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**Citation for published version:**

Gomez-Perez, N, Rodriguez, J & McWilliams, R 2017, 'Finite element modeling of melting and fluid flow in the laser-heated diamond-anvil', *Journal of applied physics*, vol. 121, 145904, pp. 145904-1.  
<https://doi.org/http://aip.scitation.org/doi/pdf/10.1063/1.4979313>

**Digital Object Identifier (DOI):**

<http://aip.scitation.org/doi/pdf/10.1063/1.4979313>

**Link:**

[Link to publication record in Edinburgh Research Explorer](#)

**Document Version:**

Peer reviewed version

**Published In:**

Journal of applied physics

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1 **Finite element modeling of melting and fluid flow in the laser-heated diamond-anvil**  
2 **cell**

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13 (Dated: 6 March 2017)

14 The laser-heated diamond anvil cell is widely used in the laboratory study of mate-  
15 rials behavior at high-pressure and high-temperature, including melting curves and  
16 liquid properties at extreme conditions. Laser heating in the diamond cell has long  
17 been associated with fluid-like motion in samples, which is routinely used to deter-  
18 mine melting points and is often described as convective in appearance. However, the  
19 flow behavior of this system is poorly understood. A quantitative treatment of melt-  
20 ing and flow in the laser-heated diamond anvil cell is developed here to physically  
21 relate experimental motion to properties of interest, including melting points and  
22 viscosity. Numerical finite-element models are used to characterize the temperature  
23 distribution, melting, buoyancy, and resulting natural convection in samples. We find  
24 that continuous fluid motion in experiments can be explained most readily by natural  
25 convection. Fluid velocities, peaking near values of microns per second for plausible  
26 viscosities, are sufficiently fast to be detected experimentally, lending support to the  
27 use of convective motion as a criterion for melting. Convection depends on the phys-  
28 ical properties of the melt and the sample geometry, and is too sluggish to detect for  
29 viscosities significantly above that of water at ambient conditions, implying an upper  
30 bound on the melt viscosity of about 1 mPas when convective motion is detected.  
31 A simple analytical relationship between melt viscosity and velocity suggests direct  
32 viscosity measurements can be made from flow speeds, given basic thermodynamic  
33 and geometric parameters of samples are known.

34 PACS numbers: 66.20.Cy, 64.70.D, 62.50.-p, 07.35.+k 47.11.Fg 44.25.+f

35 Keywords: diamond, anvil, cell, convect, motion, viscosity, high, pressure, tempera-  
36 ture, melt, laser, heat, transport, finite, element, numerical, model, liquid, fluid

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## 37 I. INTRODUCTION

38 Accurate experimental constraints on melting points and liquid properties in materials  
39 under high pressure conditions are needed in fields ranging from condensed matter theory<sup>1,2</sup>  
40 to planetary science<sup>3-5</sup>, where high-pressure melts play a central role in magmatism, thermal  
41 evolution, and magnetic field generation. For most materials the melting temperature in-  
42 creases significantly under pressure. This includes fluids such as water<sup>6</sup> or hydrogen<sup>7</sup> which  
43 solidify under pressure, and solids such as iron<sup>3,4,8-10</sup> which exhibit significantly elevated  
44 melting points. It is thus necessary to reach temperatures on the order of thousands of  
45 degrees Kelvin in experiments at pressures of tens to hundreds of GPa to study melting and  
46 the properties of fluid phases.

47 The diamond anvil cell (DAC) has been an instrument of unparalleled utility in the  
48 laboratory study of matter at high pressure and temperature. Studies using this device  
49 have paid special attention to the characterization of phase transitions, and in particular,  
50 to melting. External heating of the DAC using resistive heating can reach temperatures of  
51 roughly 1000 K in samples, below melting temperatures for many materials under pressure.  
52 In contrast, laser heating of the diamond cell – i.e. localized, direct laser illumination of high  
53 pressure samples through the diamond optical window – can achieve maximum temperatures  
54 exceeding 10 000 K,<sup>11,12</sup> enough to melt all known materials to very high pressures.<sup>1,4,5,13-17</sup>  
55 This laser-assisted DAC setup is called the laser-heated diamond anvil cell (LHDAC).

56 While providing the capability of studying high-pressure melting and melts in virtually all  
57 substances, LHDAC techniques are often complicated, compared to homogeneous external  
58 heating, by very large standing temperature gradients in samples, on the order of hundreds  
59 to thousands of degrees K per micron.<sup>9,10,12,18-31</sup> Local pockets of melt can be stabilized in  
60 these temperature gradients, surrounded by lower-temperature solid matter and the cold,  
61 heat-sinking diamond anvils. The accurate detection of melting in such experiments is a  
62 longstanding challenge in high-pressure research. There is also a pressing need to determine  
63 the properties of the fluid state, including viscosity.

64 Among the most common<sup>3,8-10,19,32-41</sup> and controversial<sup>1,4,14-17,42-44</sup> diagnostics of melt-  
65 ing in LHDAC experiments is the visual observation of motion in the laser-heated sample,  
66 which is attributed to fluid flow and often described as being ‘convective’ and ‘continuous’  
67 in appearance.<sup>3,9,32,34,36-42</sup> While this motion is readily observable in experiments, there is

68 limited understanding of the nature and origin of the motion, and thus how it is connected  
 69 to melting in the LHDAC. Sample motion has been usually characterized by qualitative  
 70 criteria,<sup>3,9,10,19,32,34,36–40,42</sup> adding significant uncertainty to experimental interpretations. If,  
 71 as qualitatively assessed, observed motions are convective in nature, then it stands to reason  
 72 that these motions, coupled to information about temperature gradients and sample geom-  
 73 etry, will enable assessment of fluid transport properties, and in particular viscosity. This  
 74 information is also needed to assess systematic differences between melting studies. Motion-  
 75 based criteria have yielded melting curves consistent with other approaches in many cases,  
 76 for example in bridgmanite<sup>32,42,45</sup>, sodium chloride<sup>14,33</sup> and aluminum<sup>1</sup> but pronounced and  
 77 as-yet unresolved discrepancies in others, as in iron<sup>3,4</sup>, tantalum<sup>16,35,44</sup> and molybdenum.<sup>15,35</sup>  
 78 In this study we address this gap in knowledge by quantitatively relating melting and motion  
 79 in the LHDAC, establishing its underlying physical basis and assessing possible observable  
 80 phenomena in experiments which may signal the cause of the flow and the character of the  
 81 fluid state.

82 In the past, order-of-magnitude considerations have been applied to estimate possible  
 83 causes of fluid flow in the LHDAC, rates of flow, and the effects of flow on heat trans-  
 84 port and temperature distributions.<sup>19,21,28</sup> Assuming that flow is convective, and driven by  
 85 the temperature gradients across fluid regions, which produce buoyancy, several estimates  
 86 regarding flow properties can be made through dimensional analysis.<sup>46</sup>

87 In free (also called natural) convection, the Grashof number  $Gr$  establishes the relative  
 88 importance of buoyant, viscous, and inertial forces. It is defined as

$$89 \quad Gr = \frac{g\rho^2\beta\Delta TD^3}{\mu^2}, \quad (1)$$

90 where  $g$  is the acceleration of gravity,  $\Delta T$  is the temperature difference across the character-  
 91 istic length scale of the fluid  $D$ , and  $\rho$ ,  $\beta$  and  $\mu$  are the material density, volumetric thermal  
 92 expansivity, and dynamic (also called shear) viscosity, respectively. On the microscopic scale  
 93 of the LHDAC the  $D^3$  factor dominates, such that  $Gr \ll 1$  is a good approximation. This  
 94 implies that inertial forces are small compared to viscous forces, which balance the buoyant  
 95 forces, giving a characteristic flow velocity  $U$  of<sup>21,46</sup>

$$96 \quad U \approx \frac{\rho g \beta \Delta T D^2}{\mu}. \quad (2)$$

97 This is equivalent to stating that the ratio of inertial force to viscous force, or Reynolds

98 number  $Re$ , given by

$$99 \quad Re = \frac{U\rho D}{\mu}, \quad (3)$$

100 is equal to  $Gr$ ,

$$101 \quad Gr \approx Re. \quad (4)$$

102 Assuming liquid properties similar to water, a typical liquid dimension  $D \approx 1 \mu\text{m}$ , and a tem-  
103 perature gradient of  $\sim 10^3 \text{ K } \mu\text{m}^{-1}$ , then  $Gr \approx 10^{-6}$  and  $U \approx 1 \mu\text{m s}^{-1}$ . Speeds within several  
104 orders of magnitude of this value are expected for a realistic range of material properties  
105 and sample geometries. Such speeds would be consistent with detectable convective motion  
106 seen under microscopy in real time in experiments. However, this estimate is crude in that  
107 it does not account for the specific geometry of the LHDAC, the flow planform and position-  
108 dependence of velocity, the detected component of velocity, and other specific aspects of  
109 experimental systems. It has been reported<sup>37</sup> that the character and vigor of convection  
110 in the LHDAC sample chamber is noticeably sensitive to “the sample itself, the pressure  
111 medium, pressure, temperature, pressure-temperature gradients, and chamber geometry”,  
112 and so is dependent on a complex interplay of sample properties, which are accounted for  
113 in this study.

114 When considering the character of convection and its influence on heat transport, we can  
115 also define the Rayleigh number  $Ra$ ,

$$116 \quad Ra = \frac{\rho g \beta \Delta T D^3}{\kappa \mu}, \quad (5)$$

117 which may be obtained by multiplying  $Gr$  and the Prandtl number  $Pr = \mu/\rho\kappa$  (the ratio  
118 of viscous diffusivity  $\mu/\rho$  to thermal diffusivity  $\kappa$ ). At  $Gr \ll 1$ ,  $Ra$  is also equivalent to  
119 the ratio of convective heat transfer to conductive heat transfer.<sup>46</sup> For the representative pa-  
120 rameters of the LHDAC discussed above,  $Ra \approx 10^{-6}$ , and for any realistic set of parameters  
121 in the LHDAC  $Ra \ll 10^3$ , roughly the critical value of  $Ra$  in ideal systems below which  
122 convection is inhibited.<sup>19,21</sup> These considerations have been argued to lead to absent<sup>19</sup> or  
123 sluggish<sup>21</sup> buoyancy convection and a correspondingly negligible effect of convection on heat  
124 transfer in the LHDAC.<sup>19,21,28</sup> A complete quantitative consideration of these dynamics is  
125 explored in this study.

