



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

## Modelling the formation of explosively formed projectiles (EFP)

**Citation for published version:**

Cardoso, D & Teixeira-Dias, F 2016, 'Modelling the formation of explosively formed projectiles (EFP)', *International Journal of Impact Engineering*, vol. 93, pp. 116-127.  
<https://doi.org/10.1016/j.ijimpeng.2016.02.014>

**Digital Object Identifier (DOI):**

[10.1016/j.ijimpeng.2016.02.014](https://doi.org/10.1016/j.ijimpeng.2016.02.014)

**Link:**

[Link to publication record in Edinburgh Research Explorer](#)

**Document Version:**

Peer reviewed version

**Published In:**

International Journal of Impact Engineering

**General rights**

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

**Take down policy**

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact [openaccess@ed.ac.uk](mailto:openaccess@ed.ac.uk) providing details, and we will remove access to the work immediately and investigate your claim.



Manuscript Number: IE-D-15-00316

Title: Modelling the formation of Explosively Formed Projectiles (EFP)

Article Type: Original Research Paper

Keywords: Explosively formed projectile; EFP; improvised explosive device; IED; high strain-rate; detonation; projectile; finite element method

Corresponding Author: Dr. Filipe Teixeira-Dias, BEng, MSc, PhD, Hab

Corresponding Author's Institution: University of Edinburgh

First Author: Diogo Cardoso

Order of Authors: Diogo Cardoso; Filipe Teixeira-Dias, BEng, MSc, PhD, Hab

**Abstract:** The number of victims of attacks from Improvised Explosive Devices (IED), especially from roadside bombs where Explosively Formed Projectiles (EFP) are frequently used, has steeply increased until 2011. Understanding these threats, how they are built and predicting how they interact with targets is of utmost importance. For this purpose it is first necessary to understand how EFPs are formed and what parameters influence their behaviour and performance. The work in this paper proposes and describes a numerical simulation methodology that allows to reproduce the conditions of formation and ballistic capabilities of explosively formed projectiles. Different EFP configurations, materials and detonation conditions are evaluated and assessed against the performance (e.g. stable flight velocity) of the resulting projectile. The model proposed is based on a generic EFP with an aspect ratio of approximately 1 and a case/base thickness of 5 mm. The dynamic interactions between the various components of the EFP are established through specific contact algorithms that allow to interpolate the resulting pressure from detonation to the remaining components, resulting in their acceleration and consequent deformation. The model is validated against experimental observations and afterwards used to assess the influence of the liner materials and thickness, high-explosive, number and off-centre distance of detonators. The performance of the EFPs is quantified from their configuration and a set of non-dimensional geometrical parameters. It is shown that the thickness (and thickness variability) of the liner is one of the most important factors, along with the off-centre distance of the detonator(s). Within the materials and range of parameters tested, the most performant and aggressive EFP has a liner with thickness between 4 and 7% of its diameter, a copper liner and dynamite high-explosive (HE).



SCHOOL of ENGINEERING

INSTITUTE for INFRASTRUCTURE and ENVIRONMENT

The University of Edinburgh  
Alexander Graham Bell Building  
The King's Buildings  
Edinburgh EH9 3JL  
Scotland, UK

Tel: +44 (0)131 650 6768

Fax : +44 (0)131 650 6554

Email: F.Teixeira-Dias@ed.ac.uk

Dear Professor Magnus Langseth,  
Editor-in-Chief of the International Journal of Impact Engineering,

Please find attached to this cover letter the manuscript entitled *Modelling the formation of Explosively Formed Projectiles (EFP)*, from the authors D. Cardoso and F. Teixeira-Dias.

The work in this manuscript proposes, describes and validates a numerical simulation methodology that allows to reproduce the conditions of formation and ballistic capabilities of explosively formed projectiles (EFP). Different EFP configurations, materials and detonation conditions are evaluated and assessed against the performance (*e.g.* stable flight velocity) of the resulting projectiles. The model proposed is based on a generic EFP, is validated against experimental observations and used to assess the influence of the liner materials and thickness, high-explosive, number and off-centre distance of detonators on the performance of the EFP, quantified from their configuration and a set of non-dimensional geometrical parameters.

We hope that this paper can be accepted for publication in the International Journal of Impact Engineering.

With best wishes,

The University of Edinburgh, 1 June 2015

---

*Filipe Teixeira-Dias*

HEAD OF SCHOOL: Professor Hugh McCann FREng

HEAD OF INSTITUTE: Professor of Structural Engineering and Computational Mechanics Asif Usmani

Arup Professor of Structures and Fire Luke Bisby

Carillion Professor Michael C Forde FREng, FRSE

Professor of Structural Mechanics Yong Lu

Professor of Particulate Solid Mechanics Jin Y Ooi

Professor of Civil Engineering J Michael Rotter FREng, FRSE

BRE Professor of Fire Safety Engineering Albert Simeoni

Professors Emeritii: D Dougal Drysdale, FRSE Arnold W Hendry, FRSE Braj P Sinha

---

**Title**

Modelling the formation of Explosively Formed Projectiles (EFP)

**Authors**

D. Cardoso, F. Teixeira-Dias

**Submitted to**

International Journal of Impact Engineering

**Date**

1 June 2015

---

**Highlights**

- Authors model the formation process of explosively formed projectiles.
- Study influence of materials (liner, HE) and detonation parameters.
- Stable flight velocity is strongly influenced by liner thickness variability.
- Kinetic energy of resulting projectile highly dependent on detonation parameters.



# Modelling the formation of Explosively Formed Projectiles (EFP)

D. Cardoso<sup>a</sup>, F. Teixeira-Dias<sup>b,\*</sup>

<sup>a</sup>*GRIDS, Universidade de Aveiro, Portugal*

<sup>b</sup>*School of Engineering, The University of Edinburgh, Edinburgh EH9 3JL, UK*

---

## Abstract

The number of victims of attacks from Improvised Explosive Devices (IED), especially from roadside bombs where Explosively Formed Projectiles (EFP) are frequently used, has steeply increased until 2011. Understanding these threats, how they are built and predicting how they interact with targets is of utmost importance. For this purpose it is first necessary to understand how EFPs are formed and what parameters influence their behaviour and performance. The work in this paper proposes and describes a numerical simulation methodology that allows to reproduce the conditions of formation and ballistic capabilities of explosively formed projectiles. Different EFP configurations, materials and detonation conditions are evaluated and assessed against the performance (*e.g.* stable flight velocity) of the resulting projectile. The model proposed is based on a generic EFP with an aspect ratio of approximately 1 and a case/base thickness of 5 mm. The dynamic interactions between the various components of the EFP are established through specific contact algorithms that allow to interpolate the resulting pressure from detonation to the remaining components, resulting in their

acceleration and consequent deformation. The model is validated against experimental observations and afterwards used to assess the influence of the liner materials and thickness, high-explosive, number and off-centre distance of detonators. The performance of the EFPs is quantified from their configuration and a set of non-dimensional geometrical parameters. It is shown that the thickness (and thickness variability) of the liner is one of the most important factors, along with the off-centre distance of the detonator(s). Within the materials and range of parameters tested, the most performant and aggressive EFP has a liner with thickness between 4 and 7% of its diameter, a copper liner and dynamite high-explosive (HE).

*Keywords:* Explosively formed projectile; EFP; improvised explosive device; IED; high strain-rate; detonation; projectile; finite element method.

---

## 1. Introduction and state-of-the-art

Shock waves from the detonation of an high-explosive (HE) can be used to deform and warp a liner of ductile metal, forming Explosively Formed Projectiles (EFP), also known as Self-Forging Fragments (SFF). These compact projectiles can reach velocities in excess of 1000 m/s, with the consequent kinetic energy.

The first publications with reference to devices similar to present-day EFPs appeared in 1935 [1] and 1936 [2]. However, it was not until the 1970s that related studies significantly increased. Johnson [3] firstly demonstrated

---

\*Corresponding author: F.Teixeira-Dias@ed.ac.uk

10 the existence of three-dimensional numerical modelling capabilities of the  
 11 explosive-metal interaction using complex surfaces. To this end, this author  
 12 used the example of an explosive that accelerates a metal projectile after  
 13 detonation. This study investigated: (i) the effect of shell (liner) thickness,  
 14 from  $0.9t_0$  at the edge of the liner up to  $1.1t_0$  in its centre ( $t_0$  being the thick-  
 15 ness of a projectile with an equivalent mass), (ii) the effect of an off-centre  
 16 detonation and (iii) the effect of an uneven distribution of the density of  
 17 the high explosive. It was shown that these parameters significantly influ-  
 18 ence the stable flight velocity of the projectile. More recently, Johnson [4]  
 19 explored issues related to modelling three-dimensional EFP, explaining the  
 20 effects of the contact interface, discretisation and finite element approach.  
 21 Similar computational topics were extensively researched by Zukas *et al.* [5],  
 22 Taylor [6], Nyström *et al.* [7] and Molinari [8], focusing on aspects such as  
 23 the effect of meshing, blast load intensity, constitutive modelling and the  
 24 use of alternative methods (*e.g.* Smooth Particle Hydrodynamics, SPH).

25 Geometrical parameters are known to play an important role on the  
 26 formation of an EFP. Miller [9] and Brown *et al.* [10] provided a set of  
 27 EFP design criteria based on projectile velocity or mass concentration. We-  
 28 ickert *et al.* [11] and Chuan *et al.* [12] discuss different design approaches,  
 29 focusing on target penetration. One of the most significant and influential  
 30 parameters is the aspect ratio (length-to-diameter ratio) of the explosive  
 31 before detonation, which led Bender and Carleone [13] to conclude that the  
 32 kinetic energy of the projectile increases with this ratio up to a maximum

of 1.5. Another important observation was the effect of adding mass to the casing, increasing the duration of the shock wave propagation and consequently the total energy transferred to the projectile. Weimann [14] and Weickert and Gallagher [15] demonstrated that adding a reinforcement ring to the case and liner has a significant effect on the shape, configuration and velocity of the resulting EFP, eventually even providing fins that aerodynamically stabilise the projectile during its flight. Bender and Carleone [16] submitted a patent in 1994 explaining the use of a thin radial spacer between the projectile and the high-explosive, leading to periodic thickness variations and, consequently, the formation of fins.

