated structure within the $i$-th block of $\mathbf{x}$. Due to the mechanism of automatic relevance determination, most $\gamma_i$’s tend to become zero during the learning process, thus promoting the group-level sparsity.

The posterior distribution for $\mathbf{x}$ can be expressed analytically as $\mathbf{x} | \mathbf{v} \sim \mathcal{N}(\mu_x, \Sigma_x)$ with mean and covariance matrix

$$\mu_x = \Sigma_0 \Phi^\top \Gamma^{-1} \mathbf{v} \in \mathbb{R}^{gh \times 1},$$

(4)

$$\Sigma_x = \Sigma_0 - \Sigma_0 \Phi^\top \Gamma^{-1} \Phi \Sigma_0 \in \mathbb{R}^{gh \times gh},$$

(5)

and $\sigma = \Psi_{N \times gh} \mathbf{x}_{gh \times 1}$

$$\triangleq \begin{bmatrix} \mathbf{1}_{h \times h} & \cdots & \mathbf{0}_{(i-1) \times h} & \mathbf{1}_{h \times h} & \cdots & \mathbf{0}_{(N-h) \times h} & \mathbf{1}_{h \times h} & \cdots & \mathbf{0}_{(N-i-h+1) \times h} \\ \mathbf{0}_{(N-h) \times h} & \cdots & \mathbf{1}_{h \times h} & \cdots & \mathbf{0}_{(N-i-h+1) \times h} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{x}_1 & \cdots & \mathbf{x}_h \end{bmatrix}^\top \begin{bmatrix} \mathbf{x}_1 & \cdots & \mathbf{x}_i & \cdots & \mathbf{x}_{i+h-1} & \cdots & \mathbf{x}_g & \cdots & \mathbf{x}_N \end{bmatrix}^\top \begin{bmatrix} \mathbf{x}_1 & \cdots & \mathbf{x}_h \end{bmatrix}^\top$$

(2)
where
\[ \Gamma \triangleq \gamma_0 I + \Phi \Sigma_0 \Phi^\top \in \mathbb{R}^{M \times M}. \]

The first step in the SA-SBL-based EIT reconstruction [3] is to update the hyperparameters \( \Theta \triangleq \{ \gamma_0, \{ \gamma_i, B_i \}_{i=1}^N \} \). This is achieved by employing the expectation-maximization (EM) method to minimize the cost function \( \mathcal{L}(\Theta) = \log |\Gamma| + v^\top \Gamma^{-1} v \). Subsequently, the MAP probability estimate \( \hat{x} \) is obtained directly from the posterior mean \( \mu_x \). Up to this point, one would naturally assume that the 2D EIT reconstruction algorithm in [3] can be directly applied to the 3D scenario, as the underlying mathematical problem intrinsically remains unchanged. However, the computational complexity of the previously proposed EM-based SA-SBL algorithm is dominated by the expectation step (E-step), i.e., (4) and (6), which respectively involves \( O(MN^2) \) and \( O(N^3) \) multiplications per iteration. In this context, the large-scale weight length \( N \) in the 3D model makes the inversion via SA-SBL computationally intractable.

Recently, the AMP methods [29]–[31] have received growing attention due to their low computational complexity, fast convergence, and close-to-Bayes-optimal estimation. We illustrate the AMP framework in Fig. 1, where blue squares and red circles represent probability density function (pdf) factors and random variables, respectively. Gaussian approximated belief propagation is performed. Concretely, the posterior pdf is first factorized into a product of simpler pdfs. Then, the locally computed messages associated with the unknown variables are passed around the factor graph until agreement on a common set of beliefs is arrived. By assuming a large and dense measurement matrix and exploiting similarity among the messages, central limit theorem and Taylor series expansion are adopted to approximate the inference.

In this work, AMP is applied to simplify the computational expensive E-step of SA-SBL-based 3D EIT reconstruction. We summarize the algorithm flow in Algorithm 1, where \( \otimes \) and \( \otimes \) respectively denote Hadamard product and element-wise division. It can be readily observed from Algorithm 1 that, \( \Phi, S \), and their transposes related vectorized multiplications constitute the majority of the overall computation load. As such, the E-step is implemented by a first-order algorithm with a computational complexity of \( O(MN) \) per iteration.