126 Numerical models have been used extensively to describe phenomena relevant to the  
127 laser-heated diamond cell, including temperature distributions<sup>12,18,20–31,47</sup> and, to a limited

128 extent, melting,<sup>12,27,28</sup> however fluid flow has not been directly modelled. In this paper, we  
129 present numerical finite-element models of natural thermal convection in the LHDAC, having  
130 a two-dimensional (axisymmetric) spatial geometry and axial orientation of gravity. We use  
131 time-dependent finite-element algorithms solving for thermal transport in the LHDAC (e.g.  
132 Montoya and Goncharov<sup>27</sup>), and include a Boussinesq fluid medium governed by the Navier-  
133 Stokes equations. Temperature gradients, sample physical properties, the occurrence of  
134 melt-solid boundaries inside heated samples, and the detailed configuration of typical sample  
135 chambers are accounted for by these numerical models of flow. Simulated samples, containing  
136 a solid metallic coupler on which laser energy is deposited, are fully fluid or locally melted by  
137 laser heating, with the melt boundary and location of melt determined self-consistently with  
138 the temperature gradient. Flow speed is found to be strongly controlled by fluid viscosity and  
139 by the particular geometry of the LHDAC. Maximum simulated flow velocities are at most  
140 small (of the order of tenths of  $\mu\text{m s}^{-1}$  for water-like viscosity), though are sufficiently fast to  
141 be observed in the laboratory. Natural thermal convection is thus confirmed to be possible  
142 in the LHDAC, though order of magnitude estimates of flow behavior discussed above have  
143 limited utility, revealing a need for detailed experimental models. The analysis of natural  
144 convection in the LHDAC developed here provides a reference model for flow and the forces  
145 that drive it, from which we consider possible alternative causes for flow and other types of  
146 motion that may occur in experiments. Ultimately, these models allow for a quantitative  
147 evaluation of experimental observations. Results are discussed in the context of motion  
148 observations previously made in LHDAC experiments and those that could potentially be  
149 made, such as velocity mapping of molten samples.

150 The simulation parameters and the equations of motion and energy are found in Sec-  
151 tion II. The model results in the steady-state limit are presented in Section III. Section IV  
152 discusses the physical and practical implications of the models and their relationship with  
153 prior work. A summary of conclusions drawn from our simulations and a discussion about  
154 future investigations is included in Section V.

## 155 II. METHODOLOGY

### 156 A. GEOMETRY

157 A DAC consists of two gem-cut diamonds pressed together at their culets, flat tips having  
158 a radius  $R_d$  on the order of tens to hundreds of  $\mu\text{m}$ . There is a gasket, a foil that is placed  
159 between the culets of the diamonds where a hole (of radius  $R_m < R_d$ ) is cut. This gasket  
160 holds the sample inside the hole and between the two diamonds. To study transparent  
161 samples in the LHDAC, such as water, a thin metallic (or other optically absorptive) foil,  
162 known as the coupler (of radius  $R_c < R_m$ ), is often introduced into the sample cavity to  
163 absorb laser radiation. To study opaque samples, such as Fe, a transparent pressure medium  
164 is placed around a foil in essentially the same configuration, with the medium acting as an  
165 insulator. The coupler may be held in place away from the diamond with grains of ruby  
166 or other material placed between the culet and the coupler. Melting of the medium or the  
167 coupler may be studied.<sup>10</sup> Optical access to the sample chamber is provided through the  
168 anvils.

169 The system modeled in this study represents this typical set up of a LHDAC experiment  
170 (Fig. 1). The modeled domain comprises a metallic coupler disk and a surrounding optically  
171 transparent pressure medium. The coupler is placed in the center of the cavity, and the  
172 medium is contained by the diamonds (on top and bottom) and gasket (laterally). The  
173 acceleration of gravity is set parallel to the DAC axis, which runs through the center of the  
174 culets, cavity and coupler. Assuming this geometry and laminar flow, the problem to solve  
175 is axisymmetric, i.e. there are no forces that would change the motion with respect to the  
176 angle  $\phi$ , measured on the surface perpendicular to the axis. This common experimental  
177 geometry is convenient for numerical models and minimizes calculation time. Once this  
178 symmetry is assumed, the nominally 3D problem of flow becomes a 2D problem where there  
179 are variations only in  $r$ , distance to the axis, and  $z$ , position in the axial direction, as a  
180 function of time. The case of a horizontal axis (perpendicular to gravity), another common  
181 experimental configuration, must be modeled using all three spatial dimensions, presenting  
182 a more challenging problem not addressed here.

184 The coupler is heated on surfaces  $s_1$  and  $s_2$  by axially-aligned laser beams incident from  
185 top and bottom, and having equal power. This is a typical ‘double-sided’ laser heating



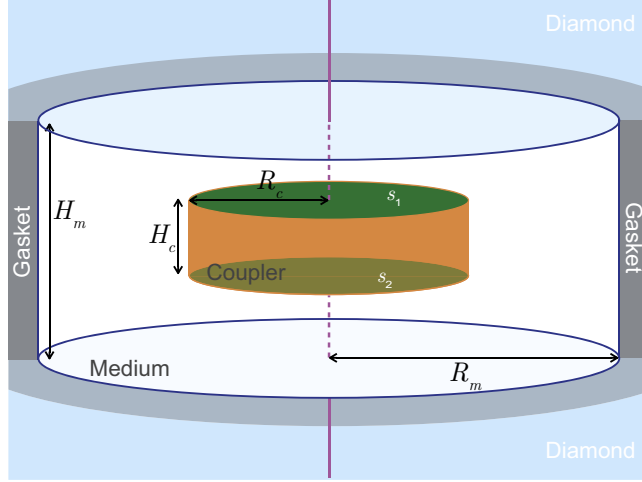


FIG. 1. This figure shows the schematic configuration of the modelled domain. We assumed a cylindrical symmetry around the axis shown in purple. The coupler disk (orange) is made of an optically opaque material and is heated with lasers on surfaces  $s_1$  and  $s_2$ , shown in green. Inside the sample cylinder (white) the pressure medium is optically transparent and it is heated only by the heat transferred from the interior disk. Outer boundaries of the sample chamber are kept at a constant temperature of 300 K.

186 configuration. We used the dimensions of a typical DAC, and of lasers currently used  
 187 in LHDAC systems (see Table I). We assumed an ambient temperature ( $T_{min} = 300$  K)  
 188 boundary condition at the edges of the sample chamber, a good approximation for the  
 189 LHDAC.<sup>18,20,25,27,28,30</sup>

TABLE I. Geometrical parameters used in the models. The LHDAC sample cavity is a cylinder of radius  $R_m$  and height  $H_m$ . The coupler is located at the center of the space and defined as a cylinder of radius  $R_c$  and height  $H_c$ , a distance  $d = (H_m - H_c)/2$  from the diamond culets. The laser heating spots on the coupler have a radius parameter  $\ell$ .

$R_m$	$H_m$	$R_c$	$H_c$	$d$	$\ell$
( $\mu\text{m}$ )	( $\mu\text{m}$ )	( $\mu\text{m}$ )	( $\mu\text{m}$ )	( $\mu\text{m}$ )	( $\mu\text{m}$ )
50	16	30	4	6	15

190

191

192 In our models we treat melting of the transparent pressure medium and assume that  
 193 the coupler remains solid. This is the configuration used to study dielectrics melting, as  
 194 applied in many of the more reliable studies using motion-based melting curve determination

195 (MgSiO<sub>3</sub><sup>32,42,45</sup> and NaCl<sup>14,33</sup> were mentioned earlier). The coupler is presumed to remain  
 196 fixed in place, even when the surrounding medium is entirely fluid. For simplicity, we neglect  
 197 any other material in the DAC other than the coupler and the medium.

## 198 B. PHYSICAL PROPERTIES OF MATERIALS

199 Material properties used in the simulations are representative of materials commonly  
 200 studied in the laser-heated diamond anvil cell (Table II). The medium was selected to have

TABLE II. Physical properties of the materials used in the simulations: mass density ( $\rho$ ), heat capacity at constant pressure ( $C_p$ ), thermal conductivity ( $k$ ), thermal diffusivity ( $\kappa = k/\rho C_p$ ), emissivity of the coupler ( $\epsilon$ ) and volumetric thermal expansion coefficient for the liquid phase ( $\beta$ ). Values of medium viscosity ( $\mu$ ) and melting temperature ( $T_{melt}$ ), were varied systematically for different simulations.

	$\rho$ kg m <sup>-3</sup>	$C_p$ J/(kgK)	$k$ W/(mK)	$\kappa$ m <sup>2</sup> s <sup>-1</sup>	$\epsilon$	$\beta$ K <sup>-1</sup>
Coupler	9100	519	20	4.2×10 <sup>-6</sup>	0.272	... <sup>a</sup>
Medium	1000	2000	10	2.6×10 <sup>-6</sup>	... <sup>a</sup>	2×10 <sup>-4</sup>

<sup>a</sup> Quantity not defined

201

202

203 physical properties similar to those of water in the range of 0-15 GPa, for fluid density  
 204  $\rho$ , heat capacity  $C_p$ , thermal conductivity  $k$ , and volumetric thermal expansivity  $\beta$ . In  
 205 order to do a parametric study, we systematically varied selected properties of the medium  
 206 which were found to have a first-order effect on flow behavior in the simulations, specifically  
 207 the melting temperature ( $T_{melt}$ ), which controls melt volume, and the melt viscosity ( $\mu$ ).  
 208 Melt viscosities  $\mu = 10^{-5}$ ,  $10^{-3}$ , 0.1, 10, and  $10^3$  Pa.s were tested. This range of values  
 209 covers very low viscosity fluids such as liquid hydrogen ( $\sim 10^{-5}$  Pa.s), water ( $\sim 10^{-3}$  Pa.s),  
 210 and silicate melts ( $\sim 10^3$  Pa.s). Medium melting temperatures  $T_{melt} = 300, 400, 1000,$  and  
 211  $2000$  K were tested in primary simulations ( $T_{melt} = 350$  and  $1500$  K were also tested in  
 212 earlier simulations, partial results of which are presented here). We assume that physical

213 properties of the medium in liquid and solid states are identical, and that the medium is  
 214 always optically transparent. The coupler is assumed to have properties similar to metals  
 215 used in such experiments, specifically iron.