Pappu and Murr [17] analysed, both experimentally and numerically, the characteristics of residual microstructures of several EFPs, testing three different liner materials (tantalum, iron and copper) using two constitutive models for each material (Johnson-Cook [18, 19] and Zerilli-Armstrong [20]). They concluded that, although the selected materials have been widely used in EFP [21, 22, 23, 24], they lead to completely distinct behaviour, influencing the melting temperature and the mechanisms by which the crystal structure deforms. The Zerilli-Armstrong model [20] led to better results for tantalum (Ta) projectiles, unlike iron (Fe) that exhibited better results with the Johnson-Cook model. Results were similar, however, for the copper (Cu) projectiles.

More recently, Wu *et al.* [25] studied the formation, flight and penetration performance of EFPs using a single geometric configuration with an

56 Arbitrary Lagrangian-Eulerian (ALE) approach. These authors considered  
57 air drag during flight through an attenuation rate equation for a fixed flight  
58 distance (of 48 m). The projectile velocity was analysed both with the sim-  
59 ilarity theory and the numerical simulation results, which were validated  
60 by experimental residual velocity measurements after impact on a 25 mm  
61 ballistic steel target. It was concluded that it is still possible to optimise  
62 the geometry of the EFP by combining the shape of the explosive and liner.  
63 As simulating the flight of the EFP is complex and impractical, only 0.5 m  
64 of flight were analysed, nonetheless leading to reasonably accurate results.  
65 The attenuation method can be considered accurate, with a loss of speed of  
66 approximately 6.4 m/s per meter of flight, consistent with the experimental  
67 results. The use of the similarity theory can be useful to solve technical  
68 problems associated to the determination of the entire flight of the EFP:  
69 the error obtained on the residual velocity for a 0.5 m flight is lower than  
70 10%. Finally, by comparing the velocity and penetration on the target re-  
71 sults, Wu *et al.* [25] concluded that simulations can reasonably predict the  
72 final shape, mass, velocity, flight stability and penetration performance of  
73 an EFP.

74 Li *et al.* [26] examined the effects of the position, timing and number  
75 of detonation points on the formation of the EFP, concluding that the sta-  
76 ble flight velocity of the projectile increases with the number of detonation  
77 points, observing that for a 60 mm diameter EFP the signal delay between  
78 detonators should not be above 200  $\mu$ s. Experimental results confirm that

79 for certain flight distances the penetration capacity doubles and the perfo-  
80 ration diameter reduces by as much as 40%.

81 According to statistics published by the Center for Strategic & Inter-  
82 national Studies (CSIS) [27] and data from the US Department of Defense  
83 published by The Washington Post in 2011 [28] and 2014 [29], the number  
84 of casualties due to Improvised Explosive Devices (IED) in Iraq strongly  
85 increased from 2009 to 2010, with increases as high as 60% on some peri-  
86 ods. Although these numbers have been dropping steadily since 2010 (IED  
87 casualties have dropped by 48% in 2012 alone), IEDs and EFP devices in  
88 particular are still, and will remain, a significant threat in years to come.  
89 It is thus highly relevant to develop efficient and reliable means of assess-  
90 ing and predicting the behaviour of such devices, in the end leading to the  
91 development of technologies, methods and systems that can better protect  
92 against them. The main aim of the present paper is then to contribute to  
93 this, with a methodology, a finite element modelling approach and formula-  
94 tion, as well as the corresponding formulations, reproducing the conditions  
95 of formation and ballistic capabilities of EFPs.

## 96 **2. Numerical model**

### 97 *2.1. Geometry and boundary conditions*

98 When developing the numerical models, attention was given to the ac-  
99 curate reproduction of the boundary conditions and geometrical configura-  
100 tions. The work of Wu *et al.* [25] was used as reference and for validation

101 purposes. The proposed geometry is that of a generic EFP, as shown in  
102 Figure 1, with a length-to-diameter ratio  $L/D = 1.07$ , liner of diameter  
103  $D = 56$  mm, thickness  $e = 2$  mm, curvature with radius  $R = 120$  mm and  
104 sweeping angle  $\alpha = 29^\circ$ . The casing and the base have thickness  $e' = 5$  mm.  
105 The remaining dimensions will change according to the specific model be-  
106 ing tested. The complexity of the dynamic interactions between the various  
107 components of the EFP (*e.g.* explosive-metal interaction) lead to a de-  
108 tailed and costly modelling process. Interactions between the products of  
109 detonation and the remaining components of the EFP are defined using a  
110 specific contact algorithm that can model surface sliding and is based on a  
111 master-slave segments approach. With this algorithm pressure values are  
112 interpolated and passed to the remaining components of the EFP, leading  
113 to their acceleration and consequent deformation.

114 The symmetry boundary conditions used in the numerical models are  
115 schematically shown in Figure 2. This allows models to run with a signifi-  
116 cantly lower computational cost. Fully three-dimensional models were used  
117 however, where no symmetry is present.

118 The detonation point — its position and detonation time (*e.g.* see Fig-  
119 ure 2) — defines the instant and geometrical coordinates of ignition, dictat-  
120 ing the behaviour of the shock wave and the subsequent deformation and  
121 flight of the projectile.

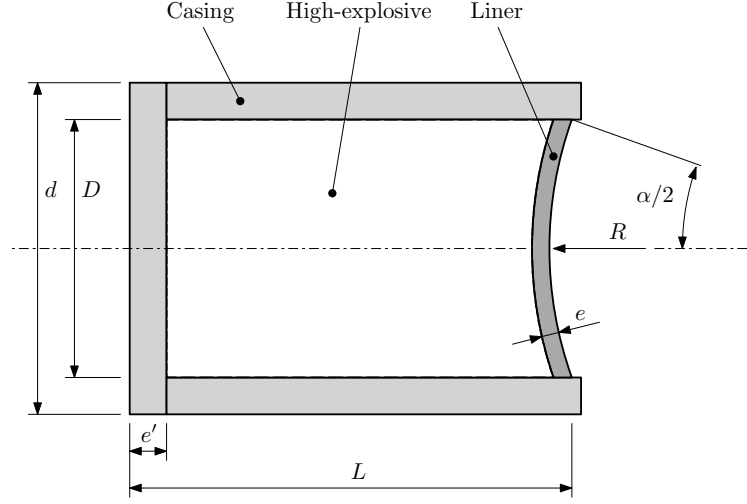


Figure 1: Schematic representation of the generic EFP geometry.

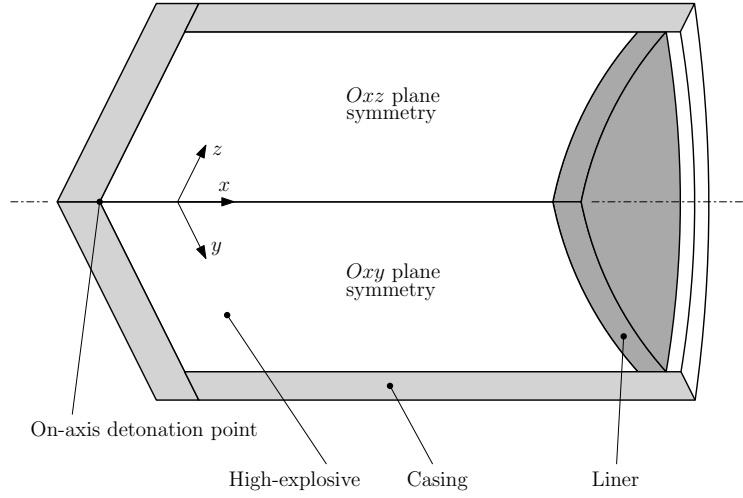


Figure 2: Schematic representation of the generic symmetry boundary conditions.

## 122 2.2. Material modelling

123 Different materials were used to allow for the study of different EFP  
 124 configurations. These include OFHC copper, ARMCO iron and tantalum



125 as liners; Octal, composition B (CompB) and dynamite as high-explosives;  
 126 and steel 1006 and aluminium alloy 6061-T6 for the casing and base of  
 127 the EFP, respectively. The properties of the materials used were validated  
 128 using numerical and experimental results previously published by other au-  
 129 thors, who have studied their behaviour in similar situations and strain rate  
 130 regimes [17, 18, 25].

Materials are subjected to high pressure, temperature and high deforma-  
 tions and strain-rates during the formation of the EFP. Johnson-Cook's  
 constitutive model was thus chosen as the most appropriate model to pre-  
 dict the high strain rate behaviour of the metallic materials [18, 19]. This  
 constitutive model is the most widely referenced for impact and high strain  
 rate behaviour when triaxial stress states depend on both the deformation  
 rate and temperature. Due to the propagation of shock waves and high  
 pressures involved within the metallic materials it is also necessary to de-  
 fine an equation of state (EOS) along with the Johnson-Cook model. The  
 Johnson-Cook effective stress can be defined as a function of the plastic  
 strain, plastic strain-rate and the temperature, as

$$\bar{\sigma} = (A + B\varepsilon^n) [1 + C \ln(\dot{\varepsilon}^*)] [1 - (T^*)^m] \quad (1)$$

131 where  $A$ ,  $B$ ,  $C$ ,  $n$  and  $m$  are the yield stress, the hardening constant,  
 132 the strain-rate constant, the hardening exponent and the thermal softening  
 133 coefficient, respectively. The effective plastic strain is  $\dot{\varepsilon}^* = \dot{\varepsilon}/\dot{\varepsilon}_0$  and the  
 134 non-dimensional temperature is  $T^* = (T - T_0)/(T_m - T_0)$ ,  $T_m$  is the melting

135 temperature,  $T_0$  is room temperature and  $T$  is the current temperature.