Algorithm 1: AMP-based E-step approximation.

\[
\begin{align*}
1 & \text{Input } : \Phi, \theta_x, \theta_a \in [0, 1], \epsilon_{\text{AMP}}. \\
2 & \text{Initialize } : \text{Set } S = \Phi \otimes \Phi, s = 0, \mu_x = 0, \tau_x > 0, \epsilon = 1. \\
3 & \text{Iterations:} \\
4 & \quad \epsilon > \epsilon_{\text{AMP}} \text{ do} \\
5 & \quad \alpha_p = 1 \otimes (S \tau_x), \\
6 & \quad p = s + \alpha_p \otimes \Phi \mu_x, \\
7 & \quad \alpha_x = \alpha_p \otimes \frac{\partial}{\partial p} f_x(p, \alpha_p), \\
8 & \quad s = (1 - \theta_x) s + \theta_x f_x(p, \alpha_p), \\
9 & \quad \tau_x = 1 \otimes (S^\top \alpha_x), \\
10 & \quad r = \mu_x + \tau_x \otimes \Phi^\top s, \\
11 & \quad \tau_x = \tau_x \otimes \frac{\partial}{\partial r} f_x(r, \tau_x), \\
12 & \quad \mu_x = (1 - \theta_x) \mu_x + \theta_x f_x(r, \tau_x), \\
13 & \quad \epsilon = \frac{\|\mu_x^{\text{new}} - \mu_x\|_2}{\|\mu_x^{\text{old}}\|_2}. \\
14 & \text{end} \\
15 & \text{Output } : \hat{\mu}_x, \hat{\tau}_x
\end{align*}
\]

Remarks 1: The Onsager correction term in step 7 is the key to the increased accuracy and computational efficiency of AMP methods, for it decouples prediction errors across iterations and ensure that \( r \) is an i.i.d.-Gaussian corrupted version of the true \( x \). In addition, to prevent divergence caused by the ill-conditioned measurement matrix with strongly correlated columns, damped mechanism is introduced in step 5 and 9.

Once the parameters \( \hat{\mu}_x, \hat{\tau}_x \) for the expected distribution are obtained, the algorithm continues to infer the hyperparameters \( \Theta \triangleq \{ \gamma_0, \{ \gamma_i, B_i \}_{i=1}^N \} \) through the maximization iterations as we did in [3]. Note that, the learning rules for these hyperparameters are slightly different from our previous work in [3]. Concretely, the regularized correlation structure matrix \( B_i \) is updated as

\[ B_i = \text{Toeplitz} \left( [r_i^0, r_i^1, \ldots, r_i^{h-1}] \right), \]

with

\[ r_i = \text{sign}(\tilde{r}_i) \cdot \min \{ |\tilde{r}_i|, 0.99 \}, \]

\[ \tilde{r}_i = \text{diag}(B_i, 1) / \text{diag}(\tilde{B}_i). \]

\[ \tilde{B}_i^{\text{new}} = \tilde{B}_i + \frac{1}{\gamma_i} \left( \text{diag}(\tilde{\tau}_x^i) + \hat{\mu}_x^i (\hat{\mu}_x^i)^\top \right), \]

where the superscript \( i \) denotes the \(( (i-1)h + 1 : ih )\)-th entries of the corresponding vectors.