### 216 C. GENERAL SIMULATION METHODOLOGY

217 In order to describe the dynamical behavior inside the DAC under various heating con-  
 218 ditions we used a finite-element solution of the time-dependent energy transfer equation

$$219 \quad \frac{\partial T}{\partial t} = -\mathbf{u} \cdot \nabla T + \kappa \nabla^2 T, \quad (6)$$

220 where  $T$  is the temperature,  $t$  is the time, and  $\mathbf{u}$  is the flow velocity (with corresponding  
 221 speed  $v = |\mathbf{u}|$ ). For the solid, there is no flow and  $\mathbf{u} = 0$ . For the liquid region it is necessary  
 222 to solve simultaneously the full Navier-Stokes equations

$$223 \quad \frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} = -\frac{\nabla P}{\rho} + \frac{\mu}{\rho} \nabla^2 \mathbf{u} + g\beta T \hat{\mathbf{z}}, \quad (7)$$

224 where  $P$  is the pressure and  $g\hat{\mathbf{z}}$  is the downward acceleration of gravity. We used the solution  
 225 for a Boussinesq fluid, where the changes in density are small and proportional to  $T$ , so the  
 226 continuity equation reads as:

$$227 \quad \nabla \cdot \mathbf{u} = 0. \quad (8)$$

228 Densities are assumed to remain constant throughout simulations and upon solid-liquid  
 229 phase change; for the solid this means that thermal expansion effects are neglected; for  
 230 the fluid, this means that thermal expansion is accounted for only through the Boussinesq  
 231 approximation.

232 The heating lasers are assumed to have a Gaussian spatial intensity distribution  $\mathcal{I}(r, t)$   
 233 at the coupler surface of

$$234 \quad \mathcal{I}(r, t) = \frac{\epsilon \mathcal{P}(t)}{\pi \ell^2} \exp\left(-\frac{r^2}{\ell^2}\right), \quad (9)$$

235 where  $\mathcal{P}(t)$  is the power of the laser,  $\ell$  defines the radius of the laser spot, and  $\epsilon$  is the surface  
 236 emissivity. The heating is modeled to be continuous in time (i.e.,  $\mathcal{P}(t) = \mathcal{P}_o$ ), by raising the  
 237 power in the first few  $10^{-8}$  s of the simulation.

238 The simulations are initialized with all the cavity at ambient temperature (300 K), and  
 239 flow velocities  $\mathbf{u} = 0$ . At  $t = 0$  the laser is turned on, and the model develops the heat  
 240 transfer and fluid motion out of equilibrium while heating the surfaces  $s_1$  and  $s_2$  of the

241 coupler. In each simulation, the temperature and velocity distribution are allowed to evolve  
242 to a steady state.

243 The temperature distribution in the sample is found to be identical whether or not flow  
244 terms are included in the simulations, confirming that heat advection does not contribute  
245 significantly to the heat transport in the case of natural convection, as expected from dimen-  
246 sional analysis. This fact allows for several simplifications in the models. Most importantly,  
247 the position of the solid-melt boundary is defined only by heat conduction, and so can be  
248 assessed *a priori* in simulations without the need to define it self-consistently with the flow,  
249 a significantly more challenging problem. Also, for all simulations at given  $\mathcal{P}_o$ , the maximum  
250 temperature  $T_{max}$  is effectively constant. Radiative contributions to heat transport are also  
251 negligible compared to the conductive contributions.<sup>28,30</sup>

252 The simulations were performed as follows. First, at a given  $\mathcal{P}_o$ , a simulation was run  
253 with two model domains (coupler and medium) assuming the medium was fully liquid  
254 ( $T_{melt} = T_{min} = 300$  K) with water-like viscosity  $\mu_w = 10^{-3}$  Pa.s. This established a ref-  
255 erence temperature distribution at this laser power. Next, a sequence of simulations at  
256 various values of  $\mu$  and  $T_{melt}$  were performed. The solid-liquid boundary was identified by  
257 the isothermal contour in the reference temperature distribution corresponding to the melt-  
258 ing temperature  $T_{melt}$ , which was used to divide the medium into solid and liquid domains  
259 producing a new geometry of three domains (coupler, solid medium, and liquid medium),  
260 as is appropriate for congruent melting.<sup>28</sup> To check the validity of this approach, the new  
261 location of the  $T_{melt}$  isotherm in the final simulation was compared with that in the refer-  
262 ence simulation ( $T_{melt} = 300$  K,  $\mu_w$ ), and the difference in isotherm position was found to be  
263 negligible. The sequential approach followed is thus physical for describing partial melting  
264 in the steady state limit.

265 The steady state was evaluated by observing flow velocity approach an asymptotic limit  
266 (Fig. 2). The time needed to reach steady-state equilibrium in the simulations is in the  
268 range of 10  $\mu$ s to 5 ms. It is longest for the lowest viscosities, because the viscous diffusion  
269 time,  $\tau_\mu$ , given as

$$270 \quad \tau_\mu \approx \rho D^2 / \mu, \quad (10)$$

271 is larger for lower viscosity, approaching  $\sim 3.6$  ms for  $\mu = 10^{-5}$  Pa.s. For all other viscosities,  
272 viscous diffusion times are very rapid, and the equilibration is mainly controlled by the

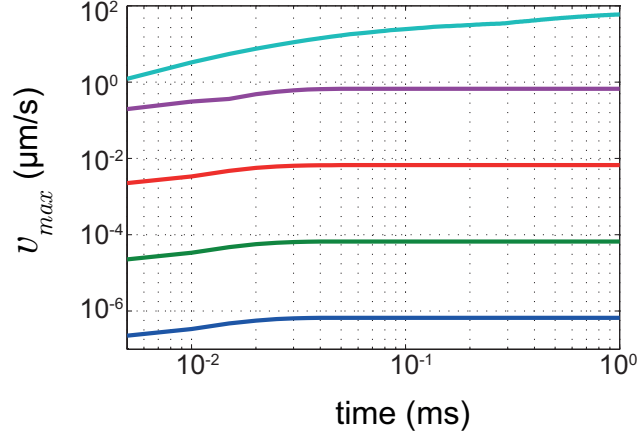


FIG. 2. Maximum velocity versus time for  $T_{melt} = 300$  K,  $T_{max} = 5051$  K and  $\mu = 10^3, 10^1, 10^{-1}, 10^{-3},$  and  $10^{-5}$  Pa s for blue, green, red, purple and cyan color lines, respectively. For the lowest viscosity, equilibrium is not achieved on the timescale of this plot. In the case of higher viscosities (bottom curves), the steady state is reached after  $\tau_{\kappa} \approx 13$   $\mu$ s; for low viscosity (top curve) steady state is not reached until  $\tau_{\mu} \approx 4$  ms.

273 thermal diffusion time  $\tau_{\kappa}$ , given as

$$274 \quad \tau_{\kappa} \approx D^2/\kappa, \quad (11)$$

275 which is  $\sim 13$   $\mu$ s. Thus the approach to steady state equilibrium in the simulations is con-  
 276 trolled by the longer of  $\tau_{\mu}$  and  $\tau_{\kappa}$ .

277 In most simulations reported here, we defined the solid-melt boundary in the medium  
 278 by a direct interpolation of the isothermal contour in the temperature distribution. In an  
 279 earlier set of simulations, we used a simplified definition of the melt boundary defined by an  
 280 ellipsoidal function, which approximated the shape and position of the solid-melt interface.  
 281 This analytical boundary allowed for a faster numerical convergence, but generally showed  
 282 more significant errors in defining the melt vesicle. Nonetheless, these results were found  
 283 to be in good agreement with later, more accurate simulations in terms of scaling behavior  
 284 (Section III B), indicating that the details of the shape of the melt package are not very  
 285 significant for estimating the steady-state flow behavior.

286 **D. LATENT HEAT EFFECTS**

287 When the laser is turned on, the system heats up reaching a maximum temperature at  
 288 the center of the coupler's surface  $T_{max}$  ( $r = 0$  and  $z = \pm 2 \mu\text{m}$ ). When  $T_{max} > T_{melt} > T_{min}$ ,  
 289 a phase boundary must be created in the medium. Phase change generally requires the  
 290 inclusion of a latent heat term in the thermal balance. We included the latent heat using  
 291 the apparent heat capacity method (AHCM),<sup>48</sup> assuming a smooth transition from one  
 292 phase to the other (and the presence of a mushy region), with  $g_l$  and  $g_s$  specifying the liquid  
 293 and solid volume fractions, respectively. Considering heat conduction only ( $\mathbf{u} = 0$ ), the  
 294 numerical algorithm solves

$$295 \quad \frac{\partial H}{\partial t} = \nabla \cdot (k_a \nabla T), \quad (12)$$

296 where  $H$  is the enthalpy, and the apparent thermal conductivity  $k_a = g_s k_s + g_l k_l$ , where  
 297  $k_s$  and  $k_l$  are the thermal conductivities of the solid and liquid phases respectively. This  
 298 method uses an apparent heat capacity

$$299 \quad c_a = \frac{dH}{dT}, \quad (13)$$

300 where

$$301 \quad H = g_s \int_{T_{ref}}^T \rho_s C_s d\theta + g_l \int_{T_{ref}}^T \rho_l C_l d\theta + \rho_l g_l L, \quad (14)$$

302 such that  $L$  is the latent heat and  $T_{ref}$  is an arbitrary reference temperature;  $C_s$ ,  $\rho_s$  and  
 303  $C_l$ ,  $\rho_l$  are the heat capacities (at constant pressure) and densities from the solid and liquid  
 304 phases, respectively. The apparent heat capacity (per unit volume) is then written as

$$305 \quad c_a = g_s \rho_s C_s + g_l \rho_l C_l + \left( \int_{T_{ref}}^T (\rho_l C_l - \rho_s C_s) d\theta + \rho_l L \right) \frac{dg_l}{dT} \quad (15)$$