The Gruneisen equation of state is used in conjunction with the Johnson-Cook constitutive model. This EOS describes how the materials react to the shock wave and is based on Hugoniot's linear relation between the shock wave velocity,  $v_s$ , and the material particle velocity,  $v_p$ , as  $v_s = c_0 + sv_p$ , where  $c_0$  is the wave speed and  $s$  is a material parameter. For a dense material, the Gruneisen EOS, which relates pressure  $p$  with internal energy  $E$ , is

$$p = \rho_0 c_0^2 \mu \Psi + (\gamma_0 + a\mu) E \quad (2)$$

with

$$\Psi = \frac{2 - a\mu^2 + (2 - \gamma_0)\mu}{2 \left[ 1 - (S_1 - 1)\mu - S_2 \frac{\mu^2}{1+\mu} - S_3 \frac{\mu^3}{(1+\mu)^2} \right]} \quad (3)$$

136 where  $\gamma_0$  is the Gruneisen coefficient,  $a$  is a first order energy correction  
 137 factor and  $S_i$  ( $i = 1, \dots, 3$ ) are material parameters.  $\mu = \rho/\rho_0 - 1$  is an  
 138 non-dimensional coefficient based on the initial and instantaneous material  
 139 densities [30]. All material properties are listed in Table 1.

The behaviour of the high-explosives can be characterised by the Jones-Wilkins-Lee (JWL) equation of state that describes the pressure-volume relationship associated with a detonation process [33, 34, 35], which is based on the Gruneisen EOS, adjusted with experimental data. As with other empirical equations of state, viscosity, conductivity, friction and field forces (*i.e.* gravity) are neglected. The practical nature and large experimental data base supported by this EOS are two major advantages over alternative

Table 1: Material properties for the Johnson-Cook constitutive model and Gruneisen and Jones-Wilkins-Lee equations of state [17, 18, 25, 31, 32].

Property	OFHC Copper	ARMCO Iron	Tantalum	Steel 1006	Aluminum 6061-T6
$\rho$ [kg/m <sup>3</sup> ]	8930	7890	16690	7896	2785
$A$ [GPa]	0.12	1	0.8	0.35	0.265
$B$ [GPa]	0.2	0.38	0.55	0.275	0.426
$C$	0.04	0.06	0.0575	0.022	0.015
$n$	0.15	0.31	0.4	0.36	0.34
$m$	0.55	0.55	0.44	1	1
$T_m$ [K]	1360	1812	3293	1811	775
$T_0$ [K]	293	293	293	293	293
$c_0$ [m/s]	3940	3630	3400	4569	5328
$S_1$	1.49	1.8	1.17	1.49	1.338
$S_2$	0.0	0.0	0.074	0.0	0.0
$S_3$	0.0	0.0	-0.038	0.0	0.0
$\gamma_0$	1.99	1.81	1.6	2.17	2.0
	Dynamite		CompB		Octol
$\rho$ [kg/m <sup>3</sup> ]	1680		1717		1821
$A$ [GPa]	852.4		524.23		748.6
$B$ [GPa]	18.02		7.678		13.38
$R_1$	4.55		4.2		4.5
$R_2$	1.3		1.1		1.2
$\omega$	0.38		0.34		0.38
$E$ [kJ/m <sup>3</sup> ]	8.5		8.5		9.6
$V_0$	1		1		1

EOS. The JWL equation of state can be described by

$$p = A' \left( 1 - \frac{\omega}{R_1 V^*} \right) e^{-R_1 V^*} + B' \left( 1 - \frac{\omega}{R_2 V^*} \right) e^{-R_2 V^*} + \frac{\omega E}{V^*}. \quad (4)$$

140 This expression relates pressure  $p$  with relative volume  $V^* = V/V_0$  and the  
141 energy  $E$ , where  $V_0$  is the initial volume of unreacted explosive and  $V$  is the

142 volume of material under pressure. The energy term accounts both for the  
 143 chemical and the kinetic energies associated with the detonation. Constants  
 144  $A'$ ,  $B'$ ,  $R_1$ ,  $R_2$  and  $\omega$  are the pressure coefficients, the first and second eigen-  
 145 values and the fractional part of the adiabatic exponent, respectively [36].

### 146 2.3. Model validation

147 The work of Wu *et al.* [25] is used as the basis for validation of the  
 148 numerical models proposed in this paper. The approach in the present  
 149 work is purely Lagrangian and does not consider any aerodynamic effects  
 150 on the projectile (*i.e.* drag and lift forces). However, the experimental  
 151 velocities observed by Wu *et al.* were measured after 48 m of flight. It was  
 152 then necessary to account for these differences objectively on the validation  
 153 procedure.

154 The generic dimensions of the model used for validation, as defined in  
 155 Figure 1, are diameter  $d = 60$  mm, liner diameter  $D = 56$  mm and length  
 156  $L = 66$  mm . Wu *et al.* [25] do not provide detailed information about the  
 157 exact thickness of the liner used in their experiments. These authors only  
 158 refer that it is within 1 to 8% of the diameter of the EFP. Consequently, the  
 159 thickness chosen to be used in the validation model is 5% of the diameter,  
 160 that is,  $e = 3$  mm.

The experimentally measured velocity for this device was  $v_x = 1267$  m/s,  
 at a distance  $D_f = 48$  m from the detonation position [25]. Additionally,  
 and still according to Wu *et al.*, the average velocity decrease with distance  
 due to aerodynamic drag is approximately  $\alpha = 6.4$  m/s per meter of flight.

Applying this velocity attenuation factor to the numerical results here presented, the stable flight velocity immediately after the projectile formation stage should be within the range of velocities defined by

$$v_f = v_x(1 \pm \lambda) + \alpha D_f \quad (5)$$

where  $\lambda$  is the maximum accepted error. For the validation procedure, it was assumed that 10% ( $\lambda = 0.1$ ) would be the maximum accepted error for the numerical model to be considered a reasonable approximation of the real physical phenomena being modelled. From the experimental observations it can be determined that  $v_f^{\max} = 1700.9$  m/s and  $v_f^{\min} = 1447.5$  m/s. The results in Figure 3 show the numerical velocity profile for the EFP device (solid line) against the 10% error band obtained from Wu *et al.* and defined by  $v_f^{\max}$  and  $v_f^{\min}$  (grey band).

The numerical stable flight velocity 400  $\mu$ s after detonation is 1489.6 m/s, leading to an estimated average numerical error of 7.66%. Although this error is already considered to be low, it can be further improved by optimising the model discretisation, as will be discussed below.

#### 2.4. Element formulation and discretisation

Several convergence numerical analyses were carried out to verify the influence of the formulations, control parameters and different mesh densities. This was done based on the settings described in Sections 2.1 and 2.2, and using the experimental data provided by Wu *et al.* [25]. Numerical models

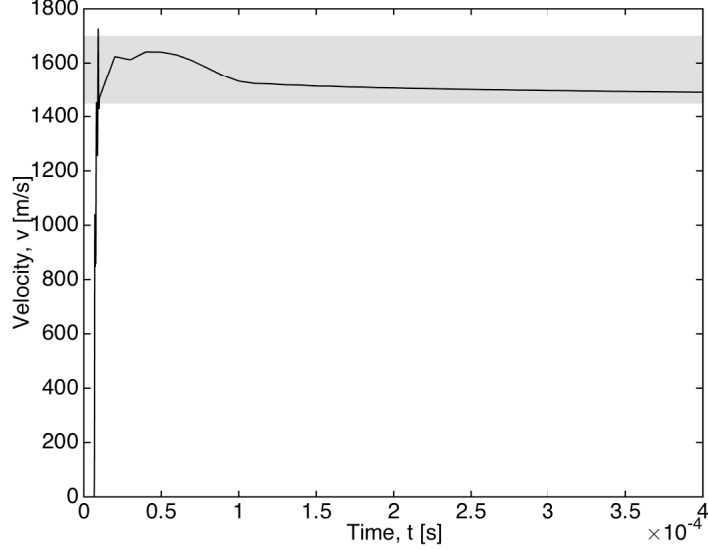


Figure 3: Numerical velocity profile for the EFP device (solid line) against the 10% error band obtained from Wu *et al.* (grey band, range defined by  $v_f^{\max}$  and  $v_f^{\min}$ ).

178 were discretised with 8-node hexahedral solid elements with the following  
 179 formulations: (i) a 1-point Eulerian formulation for the high explosive, lead-  
 180 ing to a discretisation that ensures good contact on the impact between the  
 181 shock wave and the liner/casing; and (ii) a constant stress solid element  
 182 Lagrangian formulation to describe the behaviour of the metallic liner.

183 Mesh refinement and optimisation was achieved based on the deforma-  
 184 tion histories of the liner and the explosive. A good compromise between  
 185 CPU time and accuracy of the numerical results was obtained by comparing  
 186 the stable flight velocities of the EFP with the experimental results of Wu *et*  
 187 *al.* [25], as described in the Model Validation section above (Section 2.3).  
 188 It was observed that further refining the mesh close to the liner-explosive

189 interface led to results with error levels lower than 5.5%, confirming the  
190 good predictive capability of the proposed numerical model.

The correct definition of the time step size is one important aspect on high impulsive dynamic analyses. This step size should be set to a value significantly lower than the time required for a strain wave to cross the minimum distance between two consecutive nodes ( $h_{\min}$ ) at the wave speed in the material. Disregarding this will lead to significant computational errors and hence poor and unrealistic results. In generic terms, the critical (maximum) time step size is  $\Delta t_c = h_{\min}/c$  with  $c = \sqrt{E/\rho}$ , where  $c$  is the wave speed,  $E$  is the elastic modulus and  $\rho$  is the density of the material. An additional 10% time step reduction is applied leading to a final maximum time step size defined by

$$\Delta t = \Delta x \sqrt{\frac{\rho h_{\min}}{100E}} \quad (6)$$

191 in order to minimise the possibility of occurrence of errors in the compu-  
192 tation (*e.g.* negative volumes due to the high strain rates and pressure  
193 levels).

### 194 **3. Results and discussion**

195 The formation of an EFP is a complex dynamic process, mostly the  
196 result of the interaction between the different components of the device.  
197 The developed models were analysed in two separate stages. On the first  
198 stage the detonation of the explosive, propagation of the shock wave and

consequent interaction of the detonation products, accelerate and deform the liner. This stage corresponds to approximately the first 10  $\mu\text{s}$  of the process. In the second stage, which corresponds to approximately 400  $\mu\text{s}$ , the direct effects of the explosive, the casing and the base are neglected, and only the deformation of the projectile and its speed stabilisation are modelled.