To better exploit the 3D structure correlation so as to enhance the reconstruction accuracy, a 3D pattern coupling parameter \( \beta \in [0, 1] \) is introduced to the updating formula of \( \gamma_i \) to capture the dependency between the simplex under investigation and its proximal 6 simplexes (see Fig. 2). As
such, an updated $\gamma_i$ in each iteration can be expressed as follows:

$$\gamma_i^{\text{new}} = \frac{(\gamma_i + \beta \sum_{d=1}^{6} \tilde{\gamma}_{i,d}) \cdot \text{tr} \left( B_i^{-1} \left( \text{diag}(\hat{\tau}_x^i) + \hat{\mu}_x^i \hat{\mu}_x^i\top \right) \right)}{h}.$$  

Likewise, hyperparameter $\gamma_0$ is learned by

$$\gamma_0^{\text{new}} = \frac{\|v - \Phi \hat{\mu}_x\|_2^2 + \sum_{i=1}^{N} \text{tr} \left( \text{diag}(\hat{\tau}_x^i)(\Phi_i)\top \Phi_i \right)}{M}.$$  

A pseudo-code implementation of the overall algorithm for 3D EIT reconstruction is presented in Algorithm 2. As stated in [3], $h$ and $\beta$ are two tuning-free parameters, and we set $h = 4$ and $\beta = 0.25$ in the following discussion. $\epsilon_{\text{AMP}}$ in Algorithm 1 and $\vartheta_{\text{max}}$ in Algorithm 2 are both selected according to the precision requirement and computational resource.

**Remarks 2:** The initial guess of the parameters in Algorithm 2 such as $\gamma_0$ is empirically selected by extensive numerical trials, which generally leads to a faster convergence. It has little impact on the algorithm performance since these parameters will be automatically learned afterwards.

**Algorithm 2:** SA-SBL-based 3D EIT reconstruction.

<table>
<thead>
<tr>
<th>Input</th>
<th>$v$, $J$, $h$, $\beta$, $\vartheta_{\text{max}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Initialize</td>
<td>Set $\vartheta = 0$, $\gamma_i = 1_g \times 1$, $\gamma_0^{\text{new}} = 0$</td>
</tr>
<tr>
<td></td>
<td>$g \times \sqrt{\frac{1}{N-1} \sum_{i=1}^{N}</td>
</tr>
<tr>
<td>Iterations:</td>
<td>While $\vartheta \leq \vartheta_{\text{max}}$ do</td>
</tr>
<tr>
<td></td>
<td>Execute approximated E-step in Algorithm 1;</td>
</tr>
<tr>
<td></td>
<td>Update $\gamma_i$ using (13);</td>
</tr>
<tr>
<td></td>
<td>Update $\gamma_0$ using (14);</td>
</tr>
<tr>
<td></td>
<td>Update $B_i$ using (12)–(11);</td>
</tr>
<tr>
<td></td>
<td>$\vartheta = \vartheta + 1$.</td>
</tr>
<tr>
<td>Output</td>
<td>$\hat{\sigma} = \Psi \hat{\mu}_x$.</td>
</tr>
</tbody>
</table>

### III. Experiment Results and Discussions

In this section, the proposed 3D EIT reconstruction algorithm is evaluated with real-collected data. We consider two different experimental scenarios, viz., 3D cell pellet imaging and 3D Process Tomography of solution diffusion.

In the first experimental evaluation, we reconstruct the 3D EIT image from the dataset that has been utilized in [23]. The voltage measurement under test was recorded using a planar 3D miniature EIT sensor designed for cell imaging. Fast and
high-spatial-resolution reconstruction algorithm is particularly desirable in the scenario of continuous monitoring of cell culture process. Such task is considered challenging because of the small size of the sensor/subject and the high conductivity of the culture medium [23]. In the second experiment, the jet saline flow experiment in the Section IV-B of [3] is further extended to a 3D geometry. We still acquire the EIT measurements with the same cylindrical vessel senor used in [3], but two electrode planes are enabled to collect the voltage data at this time.

The 3D inverse finite element method (FEM) mesh in both reconstruction processes is illustrated in Fig. 3. While each layer in the FEM meshes for both experiments consists of 821 square simplices, the numbers of layers $L$ in the two FEM meshes are different. The former FEM mesh in Section III-A has 12 layers, and the latter in Section III-B has 40 layers. Consequently, the numbers of 3D simplices $N$ for these two experiments are 9744 and 32480, respectively.