306 The numerical implementation thus solves the equation

$$307 \quad c_a \frac{\partial T}{\partial t} = \nabla \cdot (k_a \nabla T). \quad (16)$$

308 In order to assess the effect of the latent heat, we again used the parameters in Table II  
 309 for both liquid and solid phases, resulting in  $c_a = \rho(C_p + L dg_l/dT)$  and  $k_a = k$ , such  
 310 that outside the transition  $c_a = \rho C_p$  [i.e. Eq. (16) is equivalent to Eq. (6)] and during the  
 311 transition  $c_a = \rho C_p + \rho L/\Delta T$ . The melt fraction  $g_l = 1 - g_s$  is assumed to increase with  
 312  $T$  from 0 to 1 at  $T_{melt}$  over an interval of  $\Delta T = 1$  K. This step-like function approximates  
 313 congruent melting.<sup>28</sup>

314 In this case, the only signatures of the phase change in the simulation will be those directly  
 315 due to the latent heat. Choosing a value for the latent heat to be  $L = 300 \text{ kJ/kg}$  (similar  
 316 to water ice melting) we solved the finite element model and compared it to the solution  
 317 with  $L = 0$  (Fig. 3). We observe that when latent heat was accounted for the maximum

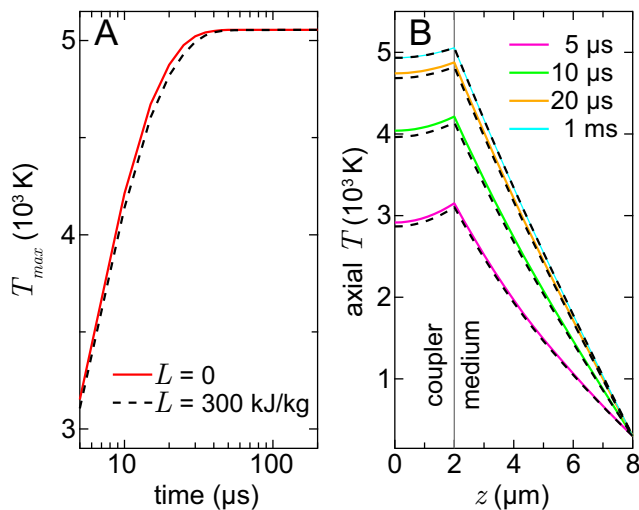


FIG. 3. Effect of latent heat of melting. Models with latent heat  $L = 0$  and  $L = 300 \text{ kJ/kg}$  are compared, for maximum laser power,  $T_{melt} = 400 \text{ K}$ , and neglecting fluid flow. A, time series of the temperature at the center of the coupler surface. The temperature grows faster for  $L = 0$  (solid line) than for  $L > 0$  (dashed line), but reaches the same equilibrium value. B, temperature profiles through the axis of the DAC from the center to the culet for four different snapshots at  $t = 5, 10, 20,$  and  $1000 \mu\text{s}$ , for  $L = 0$  (solid lines) and  $L = 300 \text{ kJ/kg}$  (nearby dashed lines).

319  
 320 temperature is reached later than in the case of  $L = 0$ . However, both simulations reach  
 321 identical maximum temperatures in the steady state limit. It is also possible to observe that  
 322 the temperature distribution over the DAC axis (Fig. 3B) depends on latent heat at earlier  
 323 times but is identical later in the simulation. This can be expected since  $\partial T/\partial t$  vanishes  
 324 when the steady state is reached, and the solution of Eq. (16) becomes independent of  $L$ .  
 325 Thus latent heat has no effect on temperatures for steady-state conditions.

### 326 III. RESULTS

#### 327 A. GENERAL OBSERVATIONS

328 All models develop temperature profiles that are symmetric about a horizontal plane  
329 through the center of the sample, due to use of double-sided laser illumination (Fig. 4A),  
330 with  $T_{max}$  reached at the axial point on the illuminated surfaces. For all models  $T_{min}$  is  
331 constant but the change in laser power changes  $T_{max}$  and the isothermal contours, and thus  
332 melt vesicle shape and size for a given  $T_{melt}$ . The solid:liquid volume ratio in the medium  
333 ranged from zero (fully molten medium,  $T_{melt} = 300$  K) to 0.995 (having two small melt  
334 vesicles at the laser-heated spots).

335 The steady state flow we find for the simulations has a constant general geometry. For  
336 the fully fluid runs ( $T_{melt} = 300$  K) three convection cells develop, with one forming away  
337 from the coupler at the sample edge (Fig. 4B); maximum velocities are found next to the  
338 coupler's outside edge (Fig. 5) and have an upward axial direction. Where the pressure  
339 medium is partially melted ( $T_{melt} > 300$  K), there are two main convection cells where  
340 maximum velocities are directed radially inward (outward) for the sample above (below) the  
341 coupler (Fig. 4C-E). Maximum flow velocity is located in a ring  $\sim 1$   $\mu\text{m}$  above and below the  
342 coupler with a radius of several  $\mu\text{m}$  (Fig. 5).

344 The flow and the maximum velocity are given by pressure imbalances due to the strong  
345 thermal gradients and resulting buoyant forces. There is a correlation between maximum  
346 velocity and differential pressure across the fluid, as well as melt geometry (Fig. 6). Both  
347 maximum velocity and maximum pressure difference are larger for larger values of  $T_{max}$   
348 and lower values of  $T_{melt}$ . Models with a fully fluid medium (lower part of Fig. 6A) and  
349 a convection pattern with a dominant cell away from the coupler (Fig. 4B) show larger  
350 velocities (by a factor of  $\sim 2$ ) than models with partial melting and fluids confined close to  
351 the coupler (upper part of Fig. 6A). This is due to a shift in the planform of convection rather  
352 than to a change in driving pressure, which scales gradually with  $T_{max}$  and  $T_{melt}$  (Fig. 6B).  
353 The maximum pressure difference across the fluid region is 0.036 Pa, for the largest  $T_{max}$   
354 and lowest  $T_{melt}$ , i.e. for fully liquid medium and highest peak temperature. That is, the  
355 larger the fluid volume and temperature variance, the larger the pressure difference across  
356 the volume resulting in faster flow speeds (Fig. 7).



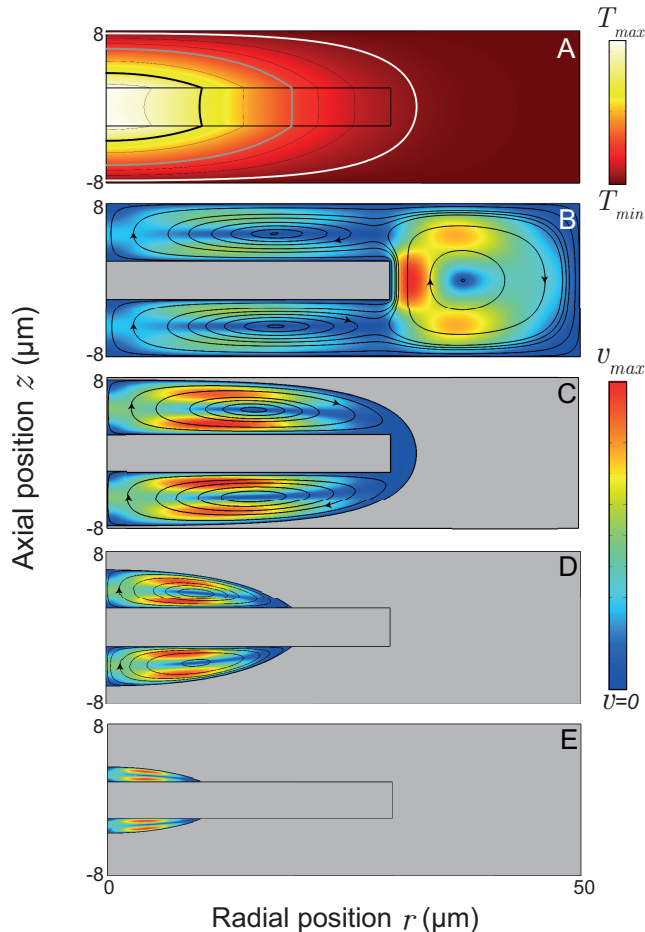


FIG. 4. Axisymmetric cuts of temperature and velocity magnitude for  $T_{max} = 2675$  K. A, temperature map; color indicates temperature; white, grey, and black lines are isothermal contours for 400, 1000, and 2000 K, respectively. B, C, D, and E, velocity maps for  $T_{melt} = 300, 400, 1000,$  and  $2000$  K, respectively; color indicates speed, with  $v_{max} = 0.337, 0.159, 0.0518,$  and  $1.93 \times 10^{-3} \mu\text{m s}^{-1}$ , respectively, for  $\mu_w$  ( $10^{-3}$  Pa s); black lines show the flow streamlines with arrows indicating the direction of the flow.

## 358 B. SCALING BEHAVIOR

359 The velocities found at a given  $T_{melt}$  and  $T_{max}$  (i.e. for a given melt geometry) scale in  
 360 direct proportion to viscosity (Fig. 8). Setting a reference value for viscosity to be  $\mu_w =$   
 361  $10^{-3}$  Pa s, if a corresponding velocity is  $v_w$ , we find that for simulations differing only in  
 362 the assumed value of viscosity the velocity generally scales as  $v = (\mu_w/\mu)v_w$ . Model results  
 363 for velocity presented here at this reference viscosity (i.e., Figs. 4 to 7 and 10B) can be

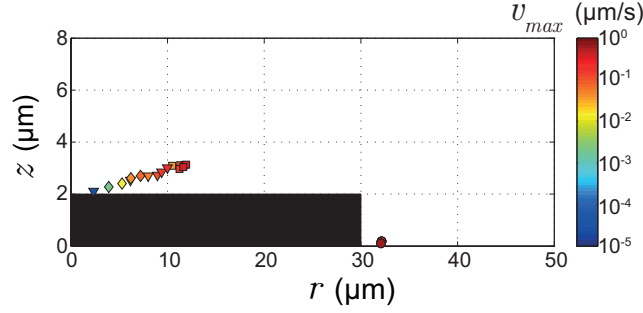


FIG. 5. Location of maximum velocity in the upper half of the sample (bottom half is symmetric). Colors indicate the velocity magnitude for  $\mu_w$ . The symbols represent  $T_{melt} = 300, 400, 1000,$  and  $2000$  K for  $\circ, \square, \nabla,$  and  $\diamond$ , respectively. At maxima locations above the coupler, flow is radially directed; for maxima outside the coupler ( $T_{melt} = 300$  K) flow is axially directed.