In the context of this paper, the ballistic performance of the resulting projectile is assessed by criteria related to its kinetic energy. Ballistic parameters such as geometry, type of detonation (number and position of detonators) and materials, influence the stable flight velocity of the EFP and, consequently, its penetration ability (*i.e.* ballistic performance). Understanding the influence of each EFP design parameter on the shape and energy of the resulting projectile is thus very important and will be analysed in detail in the following sections.

### *3.1. Liner materials and high-explosives*

The properties of the materials that constitute the EFP device are very important both in the context of the dynamic formation of the projectile and on its ballistic performance. The three-dimensional model corresponds to one quarter of the EFP, assuming two-plane symmetry. For the analyses described in this section, only one detonation point was considered, at the centre of the base of the device. All other numerical parameters are as described in Section 2. Two separate analyses were made, namely to study (i) the influence of the liner material (with dynamite as HE) and (ii) the



influence of the high-explosive (with a copper liner).

The results shown in Figures 4(a) and (b) show the evolution of the EFP velocity, during its formation, for different liner materials and different high-explosives, respectively. Figure 5 shows the evolution of the shape of the projectile during the early formation stages.

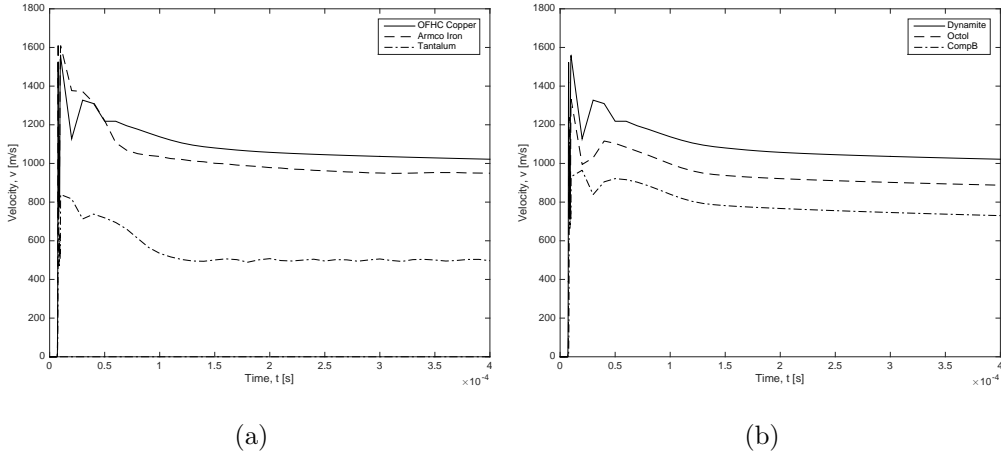


Figure 4: Evolution of the projectile velocity for (a) different liner materials (dynamite HE) and (b) different high-explosives (copper liner).

Observed velocities exhibit a maximum during the initial stages of the formation ( $0 < t < 100 \mu s$ ), which corresponds to the interaction of the detonation wave with the liner. The following stages, for  $100 < t < 400 \mu s$ , encompass most of the deformation of the liner to form the projectile and also the stabilisation of speed. Stable flight speed is reached at approximately  $t = 400 \mu s$ . From the results in Figure 4(a) and Table 2 it can be observed that the copper projectile has a final speed and kinetic energy significantly higher than either iron or tantalum. The properties of copper

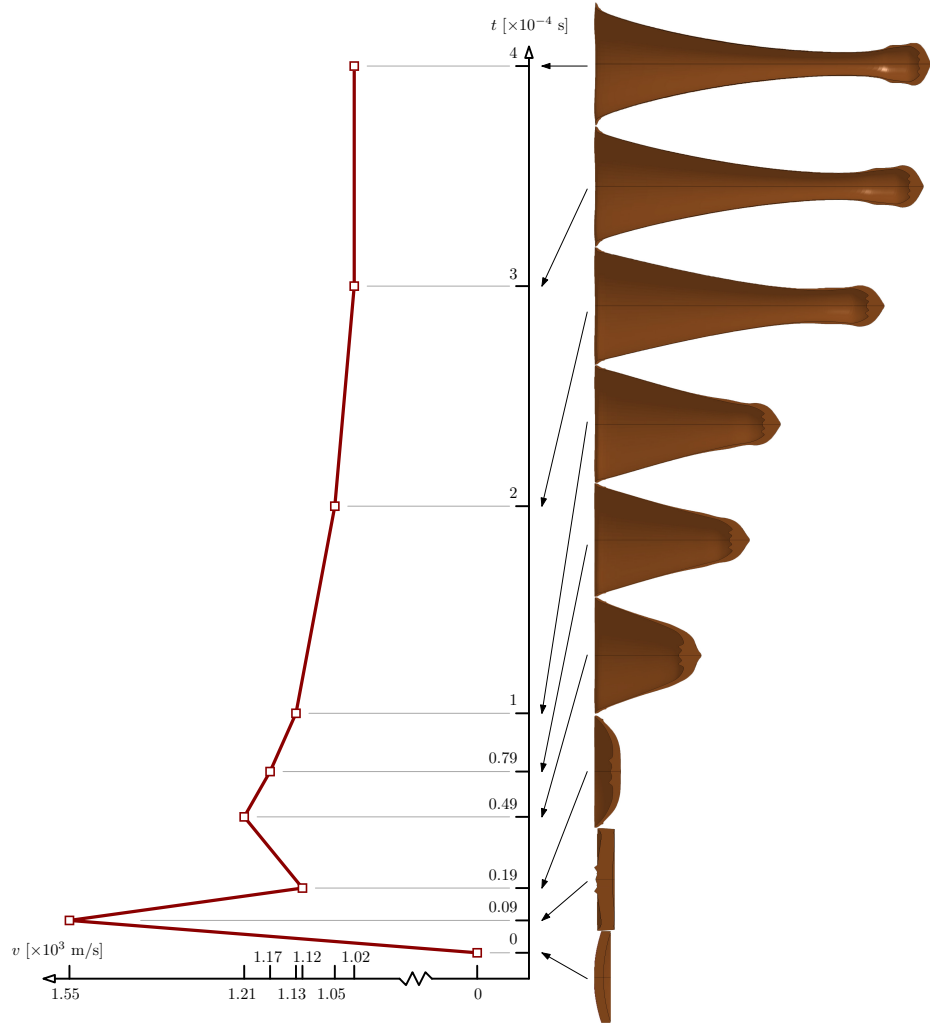


Figure 5: Evolution of the shape of the projectile during the early formation stages (for a 4 mm copper liner and dynamite HE).

(*e.g.* density and ductility) and its behaviour under impact, lead to the conclusion that this material has optimal capacity to form an EFP with high penetration capability (*i.e.* high kinetic energy).

Table 2: Stable flight velocity and resulting kinetic energy for the different material combinations.

<b>EFP device</b>	<b>Projectile mass [g]</b>	<b>Stable flight velocity [m/s]</b>	<b>Kinetic energy [kJ]</b>
Tantalum/Dyanmite	166.7	496.8	20.6
Iron/Dynamite	78.8	949.5	35.5
Copper/Dynamite	89.2	1021.8	46.6
Copper/Octol	89.2	887.5	35.1
Copper/CompB	89.2	730.1	23.8

Analysing the results in Figure 4(b) and Table 2, it is found that, among all high-explosives tested, dynamite has the most evident effect on the final configuration of the projectile. The speed of the explosion products and the energetic capability of the HE are responsible for this. In terms of final kinetic energy, copper and dynamite seem to be the most efficient combination.

Copper projectiles also have a lower drag when compared to the iron or tantalum projectiles. Although not an area of study in this work, EFP aerodynamics are known to benefit from this type of geometry, as well as from the formation of fins [16].

### 3.2. Liner configuration

The relation between the shape of the liner and the final geometry and configuration of the EFP is complex and not yet fully understood [3, 14, 16].

251 In this section, the authors present a model that attempts to correlate the  
 252 final velocity of the projectile to the initial liner geometry (*e.g.* thickness  
 253 and thickness distribution). Two different liner models were used for this  
 254 purpose: (i) constant thickness, five models with thicknesses ranging from  
 255 1 to 20% of the liner diameter; and (ii) variable thickness, considering two  
 256 different approaches: with maximum thickness at the centre or at the edge  
 257 of the liner. Model details are listed in Table 3.

258 Copper and dynamite were used for the liner and HE, respectively. All  
 259 tests were done with a single detonation point, at the centre of the base of  
 260 the EFP device (see Section 2).

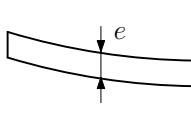
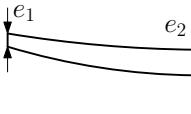
Results in Figures 6(a) and (b) show the EFP velocity during the for-  
 mation stages of the projectile for the described initial liner configurations.  
 The observed behaviour exhibits oscillations in the velocity during the ini-  
 tial 100  $\mu\text{s}$ , corresponding to the formation of the projectile, followed by  
 stabilisation at about  $t = 200 \mu\text{s}$ . Generically, it can also be observed that  
 the final velocity increases with the decrease of the liner thickness. This  
 increase is non-linear and can be approximated by the following power law:

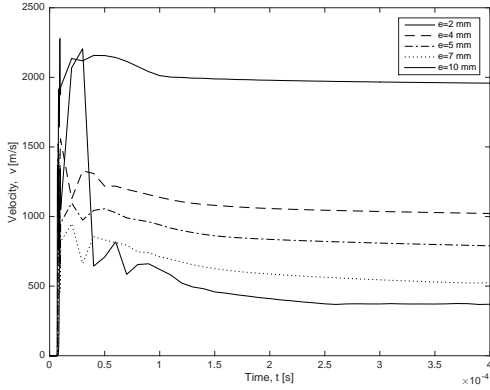
$$v_e = k_1 e^{-\alpha} \quad (7)$$

261 where  $k_1 = 4172$  and  $\alpha = 1.048$  are constants specific for the EFP config-  
 262 uration and set of materials used.  $e$  is the thickness of the liner and  $v$  the  
 263 final (stable flight) velocity of the EFP.