A. 3D Cell Pellet Imaging

In the cell pellet imaging experiment, phosphate buffered saline with a conductivity of $1.9 \, S/m$ and height of $3 \, mm$ is used as cell culture medium. The internal diameter of the sensor is $15 \, mm$. The frequency of current excitation is $10 \, kHz$, and the amplitude of current is approximately $1.5 \, mA$ peak to peak. A triangular high-density breast cancer cell pellet is used as the experimental subject to be measured, which is shown in Fig. 4. The length of the trilateral is around $4.2 \, mm$, $3.6 \, mm$, and $4.5 \, mm$, respectively.

![Fig. 4. Truth of the triangular cell pellet to be measured. (Adapted from Fig. 15(c) of [23]. Reuse with the permission from IEEE and the authors.)](image)

A comparison is drawn in Table I, which shows the 3D EIT reconstruction results of the phantom using the conventional Bayesian algorithm [32] and the proposed SA-SBL based algorithm, respectively. Note that in Table I the two images in the first row of each table box are the 3D isosurface generated from the resulting volumetric data and the corresponding lateral view, respectively. The isovalue is specified as 40% of the maximum conductivity value. White grids are added into the slice plots to allow for a more precise assessment of the reconstruction. The readers are referred to the previous related work in [23] for a comparison of reconstructed results using other deterministic algorithms.

Because the subject to be imaged is a compound of cell pellet and agarose gel with an irregular shape, and part of the compound is transparent in the field of vision, we are unable to give a precise position of the inclusion. Since neither do we have an exact truth of the conductivity distribution under investigation, a quantitative evaluation of the advantage of the proposed algorithm in terms of spatial resolution and reconstruction accuracy cannot be provided. But it is important to note that, the presented algorithm in this paper is essentially a 3D and computationally efficient extension of the SA-SBL-based EIT reconstruction algorithm in [3] with the aid of AMP-based EM iteration. The effectiveness of the SA-SBL-based algorithm in comparison with other state-of-the-art approaches has been demonstrated via sufficient synthetic data simulations in COMSOL environment. On the other hand, it has been proved with extensive numerical studies in [30] that, AMP technique is able to yield nearly minimum mean-squared error recovery. In the light of the above facts, it is unnecessary to repeat the COMSOL-based numerical verification.

As indicated in Fig. 4, the utilized dataset is essentially a pseudo-3D measurement collected from a single electrode ring. Additionally, the EIT senor and subject to be detected are both in a extremely small size. Therefore, it is reasonable to anticipate a poor reconstruction result by using conventional methods. Nevertheless, the advantage of the proposed SA-SBL based algorithm in terms of algorithm performance can be visually observed from Table I. More specifically, the proposed algorithm is able to render a clear and accurate 3D image of the triangular cell pellet, whereas with the conventional Bayesian algorithm, conspicuous errors in the reconstructed shape/height of the phantom and undesired artifacts especially in the near-boundary region can be seen. 3D structural priors intuitively introduce additional constraints to stabilize the recovered images and, thus, make them more robust to interference and noise.

B. 3D Process Tomography of Jet Flow

EIT and the related electrical capacitance tomography (ECT) [33] are emerging techniques for imaging the flow and mixing of fluids in various industrial and biomedical applications. In this work, another experiment is designed to demonstrate the feasibility of fast and accurate 3D EIT-based process monitoring of fluid flow. Jet flows are simulated in the experiment since they are amongst the most frequently encountered flow types.

The vessel senor adopts an alternate mode to acquire the measurements for 3D imaging, i.e., the voltmeter readings in each plane are alternately drawn by switching the channels back and forth. The inner diameter of the cylindrical vessel is $287 \, mm$, and the height of the background substance is $200 \, mm$. The current excitation frequency and the injected current amplitude remain the same as [3], which are respectively $10 \, kHz$ and $15.17 \, mA$. The frame collection rate is set to $62.5 \, fps$. We select one frame from every $8$ frames between the $460$-th and the $516$-th frame. The conductivities of the red jet ink and the background saline are set to $0.8 \, S/m$ and $0.25 \, S/m$ respectively. The successive video snapshots and the reconstructed conductivity distributions by using the proposed algorithm for the selected frames are shown in Table II. To create a legible visualization, we first compare the absolute value of each entry with the threshold in each frame, which
### Table I: 3D EIT Reconstruction Results of the Triangular Cell Pellet