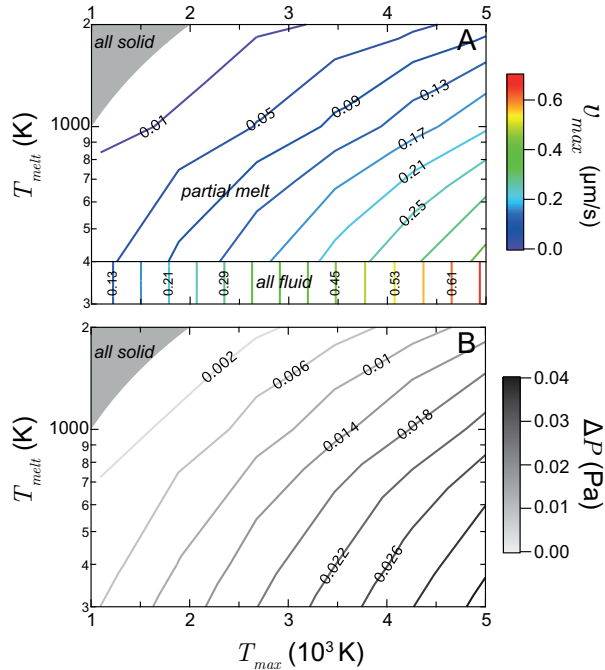


FIG. 6. Contours of A, maximum flow velocity ( $v_{max}$ ) and B, maximum pressure difference across the fluid ( $\Delta P$ ) as a function of  $T_{melt}$  and  $T_{max}$ , for  $\mu_w$ . Velocities at other viscosities can be accurately obtained by multiplying values in A by the ratio of  $\mu_w/\mu$ , whereas  $\Delta P$  is identical for all  $\mu$ . A is separated into two zones depending on the location of the velocity maxima: vertical lines at  $T_{melt} = 300 - 400$  K correspond to a fully fluid case ( $T_{melt} = 300$  K) and contours at  $T_{melt} = 400 - 2000$  K are for partial melting ( $T_{melt} \geq 400$  K).

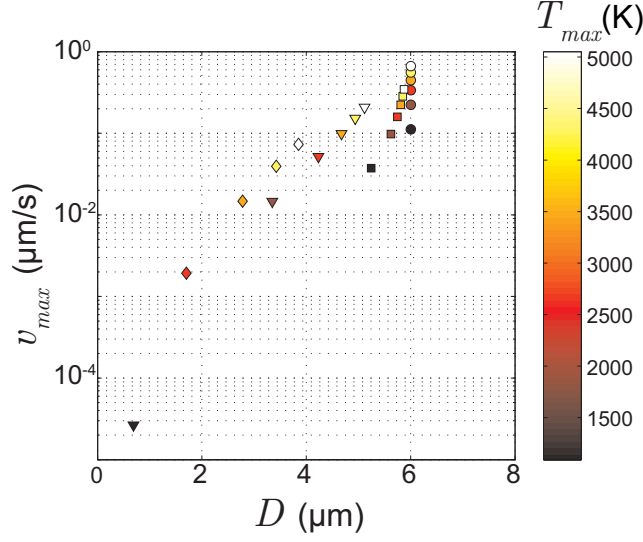


FIG. 7. Plot of maximum velocity versus the characteristic flow length-scale ( $D$ ) for  $\mu_w$ . The symbols correspond to simulations with  $T_{melt} = 300, 400, 1000,$  and  $2000$  K for  $\circ, \square, \nabla,$  and  $\diamond,$  respectively. The colors correspond to  $T_{max}$  in the color bar.

364 accurately adjusted to describe other viscosities using this scaling relationship.

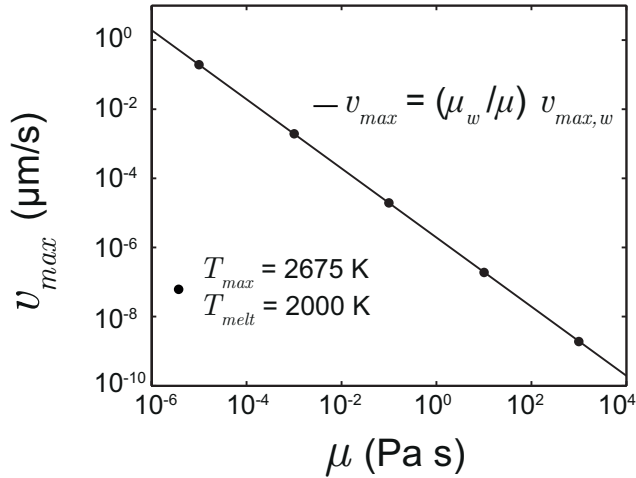


FIG. 8. Scaling of peak velocity  $v_{max}$  with viscosity  $\mu$  for a series of simulations at fixed melt volume as shown in Fig. 4E ( $T_{max} = 2675$  K,  $T_{melt} = 2000$  K).

365 Following Section I we expect that for the present experimental system  $Re \simeq Gr$  should  
 366 provide a good approximation for the dynamics. Indeed, one of the key predictions of this  
 367 model is the inverse proportionality of  $v_{max}$  and  $\mu$  [Eq. (2)], as seen in the simulations  
 368 (Fig. 8). We therefore calculated  $Re$  and  $Gr$  for our dataset to compare with the predictions

369 of dimensional analysis. Given the geometry of this system (Fig. 9A) and our approximation  
 370 that the thermal conductivity of the medium is constant and identical in solid and liquid,  
 371 the axial temperature gradient in the medium is linear (Fig. 9B), and we may transform  
 372  $Re$  and  $Gr$  into known (measurable) parameters in our experimental setup: the maximum  
 373 temperature,  $T_{max}$ , located on the axis of symmetry; the melting temperature  $T_{melt}$ ; the  
 374 minimum temperature  $T_{min}$  corresponding to the anvil surface; and the thicknesses of the  
 375 medium  $d$  and the melt  $D$  along the axis. Hence  $D$  is the characteristic length scale of the  
 376 fluid vesicle. The temperature difference across the liquid zone is then

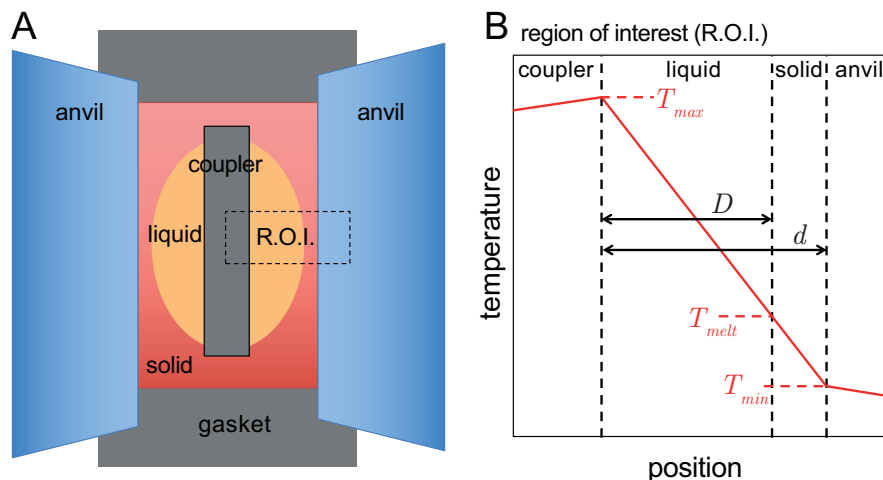


FIG. 9. Simplified geometry of a laser-heated diamond cell. A, the LHDAC configuration. B, a  
 1D view along the axis of symmetry. Panel A highlights the region of interest (R.O.I) around the  
 axis of symmetry corresponding to the temperature distribution in B.

377  
 378

$$\Delta T = T_{max} - T_{melt} \quad (17)$$

379

380 and

$$D = \frac{T_{max} - T_{melt}}{T_{max} - T_{min}} d \quad (18)$$

381

382 With these definitions, we plotted  $Re$  versus  $Gr$ , assuming  $U = v_{max}$  (Fig. 10).

383 The dynamic behavior thus obtained follows a relationship  $Re \propto Gr$ , previously suggested  
 384 by the dimensional analysis [Eqs. (2) and (4)], but  $Re$  and  $v_{max}$  for any given  $Gr$  are lower  
 385 than expected by roughly three orders of magnitude. We can represent the results, for any  
 386 given set of conditions, using a proportionality factor  $A$ , i.e.