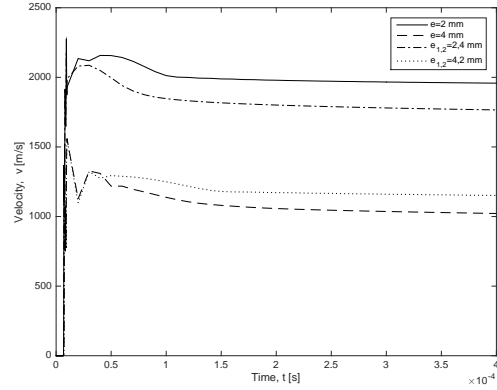
264 As a consequence of its curved shape, the centre of the liner receives the

Table 3: Stable flight velocity and resulting kinetic energy for the different liner thicknesses.

	Thickness	Liner mass [g]	Stable flight velocity [m/s]	Kinetic energy [kJ]
	$e = 2$ mm	44.6	1958.1	85.5
	$e = 4$ mm	89.2	1021.8	46.6
	$e = 5$ mm	111.5	789.8	34.8
	$e = 7$ mm	156.1	524.9	21.5
	$e = 10$ mm	223.1	369.9	15.3
	$e_1 = 2$ mm	66.1	1151.3	43.8
	$e_2 = 4$ mm			
	$e_1 = 4$ mm	65.5	1766.0	102.1
	$e_2 = 2$ mm			



(a)



(b)

Figure 6: (a) Velocity profiles for liners with constant thickness and (b) comparison with variable thickness liners.

265 impact of the detonation wave before its periphery. The energy transferred  
 266 to the liner accelerates and deforms it to form the projectile. When com-  
 267 paring variable and constant thickness models (with similar mass), there

seems to be a correlation between the thickness at the centre of the liner and the final EFP velocity. It was observed that the thickness at the centre of the liner is one of the most important parameters defining its final shape. Additionally, liners with a smaller centre thickness lead to higher speeds for similar masses, as can be seen from the results shown in Table 3. From the results shown in Figure 6(b) it can be observed that it is possible to change the stable flight kinetic energy just by changing the thickness (and consequently volume of material) at the periphery of the liner. Generically, from the observed results, higher stable flight velocities are obtained for liners with thicknesses between 4 and 7% of the diameter.

### 3.3. Layout of detonators

The number and position of the detonation points understandably has a strong influence on the whole process of releasing energy and, consequently, on the formation of the EFP, and will thus be assessed in this section. Five different sets of tests are done, with the parameters listed in Table 4 and shown in Figure 7. A complete three-dimensional FEA approach was used for the models with no symmetries. Dynamite and copper were used as HE and liner material, respectively. The liner thickness is  $e = 4$  mm and the control parameters described in Section 2 were used. A synchronous detonation was assumed for all multi-detonator tests.

This study allows for a better understanding of the development of shock waves and how these influence the formation of the projectile. The EFP velocity for the various detonation parameters is shown in Figures 8(a) to (c).

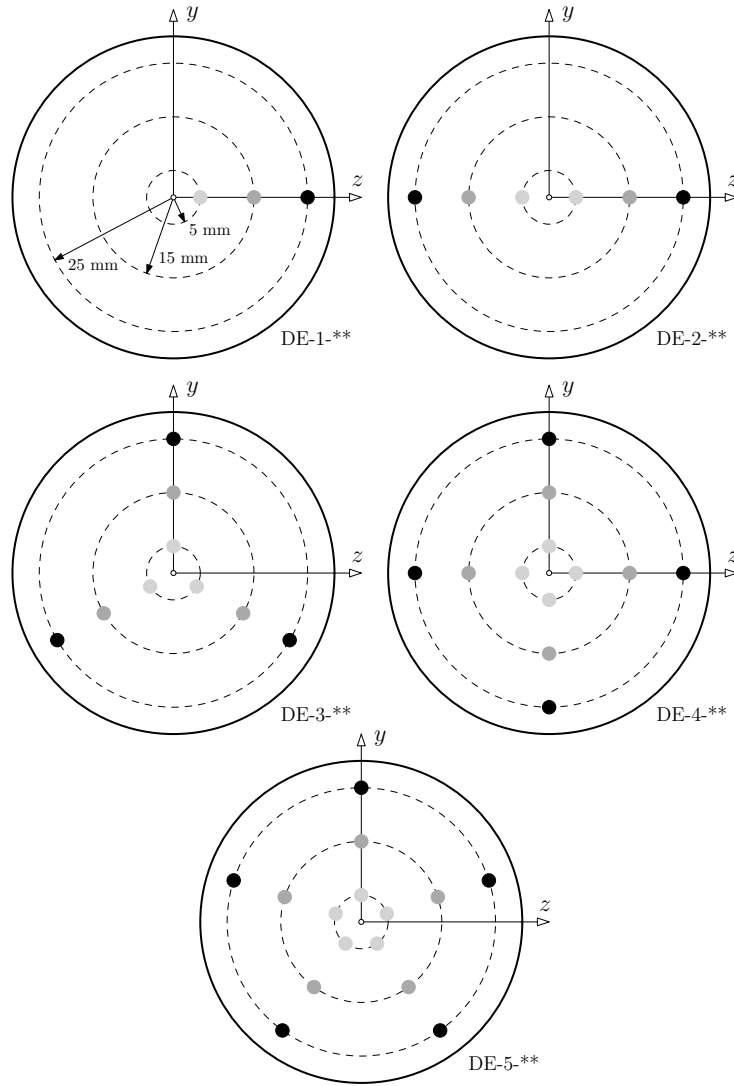


Figure 7: Number, relative position of detonators and test nomenclature (see also Table 4).

Table 4: Number and position of detonators.

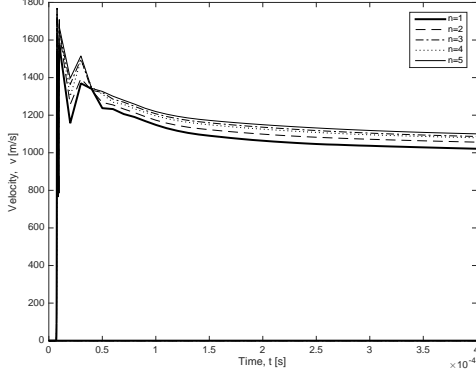
Model designation	Number of detonators	Off-centre distance [mm]	Angular spacing [°]
DE-1-05	1	5	—
DE-1-15		15	
DE-1-25		25	
DE-2-05	2	5	180
DE-2-15		15	
DE-2-25		25	
DE-3-05	3	5	120
DE-3-15		15	
DE-3-25		25	
DE-4-05	4	5	90
DE-4-15		15	
DE-4-25		25	
DE-5-05	5	5	72
DE-5-15		15	
DE-5-25		25	

It can be seen from these results that the stable velocity of the EFP increases with the number of detonators. A similar effect can be observed for increasing detonator off-centre distances.

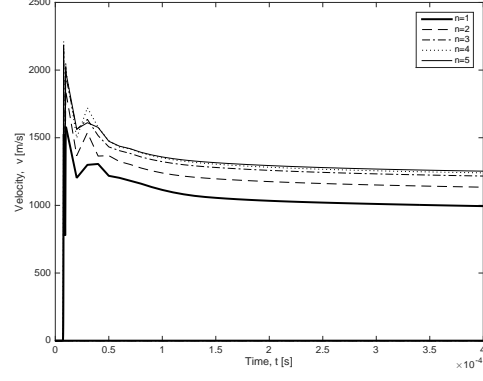
From the results in Figure 8(a), corresponding to a detonator off-centre distance of 5 mm, it can be observed that three detonation points lead to a higher stable flight velocity, as compared to the four detonation points device. From Figures 8(b) and (c), which corresponds to a detonator off-centre distance of 15 mm and 25 mm, respectively, this effect is no longer visible.

The lateral velocity of the EFP for different positions of a single detona-

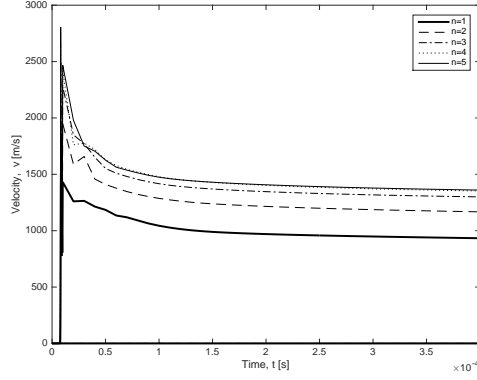




(a)



(b)



(c)

Figure 8: EFP velocity profiles with multiple detonators at off-centre distances of (a) 5 mm, (b) 15 mm and (c) 25 mm.

tor (see Figure 9) increases, as expected, with the off-centre distance. For off-centre distances larger than 15 mm the EFP becomes more unstable in flight due to the fluctuations in the lateral speed, as increasing the lateral velocity leads to a decrease on the relative axial velocity, leading to a reduction of the kinetic energy that contributes to impact and, consequently, the accuracy of the projectile. Increasing the number of detonators and

307 their off-centre distance, the EFP develops more prominent fins in the final  
 308 formation stages, leading to better in-flight stability and improved accu-  
 309 racy [16].

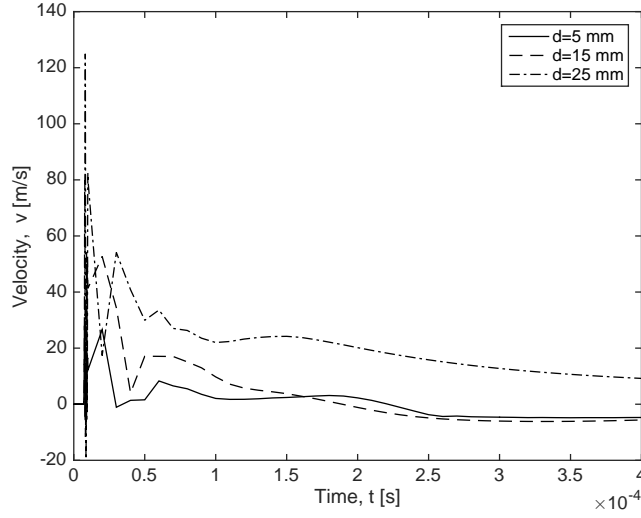


Figure 9: Lateral velocity of the EFP with one detonation point at different off-centre distances.