<table>
<thead>
<tr>
<th>Conventional Bayesian Method</th>
<th>Proposed Method</th>
</tr>
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<tbody>
<tr>
<td><img src="image1" alt="Layer 1" /></td>
<td><img src="image2" alt="Layer 1" /></td>
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<td><img src="image1" alt="Layer 2" /></td>
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<td><img src="image1" alt="Layer 3" /></td>
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<td><img src="image1" alt="Layer 8" /></td>
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<td><img src="image1" alt="Layer 10" /></td>
<td><img src="image2" alt="Layer 10" /></td>
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<td><img src="image1" alt="Layer 11" /></td>
<td><img src="image2" alt="Layer 11" /></td>
</tr>
<tr>
<td><img src="image1" alt="Layer 12" /></td>
<td><img src="image2" alt="Layer 12" /></td>
</tr>
</tbody>
</table>

Legend:
- Color bar: 
  - 0.16 to 0.08
  - 0.08 to 0.02
  - 0.02 to 0
  - -0.02 to -0.08
  - -0.08 to -0.12
  - -0.12 to -0.15
  - -0.15 to -0.2
  - -0.2 to -0.25
is set to 40% of the maximum absolute value in the frame. We then discard the conductivity values below the threshold and draw slices through the resulting EIT volumetric data. As such, only significant values induced by the jet flow are preserved and visualized in the 3D slices in Table II, so that the occlusions caused by the background and noise are removed. It can be observed from Table II that the estimates are in a good agreement with their corresponding video snapshots. Very few peripheral artifacts exist, and the entire injection process of the jet flow is accurately reconstructed.

Remarks 3: Note that the threshold 40% adopted in producing Table II is empirically selected for illustrative purpose. The use of a fixed percentage cut-off from the maximum value may lead to incorrect EIT result if there are no inclusions inside the sensor. In this situation, background fluctuations may not be filtered correctly and, consequently, artifacts from non-existing objects may appear in the output image. Thus, in practice one should always refer to the original 3D images/slices without the threshold. It is also observed that this threshold at some point reduces the size of inclusions in comparison to the reference snapshots in the video. However, if we decrease the threshold, the thin stream adjacent the syringe outlet in the upper layers can become overly thick in the resulting 3D images. Bear in mind the fact that EIT inverse problem is mathematically ill-posed and ill-conditioned. Here we are reconstructing a 32480-pixel 3D image using 208 voltage measurements from 2 × 16 electrodes. Although the structural a priori knowledge is exploited, we can never obtain the exact and true 3D conductivity distribution. Additionally, the injected saline with a conductivity below the EIT sensitivity may still be clearly visible to the naked eyes in the video snapshot due to the bright color of the ink. Thus, the actually conductivity distribution can also disagree considerably with the color dispersion in the vessel.

IV. Conclusion

In summary, for the underlying large-scale inverse problem of 3D EIT reconstruction, this paper has developed an accelerated SA-SBL-based algorithm via AMP, which offers enhanced reconstruction accuracy and reduced artifacts by exploiting 3D structure priors. It is noteworthy that the proposed algorithm is generalizable to other similar process tomography modalities. The advantage of the proposed algorithm over conventional methods has been validated by numerical experiments using real collected measurements, and the visualization of 3D fluid flow process has also been attempted. This study takes an important step towards practical and more sophisticated real-time impedance tomography. The enhanced imaging quality and reduced computational complexity offers exciting possibilities for imaging tasks in several practical applications, such as dispersion control in mixing vessels and monitoring of brain function. Together with its characteristic strength in time and contrast resolution, EIT instrumentation should be able to evolve as an attractive complement/alternative to the prevailing radionuclide modalities in the foreseeable future.

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TABLE II
3D EIT RECONSTRUCTION RESULTS OF THE JET FLOW.


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