387

$$Re = A Gr, \quad (19)$$

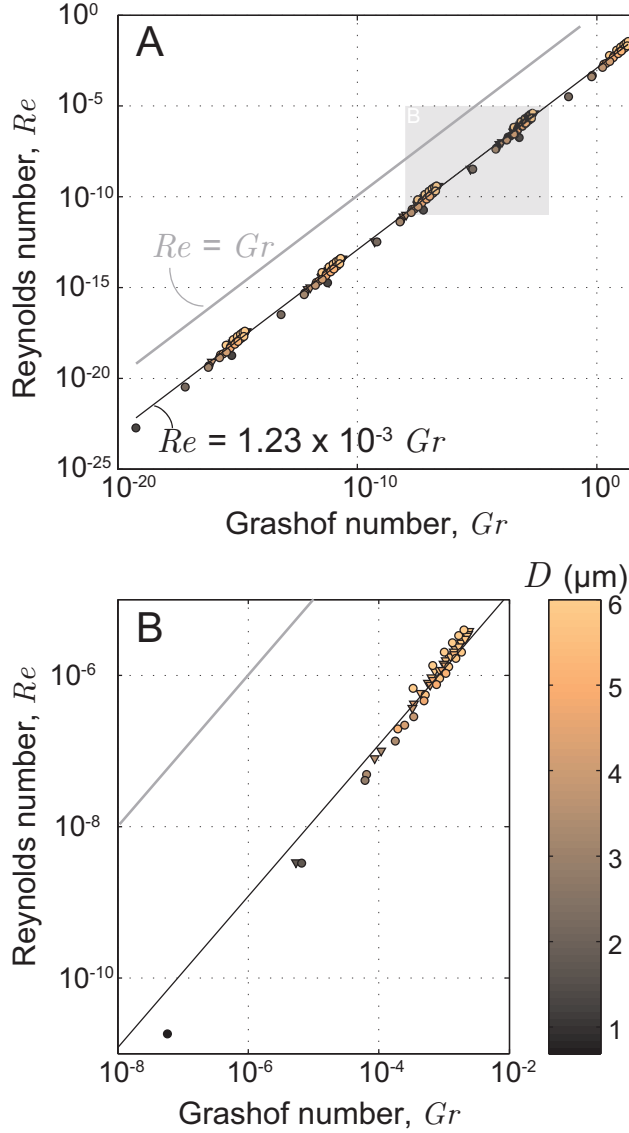


FIG. 10. Reynolds number  $Re$  versus Grashof number  $Gr$  for the complete set of model results. The colors and color bar correspond to the characteristic length scale ( $D$ ) for each simulation. The solid black line is the fit to the relation  $Re = A Gr$  [Eq. (19)], taking  $A$  as a constant. The grey line is the upper bound<sup>21</sup> on  $Re$  [Eq. (4)]. The circles represent simulations that used the isothermal contour at  $T_{melt}$  to define the solid/liquid boundary while the triangles are simulations that used an ellipsoidal function to estimate the boundary position. Panel A shows all simulation results; the fit of Eq. (19) to these data gave  $A = 1.23 \times 10^{-3}$ . Panel B shows only results from simulations with  $\mu_w$ , from the grey region of A.

388 where  $A$  is found to be approximately constant, with the total set of simulations obtained  
 389 closely described with a value of  $A = 1.23 \times 10^{-3}$ . This is consistent with the expectation  
 390 that Eq. (2) provides an upper bound ( $A \leq 1$ ) for velocity in the system.<sup>21</sup>

391 The value of  $A$  is insensitive to the specific geometry and size of the fluid region: it  
 392 is nearly the same for complete melting (Fig. 4B) as for local melting confined to near  
 393 the laser hotspot (Fig. 4E). Some higher-order deviations from a fixed  $A$  are evident, such  
 394 as weakly decreasing  $A$  with melt volume (Fig. 10B). In general, different geometries for  
 395 specific experimental set ups yield different values of  $A$ , sensitive to relative axial and radial  
 396 dimensions, laser spot size, the orientation of gravity, and other assumed characteristics of  
 397 the system.

398 While the prior analysis followed from the assumption that  $Gr \ll 1$  and hence  $Re \propto Gr$   
 399 for the LHDAC, we find  $Gr \gtrsim 1$  at the upper limit of the simulated range (Fig. 10A). At  
 400 such conditions, dimensional analysis implies the inertial contribution to the force balance  
 401 should become non-negligible, manifesting as a different scaling law<sup>46</sup> similar to  $Re \propto \sqrt{Gr}$ .  
 402 However, in our simulations there is no evidence for a deviation from the linear relationship.  
 403 This is likely due to the inertia being smaller than expected from dimensional arguments.  
 404 The scaling laws obtained here thus remain approximately valid throughout the realistic  
 405 parameter space of the LHDAC.

406 Combining Eqs. (17) to (19), the maximum fluid velocity in the liquid medium can be  
 407 described by

$$408 \quad v_{max} = A \lambda \frac{d^2 (T_{max} - T_{melt})^3}{\mu (T_{max} - T_{min})^2}, \quad (20)$$

409 where

$$410 \quad \lambda = \rho g \beta \quad (21)$$

411 is a constant from the physical properties of the material.

412 While coupler melting was not included in the simulations, coupler and medium melting  
 413 share a number of similarities that allow some predictions regarding convective flow in the  
 414 coupler. In the limit of small melt volume, melt vesicles in the coupler and medium have  
 415 similar size and shape,<sup>10</sup> similar boundary conditions (i.e.  $T_{melt} \leq T \leq T_{max}$ ), and are  
 416 expected to exhibit similar flow planform given that flow is symmetric for vesicle inversion  
 417 (Fig. 4D-E). With these similarities, the relationship  $Re = AGr$  [Eq. (19)] should also hold

418 for coupler melting, with similar values of  $A$ , and may be expressed as

$$419 \quad v_{max} = A \lambda \frac{D^2}{\mu} (T_{max} - T_{melt}). \quad (22)$$

420 Together with the earlier conclusion that flow systematics depend little on the particular  
421 geometry of liquid regions, we conclude that a simple scaling law, similar to Eq. (22),  
422 generally describes the thermal convective flow within melts in the LHDAC. Another scenario  
423 that likely follows these systematics is that of direct laser heating and melting of a semi-  
424 transparent medium.<sup>6,21</sup> However, cases where both medium and a coupler melt could be  
425 potentially more complicated: while the above law [Eq. (22)] would plausibly hold for minor  
426 interfacial deformations observed in such experiments that preserve the basic shape and  
427 size of the melted region,<sup>44,49</sup> larger distortions including hole and droplet formation and  
428 multiphase mixing,<sup>50</sup> and associated surface tensions (see Section IV), could significantly  
429 alter flow behavior.

#### 430 IV. DISCUSSION

431 The well-defined relationship between viscosity and convective flow speeds in the LHDAC  
432 suggests velocimetry as a means to establish viscosity in convecting fluids under pressure. At  
433 fixed size of melt, velocities are inversely proportional to viscosity [Eq. (22) and Fig. 8], and  
434 so can vary by many orders of magnitude over the plausible range of viscosities encountered  
435 in fluids. Velocities also increase by orders of magnitude (at constant viscosity) with the  
436 size of the molten region (Fig. 7), which is controlled by initial sample dimensions, melting  
437 temperature, and peak temperature, and may be estimated from these known parameters  
438 [e.g. Eq. (18)] or through direct observation. Velocity is also linearly dependent on density  
439 and thermal expansivity, but given that these are well constrained and relatively invariant  
440 under pressure, their uncertainty should not play a major role in viscosity determination.  
441 Thus, viscosity and melt dimensions are the primary variables determining the convective  
442 flow behavior for any given sample configuration, with the latter being independently mea-  
443 surable. There are hence good prospects for measuring high-pressure viscosity if convection  
444 in the LHDAC can be observed and characterized.

445 It is evident that while thermal convective flow is possible in the LHDAC, it is more  
446 sluggish than previously predicted<sup>21</sup> and may be challenging to detect in many cases. For

447 viscosities on the order of mPas (similar to water), fluid velocities in LHDAC samples due  
 448 to buoyancy flow are expected to be  $\lesssim 1 \mu\text{m s}^{-1}$  (Fig. 7). Assuming a minimum detectable  
 449 flow velocity of  $0.01 \mu\text{m s}^{-1}$  (or roughly  $0.1 \mu\text{m}$  per minute) it is evident that in some of the  
 450 possible parameter space for the LHDAC convective flow will be detectable (Fig. 11). This  
 451 limit assumes that material would have to move by a significant fraction of the wavelength  
 452 of visible light (about  $1 \mu\text{m}$ ) on a typical experimental timescale (about 1 minute) to be de-  
 453 tected optically, such as by direct visual observations<sup>3,8,9,19,32,36,37</sup> or by interference changes  
 454 (i.e. the ‘speckle method’).<sup>10,33–35,38–41</sup> Thermal convection should thus be readily visible for

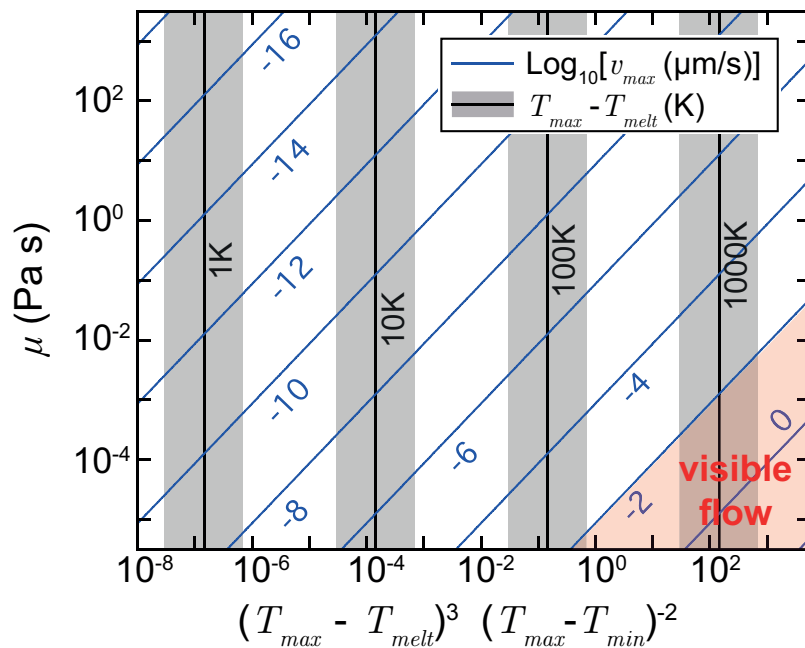


FIG. 11. Flow velocity as a function of viscosity and temperature above melting. Blue lines are velocity contours labeled with the logarithmic velocity in  $\mu\text{m s}^{-1}$ , after Eq. (20). Black vertical lines with grey envelopes are the conditions of experiments where peak temperature (1,500-6,000 K) exceeds the melting point by 1, 10, 100, and 1000 K. The red shaded region in the lower right represents the domain where natural convection could be readily observed ( $v_{max} > 10^{-2} \mu\text{m s}^{-1}$ ).

455  
456

457 viscosities similar to water, or lower.