The power law

$$v_d = k_2(d)n^{\gamma(d)} \quad (8)$$

describes the stable flight velocity of the EFP as a function of the number of detonators  $n$  and their off-centre distance  $d$  (see Figure 10).  $k_2(d)$  and  $\gamma(d)$  are linear functions of the off-centre distance of the detonators given by

$$k_2(d) = 1045 - 3.21d \quad (9)$$

and

$$\gamma(d) = \frac{9.9d - 1.43}{1000} \quad (10)$$

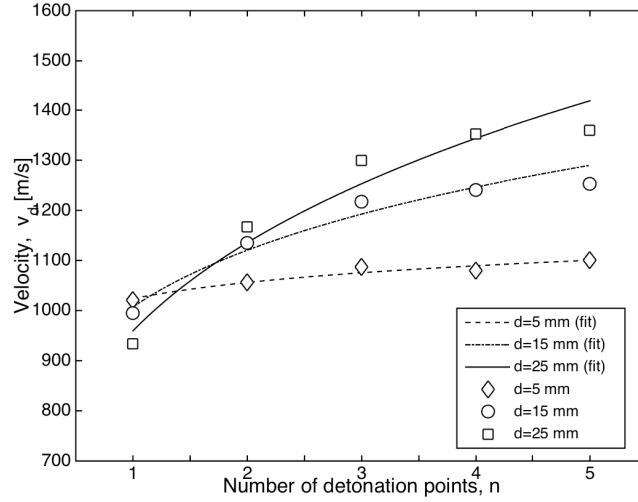


Figure 10: Stable flight velocity as a function of the number of detonators (see Equation 8).

Equations 7 and 8 can be combined to account for the influence of the thickness of the liner, yielding

$$v = v_e + (v_d - v_r) \quad (11)$$

where  $v_r$  is a constant that accounts for the contribution of multiple detonation points. The term  $(v_d - v_r)$ , that represents the contribution of the type of detonation, is zero for a single central detonation point with  $d = 0$ , is negative for a single off-centre detonation point, and positive for multiple detonation points. Combining all previous relations, the total EFP stable

flight velocity is

$$v = k_1 e^{-\alpha} + k_2(d)n^{\gamma(d)} - v_r \quad (12)$$

where  $v_r = 1024.2$  m/s for the specific device analysed in this work. An overall perspective of the relation between the projectile stable flight velocity and the configuration of the detonators (*i.e.* number and off-centre distance) is shown in Figure 11. EFP devices with different configurations (geometry, materials, HE, *etc.*) will naturally yield different curve fits and constants.

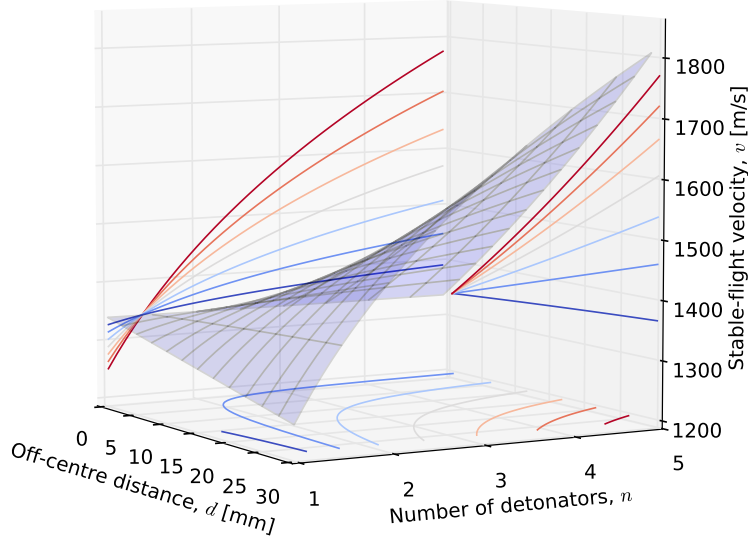


Figure 11: Stable flight velocity as a function of the number and off-centre distance of the detonators for a 3 mm constant thickness liner (see Equation 12).

### 3.4. EFP configuration and geometry

The configuration and dimensions of the projectile influence its behaviour both during flight and on impact. Mass should ideally be con-

centrated at the leading edge of the projectile in order to maximise focusing impact energy and thus facilitating penetration of the target. This can be better discussed by analysing the following dimensionless geometrical parameters:

$$e^* = \frac{P}{e} \quad \text{and} \quad \beta = \frac{L}{D} \quad (13)$$

where  $P$ ,  $L$  and  $D$  are the dimensions shown in Figure 12, and  $e$  is the thickness of the liner. Detailed results obtained for different combinations of liner material, liner thickness, and high-explosive are listed in Table 5.

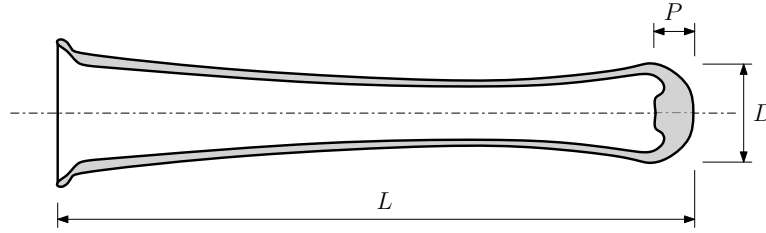


Figure 12: Transverse section of an EFP with the geometric variables used for the non-dimensional analysis.

From the analysis of different liner materials, copper is the only material where  $e^* > 1$ , meaning that the thickness at the point of impact will be higher than the initial thickness of the liner. Additionally, copper liner EFPs have a higher aspect ratio  $\beta$ , an indication of a higher relative length  $L$  and decrease in calibre  $D$ .

The results obtained for constant thickness liners show a slight increase on  $e^*$  with increasing liner thickness, as opposed to  $\beta$ , which decreases significantly, as can be seen in Figure 13.

The final geometry (*e.g.* length) of the 2 mm liner device is clearly unre-

Table 5: Geometrical parameters defining the configuration of the EFP for all analyses performed.

<b>Models</b>	$L$ [mm]	$D$ [mm]	$P$ [mm]	$e^*$	$\beta$
Iron/Dynamite	69.7	35.2	3.6	0.89	1.98
Tantalum/Dynamite	33.3	34.9	3.6	0.91	0.96
Copper/Dynamite	233.4	25.8	8.8	2.21	9.03
Copper/Octol	187.4	28.1	6.6	1.65	6.66
Copper/CompB	127.8	31.2	5.2	1.31	4.10
$e = 2$ mm	555.8	20.1	4.1	2.03	27.62
$e = 4$ mm	233.4	25.8	8.8	2.21	9.03
$e = 5$ mm	165.8	27.9	14.2	2.84	5.95
$e = 7$ mm	90.9	29.3	19.3	2.74	3.10
$e = 10$ mm	71.8	49.1	39.7	3.97	1.46
$e_{1,2} = 2, 4$ mm	216.2	33.6	9.7	2.43	6.43
$e_{1,2} = 4, 2$ mm	534.6	14.9	4.0	1.98	35.98
DE-1-05	239.3	25.0	9.2	2.30	9.57
DE-1-15	236.3	24.9	9.4	2.35	9.49
DE-1-25	220.1	24.3	9.0	2.25	9.05
DE-2-05	253.1	24.0	9.5	2.37	10.56
DE-2-15	291.2	19.8	11.2	2.80	14.68
DE-2-25	315.9	17.4	12.2	3.06	18.21
DE-3-05	264.6	24.2	10.3	2.57	10.96
DE-3-15	321.9	20.3	11.9	2.98	15.89
DE-3-25	367.1	16.8	13.9	3.48	21.89
DE-4-05	262.4	24.1	10.2	2.56	10.90
DE-4-15	333.2	18.5	14.2	3.55	18.04
DE-4-25	392.0	14.1	16.2	4.05	27.83
DE-5-05	269.4	24.0	10.6	2.64	11.22
DE-5-15	341.9	19.3	13.2	3.29	17.68
DE-5-25	390.3	16.5	13.6	3.40	23.69

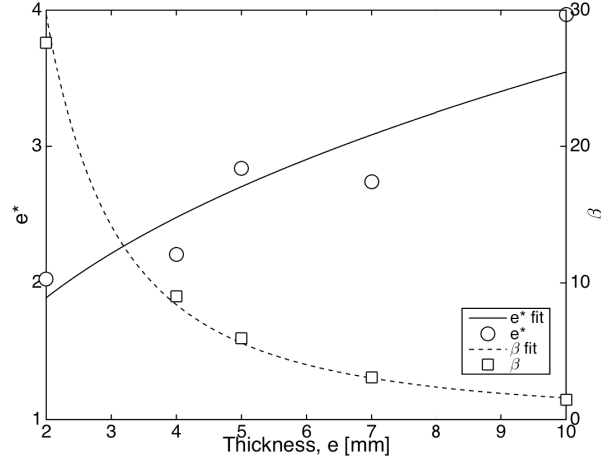


Figure 13: Dependence of  $e^*$  and  $\beta$  on the thickness of the liner (for constant thickness liners).

328 alistic. This is most probably due to the fact that the proposed model does  
 329 not account for fracture/damage. By comparing the geometrical parame-  
 330 ters to the final kinetic energy of the EFP it is possible to establish that a  
 331 reasonable range for  $\beta$  would be  $9 < \beta < 27$ , corresponding to the 4 and  
 332 2 mm of constant thickness models, respectively. For the liners with vari-  
 333 able thickness however, an exception to this interval should be made only  
 334 when the kinetic energy is higher than that of the model that established  
 335 the limit. By limiting  $\beta$  and maximising  $e^*$  it is possible to estimate the  
 336 penetration capacity of the resultant EFP. From the results in Table 5 and  
 337 Figure 14 it can be observed that both  $e^*$  and  $\beta$  gradually increase with the  
 338 detonator off-centre distance, the only exception being the model with one  
 339 detonation point. The model with 4 detonation points at a radial distance  
 340 of 25 mm is the one with the highest values of both  $e^*$  and  $\beta$ . The values

341 of  $\beta$  however, are outside the optimal interval due to the smaller calibre  
 342 of the projectile. Therefore, the model with 5 detonation points at 25 mm  
 343 off-centre distance has better results within the accepted values.