458 Furthermore, the melting temperature must be exceeded significantly, by 100-1000 K  
 459 according to our models (Fig. 11), before convection is detectable. Naturally,  $D$  and  
 460  $T_{max} - T_{melt}$  (and hence convective vigor) [Eq. (22)] tend to zero as  $T_{max} \rightarrow T_{melt}$ , and con-  
 461 vection at the melt temperature is not possible regardless of the size of the molten region;



462 but our results show that considerable overheating is necessary to produce observable flow.  
 463 This questions the feasibility of reliably detecting melting via convective motion, suggesting  
 464 that significant overestimates of melting temperature are possible if convective motion is  
 465 used as a criterion. Indeed, in experiments, initial motion associated with melt may be  
 466 difficult to see, with ‘clear, continuous convection’ observed only several hundred degrees K  
 467 above the putative melting point.<sup>36,37</sup> However, it should be noted that measurements using  
 468 *in-situ* motion-based criteria more often underestimate melting temperatures compared to  
 469 other measurement techniques and theoretical predictions.<sup>1,4,14–17,42–44</sup> This suggests that  
 470 the motion observed in many experiments at proposed melting points may not be due to  
 471 thermal convection, but other causes, as considered in more detail below.

472 The significant overestimation of velocity using order of magnitude dimensional arguments<sup>21,46</sup>  
 473 can be explained, in part, by the very confined geometry of melts in the LHDAC, such that  
 474 the convecting material is at all points being deflected by the boundary of the liquid region  
 475 rather than freely rising and falling in free space. That the factor  $A$  decreases with the size  
 476 of the molten region (Fig. 10B) is further suggestive of this confinement effect.

477 Another apparent control on peak velocity is that the simulated geometry approaches that  
 478 of plane-layer convection near the laser heating spot. In perfectly plane-layer (i.e. Rayleigh-  
 479 Bénard) natural convection, with liquid confined in a horizontal layer, perpendicular to  
 480 gravity, across which a temperature difference is imposed, convection is inhibited for sub-  
 481 critical  $Ra$  (i.e.  $Ra \lesssim 10^3$ , as characterize the LHDAC). This stability criterion does not  
 482 generally apply in the LHDAC due to the horizontal thermal gradients.<sup>21</sup> However, horizontal  
 483 gradients tend to zero close to the sample hotspot (at  $r = 0$ , Figs. 4 and 9), and this evidently  
 484 inhibits flow in this region. Despite this near-hotspot region having the largest local liquid  
 485 thickness  $D$  and local temperature gradient  $|\nabla T|$ , peak velocities tend to occur elsewhere,  
 486 in adjacent areas of the melt (Fig. 4C-E) having smaller  $D$  and  $|\nabla T|$  (Fig. 4A) but nonzero  
 487 horizontal temperature gradients  $\partial T/\partial r$ . This contrasts with expectations from the scaling  
 488 behavior developed and validated generally in this work that flow velocity should follow a  
 489 relation similar to

$$490 \quad U \propto D^3 |\nabla T|. \quad (23)$$

491 Consequently the largest flow velocities in the LHDAC occur not at the hotspot, but rather  
 492 around it in a toroidal or ring-like convecting region (see also Fig. 5). This further reflects  
 493 the strong geometric controls on convective vigor in LHDAC melts.

494 Buoyant pressure differences across liquid regions that drive natural convection are ex-  
 495 ceedingly small (of order  $10^{-2}$  Pa, Fig. 6B), and so if convective motion is possible, motions  
 496 driven by other forces of larger magnitude are also possible and, when present, may supersede  
 497 convection as the dominant mechanism of motion. Non-hydrostatic pressure gradients across  
 498 solid samples imposed on compression in typical DAC experiments can be of the same order  
 499 as the static pressure, i.e.,  $\sim 10^9$  Pa, and could drive sudden, rapid motion as melting occurred.  
 500 Boundaries in samples (such as planar coupler-medium interfaces) also routinely deform near  
 501 melting, often into a bead- or droplet-like features<sup>3,9,32,35,36,44,49</sup> presumably arising from sur-  
 502 face tension; the pressure associated with surface tension is of order  $2\gamma/R$  or  $\sim 10^3$  Pa for  
 503 equilibrium interfacial radius of curvature  $R \approx 10^{-5}$  m (determined experimentally<sup>44,49</sup>) and  
 504 typical surface energy  $\gamma \approx 10^{-2}$  N m<sup>-1</sup>. Also significant are stresses induced by thermal ex-  
 505 pansion upon heating to the melting point (of order  $\beta K_T [T_{melt} - T_{min}]$  or  $\sim 10^9$  Pa, for bulk  
 506 modulus  $K_T \approx 10^{10}$  Pa and  $T_{melt} \approx 10^3$  K) or by phase transformation, i.e. induced by the  
 507 melting process itself (of order  $K_T \Delta V/V$  or  $\sim 10^8$  Pa, for relative volume change  $\Delta V/V \approx 1$   
 508 % as in high-pressure melting). In addition to the associated forces being significant in the  
 509 context of driving fluid flow, phase change,<sup>39,42</sup> surface tensional adjustment, and thermal  
 510 expansion imply motion directly. Brownian motion has also been proposed as a cause of  
 511 motion in the LHDAC,<sup>19</sup> though this effect seems limited to cases where mixed phases are  
 512 present, such as for inhomogeneous or incongruent melting, suspensions or colloids.

513 Most of these phenomena and the associated forces (with the exception of Brownian  
 514 motion) would be transient in nature, annealing out with time at constant temperature, and  
 515 so flow and other motion due to them might dissipate as an equilibrium state is reached,  
 516 and be distinguishable from the continuous motion of thermal convection achieved in the  
 517 the long-duration limit (the scenario examined in this study). Transient modes of motion  
 518 reported in experiments,<sup>36,37,39</sup> such as ‘occasional small movements’, ‘abrupt, discontinuous  
 519 change’, or ‘disappearance’ of motion, may possibly originate in temporary, annealing driving  
 520 forces. In the interest of interpreting motion in terms of material viscosity, it is expected  
 521 that the character of motion depends on and can indicate the primary driving mechanism;  
 522 observations of flow planform, duration, and temperature-dependence could help isolate the  
 523 appropriate physical model and thereby enable viscometry. Perhaps most usefully, we find  
 524 that it is reasonable to interpret persistent motion as being due to convection as it seems  
 525 difficult to explain this generally through other means.

526 Thermal instabilities that create thermal pressure fluctuations in an already molten sam-  
 527 ple have also been previously proposed as driving continuous flow,<sup>19,28</sup> however this possibil-  
 528 ity is difficult to substantiate. A thermal perturbation  $\Delta T_i$ , operating through thermal ex-  
 529 pansion, could drive flow at a velocity comparable to natural convection if  $\Delta T_i \approx \Delta P_i / \beta K_T$   
 530 where  $\Delta P_i$  is the buoyant pressure difference across the fluid region in convection, i.e.  
 531  $\sim 10^{-2}$  Pa (Fig. 6). This implies  $\Delta T_i \approx 10^{-7}$  K. Such temperature fluctuations are almost  
 532 certainly present even under the most stable heating conditions. However, thermal pres-  
 533 sure fluctuations of this type relax very quickly in hydrostatic conditions, on the timescale  
 534 of pressure wave propagation,  $\tau_s \simeq D/v_B$ , where  $v_B$  the bulk sound velocity – i.e within  
 535  $\sim 1$  ns. This is probably not sufficient time to produce detectable flow even if the pressure  
 536 perturbations, and the associated flow speeds, were substantially larger than for natural  
 537 convection; moreover, as the thermal response time of the LHDAC is significantly longer  
 538 than this ( $\tau_\kappa \gg \tau_s$ ) it seems unlikely that large-scale thermal pressure perturbations could  
 539 be imposed within the required timescale. Thus we conclude that differential thermal pres-  
 540 sures are probably not produced in the fluid in nominally continuous heating. A plausible  
 541 way thermal fluctuations could influence flow would be via the buoyancy force itself. To  
 542 further examine this issue of instability driven flow, we have tested flow sensitivity to tem-  
 543 perature fluctuations in our simulations by introducing a sinusoidal instability in the laser  
 544 power and examining its influence on flow (Fig. 12). For  $\mu_w$ , only fluctuations at a frequency  
 545 below  $\sim 100$  kHz influence the flow significantly. This is due to the finite response time of  
 546 the system (Section IIC), on the order of microseconds ( $\tau_\kappa$ ) in this case, such that more  
 547 rapid fluctuations in laser power are damped and only weakly influence temperature while  
 548 having no discernible influence on flow. In cases where the flow is influenced, convective  
 549 flow velocity is only weakly modulated, and thus this phenomenon is not likely to enhance  
 550 detectability of motion beyond that of steady thermal convection. While thermal fluctu-  
 551 ations are thus unlikely to directly lead to detection of fluid motion, they may indirectly  
 552 lead to motion via the rapid conductive adjustment of temperature gradients producing, for  
 553 example, phase changes and melt boundary migration.<sup>39,42</sup>

555 In any case, the alternative forcings explored above can in principle modify the fluid  
 556 flow but do not affect the relationship between flow onset and melting. However, on  
 557 a final note, solids in a high-temperature solid-solid phase transforming,<sup>10,15,39,51</sup> rapidly  
 558 recrystallizing,<sup>4,10,16,17,42,52</sup> or thermally-softened<sup>14,17,42,43</sup> regime could also play a role in

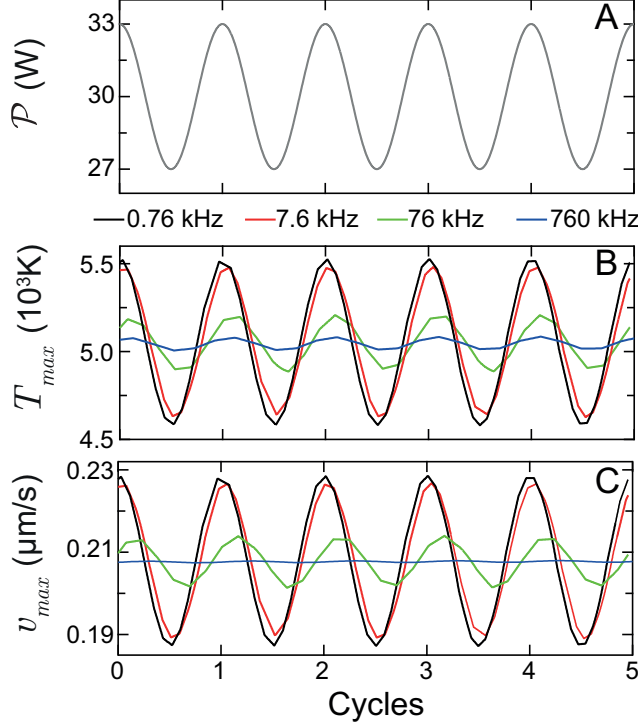


FIG. 12. Effect of fluctuating laser power (A) on temperature (B) and flow velocity (C) for frequencies ranging from 0.76 to 760 kHz, for  $\mu_w$ ,  $T_{melt}=1000$  K, and  $T_{max}=5051$  K. Above 100 kHz ( $\sim 1/\tau_\kappa$ ), the effect of fluctuations on temperature is dramatically reduced and the effect on velocity is negligible and damped by the response time of the system. Variations in fluid dimensions due to temperature change were not considered.

559 thermally induced motions, and in some cases solid states might respond to the same forces  
 560 that could affect the fluid states – even, possibly, to the buoyant force. For example, in  
 561 principle a viscoelastic state<sup>17</sup> could undergo thermal convection; or recrystallization could  
 562 be induced by the buoyant stresses. Such phenomena could lead to underestimation of melt  
 563 temperature by motion criteria (cases of Fe<sup>3,4</sup> and Ta<sup>16,35,44</sup> have been discussed), however  
 564 the behavior of solids is beyond the scope of this study.

565 Accounting for latent heat associated with melting only influences the behavior of the  
 566 sample when temperatures are unsteady – for example, when temperatures are changing  
 567 as the simulation is heating up and approaching an equilibrium steady-state (Fig. 3). In  
 568 the steady-state limit, phase change is not occurring and no energy is used in transforming  
 569 material, so latent heat does not play a direct role in defining the temperature distribution  
 570 in the sample, the position of the melt boundary, or the laser power required to sustain the

571 given temperature. This is consistent with previous conclusions<sup>27,28</sup> that latent heat alone  
572 has little to no effect on the thermal response of the LHDAC, particularly in the steady  
573 state limit. Thus our result supports the conclusion that ‘plateau’-like deviations from a  
574 smooth, continuous increase in temperature with laser power, often seen experimentally near  
575 melting and often associated with visible motion,<sup>3,6,9,19,36,37,41,45</sup> cannot be caused by latent  
576 heat and must instead be caused most directly by changes in material physical properties<sup>27,28</sup>  
577 or dynamic phenomena such as rapid convective heat transfer.<sup>28</sup> While our study rules out  
578 natural convection as a cause of the plateau effect, flow driven by other forces, as discussed  
579 above, might play a role if it were particularly vigorous and persistent.

## 580 V. CONCLUSIONS

581 This study confirms that natural convection is possible in fluids in the laser-heated dia-  
582 mond anvil cell for a typical experimental configuration, consistent with previous order-of-  
583 magnitude estimates<sup>21</sup> and qualitative assessment of experiments.<sup>3,9,32,34,36–42</sup> Natural con-  
584 vective motion cannot affect the energy balance of the diamond cell – thermal conduction  
585 remains the dominant mechanism of energy transfer in the LHDAC – so the natural convec-  
586 tion can be thought of as a passive response to temperature gradients. Flow velocities are  
587 found to be significantly less than the upper bound expected on the basis of dimensional  
588 analysis.<sup>21,46</sup> We found that the dynamics of natural convection in the LHDAC follow a scal-  
589 ing law [Eq. (22)] where the Reynolds number ( $Re$ ) is proportional to the Grashof number  
590 ( $Gr$ ), or  $Re = AGr$ , with a constant of proportionality  $A \simeq 10^{-3}$ . This scaling behavior is  
591 expected to be of general validity for the LHDAC when gravity is parallel to the symmetry  
592 axis.

593 The routine, wide-ranging observations of motion at high-temperatures in the LHDAC,<sup>3,8–10,19,32–41</sup>  
594 the observation of ‘vigorous’ and rapid motion, and the common attribution of this motion  
595 to melting and convection, is somewhat in contrast with our conclusion that convective  
596 fluid flow would be difficult or impossible to observe in real time when the melting point  
597 is just exceeded (Figs 6A and 11). Flow speed increases quadratically with the length  
598 scale of the molten region and linearly with the temperature difference across the melt  
599 [Eqs (2) and (22)], such that convective flow appears gradually above the melting point,  
600 strengthening with increasing peak temperature (and hence melt volume) and becoming

601 realistically detectable only when the melting point is significantly exceeded (by 100-1000  
602 K in representative cases). Thus relating an observation of genuine convective motion to  
603 melting is not straightforward, and suggests most directly an upper bound on melt tem-  
604 perature. Documented motions with different behavior, such as a sudden onset of vigorous  
605 motion with increasing temperature, or transient motion at constant temperature, might  
606 be driven by other forces (related to sample annealing), and could occur at or nearer to  
607 precise melting points, and potentially below them (as for fast recrystallization<sup>4,10,16,17,42,52</sup>).  
608 Indeed, non-convective motions could dominate in a number of scenarios. There is thus  
609 a need to identify the dominant causes of flow and motion in the LHDAC and hence the  
610 relationship of these motions to melt temperatures and melt properties. Continuous, steady  
611 fluid motion is likely an indication that convection is occurring, providing a simple initial  
612 test of whether the observed process of motion is plausibly convective in nature. Our study  
613 predicts specific observables, such as convection in a ring or torus for axially oriented gravity,  
614 annealing-driven flow, and temperature-dependence of flow vigor, that can better inform  
615 the true nature of flow phenomena, and their origin in convection or otherwise.

616 Another common criterion for high-pressure melting are anomalies (such as plateaus)  
617 in temperature observed when increasing laser power through melting points.<sup>3,6,9,19,36,37,41,45</sup>  
618 Our models rule out both latent heat of melting and fluid flow as potential causes for  
619 these anomalies, assuming well-annealed samples at thermal equilibrium. This restricts the  
620 possible origin of such plateaus, with the most probable remaining general explanation being  
621 changes in material properties upon melting (e.g. thermal conductivity, heat capacity, or  
622 optical properties). Studies of motion and temperature as a function of both laser power  
623 and time since power increase could yield valuable information about the nature of motion,  
624 its principal causes, and its relationship to melting and other common melting criteria.

625 It is interesting to note that, as demonstrated in our simulations, pressure gradients can  
626 never be fully annealed in the LHDAC as buoyant pressure differences always exist. Whether  
627 the liquid (or solid) responds to these buoyancy forces on an experimental timescale is  
628 dependent on the material properties. Buoyant forces should become increasingly important  
629 at high temperatures where material softening, melting, recrystallization and other forms of  
630 annealing are increasingly available to relax shear stresses.

631 The measurement of fluid transport properties at conditions of extreme pressure and  
632 temperature is a longstanding challenge. Due to the strong control of flow speed by viscosity

633 in LHDAC convection, there are good prospects for determining viscosity at high pressure  
634 using the melt production and flow behavior induced by laser heating. If the origin of  
635 flow is natural convection, the flow velocity is inversely proportional to viscosity [Eq. (22)].  
636 Since viscosity varies by roughly 10 orders of magnitude over the typical viscosity range  
637 of natural fluids, the relatively minor uncertainties in the other parameters appearing in  
638 the scaling model [Eq. (22)] (e.g. melt size, melt temperature, and peak temperature) do  
639 not have a major influence on determining, at least, the order of magnitude of viscosity. If  
640 melt dimensions could be assessed precisely, for example by direct observation as part of  
641 fluid velocity measurements, the quality of the viscometry could be particularly accurate.  
642 Recent efforts to quantify motion via the changing speckle pattern of laser light reflected  
643 from molten samples suggests one way to assess the vigor and rate of flow,<sup>41</sup> however a  
644 physical understanding of the relationship between speckle changes and flow rates must  
645 be established. In any case, more direct probes of flow rates, streamlines, and spatial  
646 distributions may be required to provide a complete comparison to models and suitable  
647 data for accurate viscometry.

648 Observation of convective motion alone can be enough to place a significant constraint  
649 on viscosity. Only convective flow in fluids with viscosities similar to water ( $\sim 10^{-3}$  Pa s), or  
650 lower, are readily detectable in the LHDAC according to our simulations (Fig. 11). Mean-  
651 while, condensed fluids rarely exhibit viscosities much lower than  $10^{-4}$  Pa s (group 1 and  
652 low-Z group 18 elements being notable exceptions). Thus it is likely that, in most cases,  
653 detectable convection corresponds to a viscosity within about an order of magnitude of that  
654 of water. For example, the routine observation of apparent convective motion in molten Fe  
655 under pressure<sup>3,8,9,36</sup> is consistent with the common assumption that molten Fe at Earth's  
656 core conditions has a viscosity similar to water.<sup>2,53</sup> This also suggests that melt detection by  
657 sample convective motion should not be possible for viscous melts such as silicate liquids.

658 In summary, the intrinsic natural convection in melts produced by laser heating in the  
659 diamond anvil cell may be one way of measuring fluid viscosities at extreme pressure and  
660 temperature. In addition to providing essential data on fluid transport under pressure, as  
661 relevant to melts in planetary deep interiors, high-pressure viscosity measurements offer one  
662 way to characterize pressure-induced changes in fluid bonding and structure that may be  
663 otherwise difficult to detect, such as liquid-liquid phase transformation, polymerization or  
664 dissociation. Our results suggest a novel approach to measuring viscosity in the laser-heated

665 diamond cell, by comparing observations of convective flow speeds in melts with numerical  
666 models. Such models are essential for describing this unique case of convection at ultra-low  
667 Rayleigh number, in which geometric controls on flow are especially pronounced. Theoretical,  
668 *ab-initio* descriptions of materials transport and mechanical properties at extremes can  
669 also assist in the collection and interpretation of motion data. Of particular interest for theoretical  
670 investigation are the viscosities of high pressure liquids, but mechanical properties  
671 of high pressure-temperature solids are also needed, for example, where melt temperatures  
672 approach bond-dissociation and diffusion-activation energies<sup>5</sup> and where viscoelastic<sup>17</sup> or  
673 rapidly-recrystallizing<sup>4,10,16,17,42,52</sup> states appear.

## 674 ACKNOWLEDGEMENTS

675 We thank two anonymous reviewers for helpful comments on this manuscript. This work  
676 was supported by the British Council Researcher Links Programme, and the Carnegie Trust  
677 Research Incentive Grant no. 70249.

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