344 As previously stated, the detonation parameters of an EFP strongly  
 345 influence the final configuration of the projectile. To illustrate this, the  
 346 view along the axis of each EFP model is shown in Figure 15, where the  
 347 effects of the detonation parameters become evident.

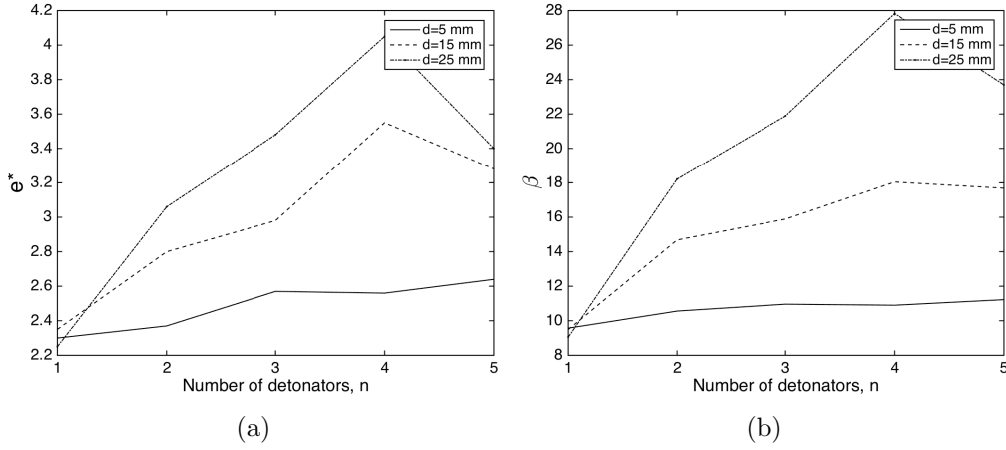


Figure 14: Relation between (a)  $e^*$  and (b)  $\beta$ , and the number and position of detonators, for constant thickness liners.

#### 348 4. Conclusions

349 In the present paper the authors propose and describe a finite element  
 350 based numerical model of a medium calibre explosively formed projectile  
 351 (EFP) device. This model is based on a generic EFP with an aspect ratio  
 352 of 1.07 and is initially validated against experimental observations. This



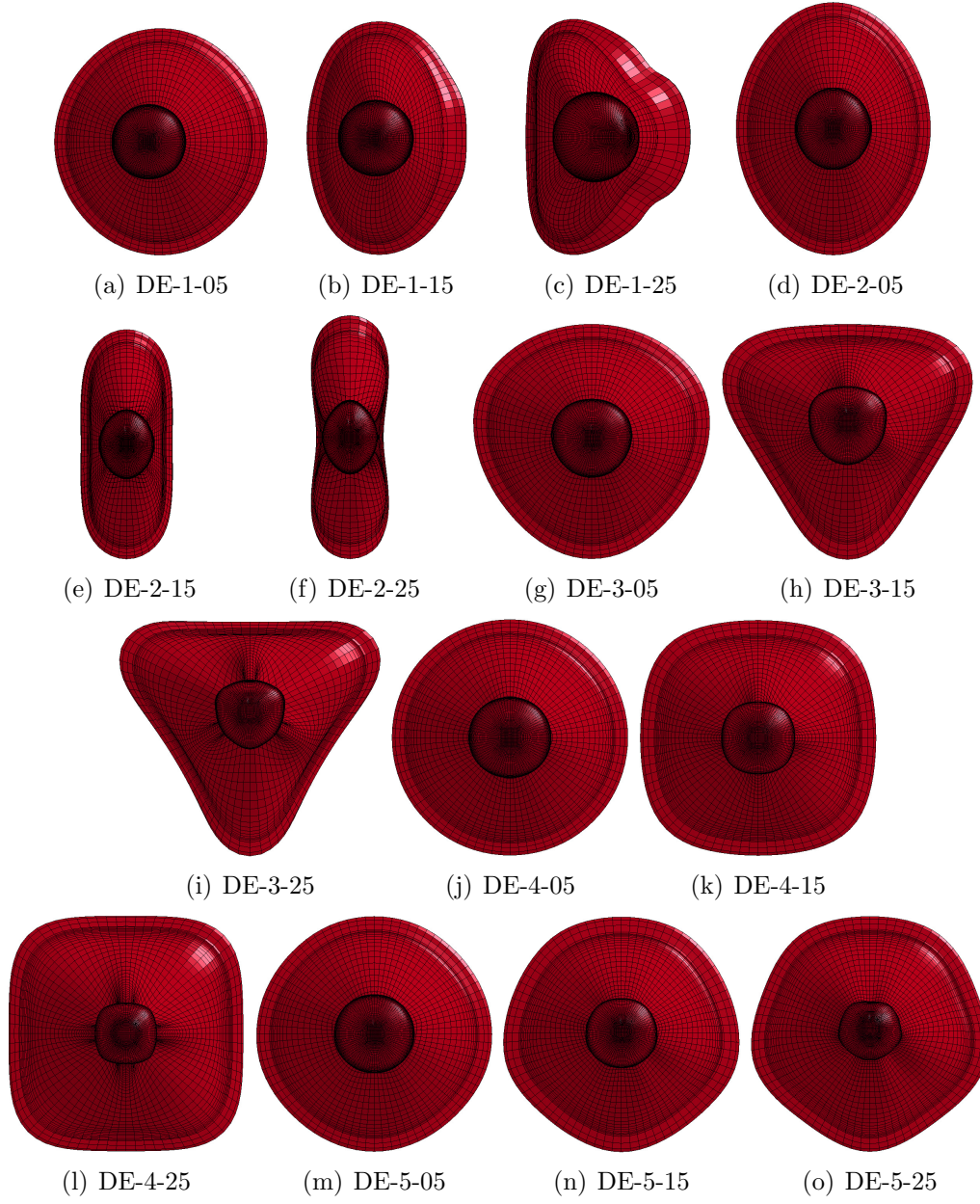


Figure 15: View along the axis of the projectiles with 1 to 5 detonation points at 5, 15 and 25 mm off-centre distance (see Table 4 for test nomenclature).

approach is then used to assess the influence of the liner materials and thickness, geometrical imperfections (*i.e.* variability in liner thickness), high-explosive, and number and off-centre distance of detonators on the performance of the projectile. This performance is quantified by analysing the formation stage of the projectile, the stable flight velocity profiles and the projectile configuration (based on a set of non-dimensional geometrical parameters).

In generically terms and from the results obtained it is shown that the thickness (and thickness variability) of the liner is one of the most important factors, along with the off-centre distance of the detonator(s), influencing the stable flight velocity of the EFP. It is also observed that, within the materials and range of parameters tested, the most performant (and aggressive) EFP has a liner with thickness between 4 and 7% of its diameter, a copper liner and dynamite high-explosive (HE). For variable thickness liners however, results show that there is a relationship between the centre thickness of the liner and the final velocity achieved, proving more advantageous to have a smaller thickness closer to the centre of the liner, resulting in higher velocities for such a mass and thus higher kinetic energy.

In evaluating geometric parameters of the EFP, more specifically the study of the effect of varying the liner thickness in the projectile, the results obtained from the performed simulations show that with increasing mass of the projectile and with the same  $L/D$  ratio of the explosive, the final speed of the projectile decreases.

376 In the evaluation of the effects of detonation parameters, namely the  
377 number and the distance to the centre of the explosive, there were significant  
378 improvements in the results obtained from simulations as the number of  
379 detonators increased. The same happened when their off-centre distance  
380 increased, the exception being the single point detonation. An increasing  
381 tendency for the development of fins was also observed for increasing number  
382 of detonators and off-centre distance. In terms of kinetic energy, the EFP  
383 with five detonation points with 25 mm of radial distance proved most  
384 advantageous presenting the maximum final velocity for the same projectile  
385 mass.

386 The numerical models developed are able to correctly predict the com-  
387 plex behaviour of an EFP and evaluate the influence of different materi-  
388 als/configurations used. An analytical model is also proposed, which can  
389 be used to predict the stable flight velocity of the EFP based on the mate-  
390 rials, configuration and detonation parameters. This analytical model has  
391 however, some limitations, the most important being the consideration of a  
392 perfectly synchronous detonation when multiple detonators are present.

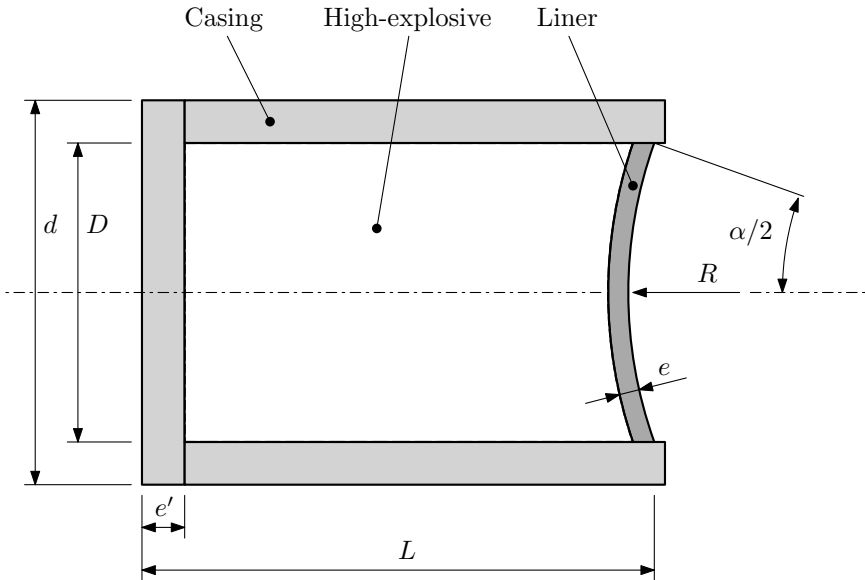
## 393 References

- 394 [1] W. Payman, D.W. Woodhead, H. Titman. Explosion waves and shock waves, Part  
395 II – The shock waves and explosion products sent out by blasting detonators. *Pro-*  
396 *ceedings of Royal Society of London* **148**:604-622, 1935.
- 397 [2] R.W. Wood. Optical and physical effects of high explosives. *Proceedings of The*  
398 *Royal Society of London* **157A**:249-261, 1936.

- 399 [3] G.R. Johnson. Dynamic analysis of explosive-metal interaction in three dimensions.  
400 *Journal of Applied Mechanics* **48**(1):30-35, 1981.
- 401 [4] G.R. Johnson, R.A. Stryk. Some considerations for 3D EFP computations. *Inter-*  
402 *national Journal of Impact Engineering* **32**:1621-1634, 2006.
- 403 [5] J.A. Zukas, D.R. Scheffler. Practical aspects of numerical simulations of dynamic  
404 events: effects of meshing. *International Journal of Impact Engineering* **24**:925-945,  
405 2000.
- 406 [6] E.A. Taylor. Simulation of hollow shaped charge jet impacts onto aluminium whipple  
407 bumpers at 11 km/s. *International Journal of Impact Engineering* **26**:773-784, 2001.
- 408 [7] U. Nyström, K. Gylltoft. Numerical studies of the combined effects of blast and  
409 fragment loading. *International Journal of Impact Engineering* **36**:995-1005, 2009.
- 410 [8] J.F. Molinari. Finite element simulation of shaped charges. *Finite Elements in Anal-*  
411 *ysis and Design* **38**:921-936, 2002.
- 412 [9] S. Miller. A new design criteria for explosively-formed hypervelocity projectile  
413 (EFHP). *International Journal of Impact Engineering* **10**:403-411, 1990.
- 414 [10] R.E. Brown, M.E. Majerus, J. S. Lewis. Building characteristics into a shaped charge  
415 to achieve unique performance requirements. *International Journal of Impact Engi-*  
416 *neering* **17**:121-130, 1995.
- 417 [11] C.A. Weickert, P.J. Gallagher. Penetration of explosively formed projectiles. *Inter-*  
418 *national Journal of Impact Engineering* **14**:809-818, 1993.
- 419 [12] Y. Chuan, T. Yanjin, Y. Chengli, L. Fabo, G. Yulin, Z. Ming, W. Bingren, X.  
420 Panhai, L. Liangzong. Applied research of shaped charge technology. *International*  
421 *Journal of Impact Engineering* **23**:981-988, 1990.
- 422 [13] D. Bender, J. Carleone. *Tactical Missile Warheads*, in: Progress in Astronautics and  
423 Aeronautics, American Institute of Aeronautics and Astronautics, Vol. 155, 1993.
- 424 [14] K. Weimann, K. Doenngsfeld. *Modeling, testing, and analysis of EFP performance*  
425 *as a function of confinement*. in: Proceedings of the 12<sup>th</sup> International Symposium  
426 on Ballistics, 228-237, 1990.

- 427 [15] C.A. Weickert, P.J. Gallagher *Ogive-nosed, finned, explosively-formed projectiles*,  
428 in: Proceedings of the 16<sup>th</sup> International Symposium on Ballistics, 613-614, 1996.
- 429 [16] D. Bender, J. Carleone. *Method and apparatus for providing a explosively formed*  
430 *penetrator having fins*. United States Patent, num. 5365852, Nov. 22, 1994.
- 431 [17] S. Pappu, L.E. Murr. Hydrocode and microstructural analysis of explosively formed  
432 penetrators. *Journal of Materials Science* **37**:233-248, 2002.
- 433 [18] G.R. Johnson, W. Cook. *A constitutive model and data for metal subjected to large*  
434 *strains, high strain rates and high temperatures*. in: Proceedings of the 7<sup>th</sup> Interna-  
435 tional Symposium on Ballistics, 541-547, 1983.
- 436 [19] G. Johnson, W. Cook. Fracture characteristics of three metals subjected to various  
437 strains, strain rates, temperatures and pressures. *Engineering Fracture mechanics*  
438 **21**(1):31-48, 1985.
- 439 [20] F. Zerilli, R. Armstrong. Dislocation mechanics based constitutive relations for ma-  
440 terial dynamics calculations. *Journal of Applied Physics* **61**:1816-1825, 1987.
- 441 [21] J.R. Assay, G.I. Kerley. The response of materials to dynamic loading. *International*  
442 *Journal of Impact Engineering* **5**:69-99, 1987.
- 443 [22] S.M. Cardonne, P. Kumar, C.A. Michaluk, H.D. Schwartz. Tantalum and its alloys.  
444 *International Journal of Refractory Metals and Hard Materials* **13**:187-194, 1995.
- 445 [23] M. Katayama, S. Kibe, T. Yamamoto. Numerical and experimental study on the  
446 shaped charge for space debris assessment. *Acta Astronautica* **48**:363-372, 2001.
- 447 [24] L.E. Murr, M.A. Meyers, C.S. Niou, Y.J. Chen, S. Pappu, C. Kennedy. Shock-  
448 induced deformation twinning in tantalum. *Acta Materialia* **45**:157-175, 1997.
- 449 [25] J. Wu, J. Liu, Y. Du. Experimental and numerical study on the flight and pene-  
450 tration properties of explosively-formed projectile. *International Journal of Impact*  
451 *Engineering* **34**:1147-1162, 2007.
- 452 [26] W. Li, X. Wang, W. Li. The effect of annular multi-point initiation on the forma-  
453 tion and penetration of an explosively formed penetrator. *International Journal of*  
454 *Impact Engineering* **37**:414-424, 2010.

- 455 [27] A.H. Cordesman, M. Allison, J. Lemieux. *IED Metrics for Afghanistan January*  
456 *2004 — September 2010*. Center for Strategic & International Studies, November  
457 11, 2010.
- 458 [28] C. Whitlock. *Number of U.S. casualties from roadside bombs in Afghanistan sky-*  
459 *rocketed from 2009 to 2010*. The Washington Post, January 25, 2011.
- 460 [29] M. Jean-Louis, W. Fetterhoff, M. Hadar. *Faces of the fallen*. The Washington Post.  
461 Retrieved from <http://apps.washingtonpost.com/national/fallen/>, April, 2015.
- 462 [30] G.A. Christou, L.R. Young, R. Goel, A.P. Vechart, A. Jerusalem. Shock attenuation  
463 of PMMA sandwich panels filled with soda-lime glass beads: A fluid-structure inter-  
464 action continuum model simulation. *International Journal of Impact Engineering*,  
465 **47**:48-59, 2012.
- 466 [31] K. Vahedi, N. Khazraian. *Numerical modeling of ballistic penetration of long*  
467 *rods into ceramic/metal armors*, in: 8<sup>th</sup> International LS-Dyna Users Conference:  
468 Drop/Impact simulations **14**:39-50, 2004.
- 469 [32] C.E. Zhou, G.R. Liu, K.Y. Lou. Three-dimensional penetration simulation using  
470 smoothed particle hydrodynamics. *International Journal of Computational Methods*  
471 **4**:671-691, 2007.
- 472 [33] J. Hallquist. *LS-Dyna Theory Manual*. Livermore Software Technology Corporation,  
473 March 2006.
- 474 [34] M.L. Wilkins. Calculations of Elastic Plastic Flow. *Methods in Computational*  
475 *Physics* **3**:211-263, 1964.
- 476 [35] E.D. Giroux. *HEMP User's Manual*. Lawrence Livermore National Laboratory, Uni-  
477 versity of California, Rept. UCRL-51079, 1973.
- 478 [36] P.A. Urtiew, B. Hayeo. Parametric study of the dynamic JWL-EOS for detonation  
479 products. *Fizika Goreniya i Vzryva*, **27**(4):126-137, 1991.



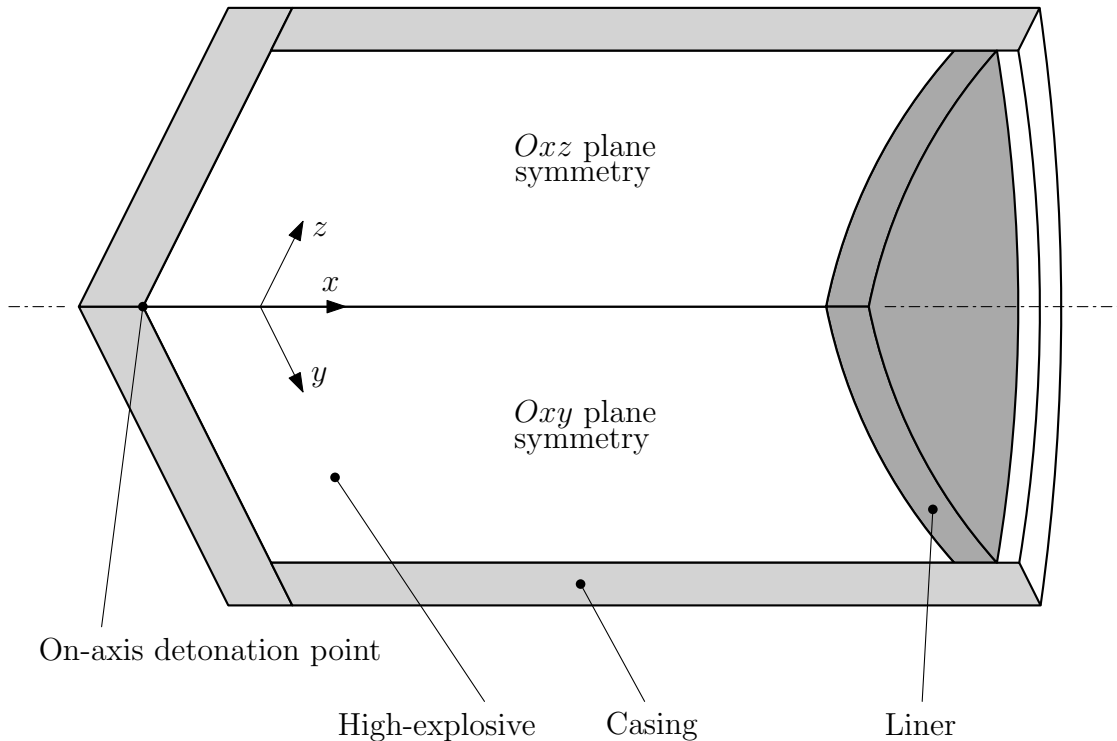




Figure 3

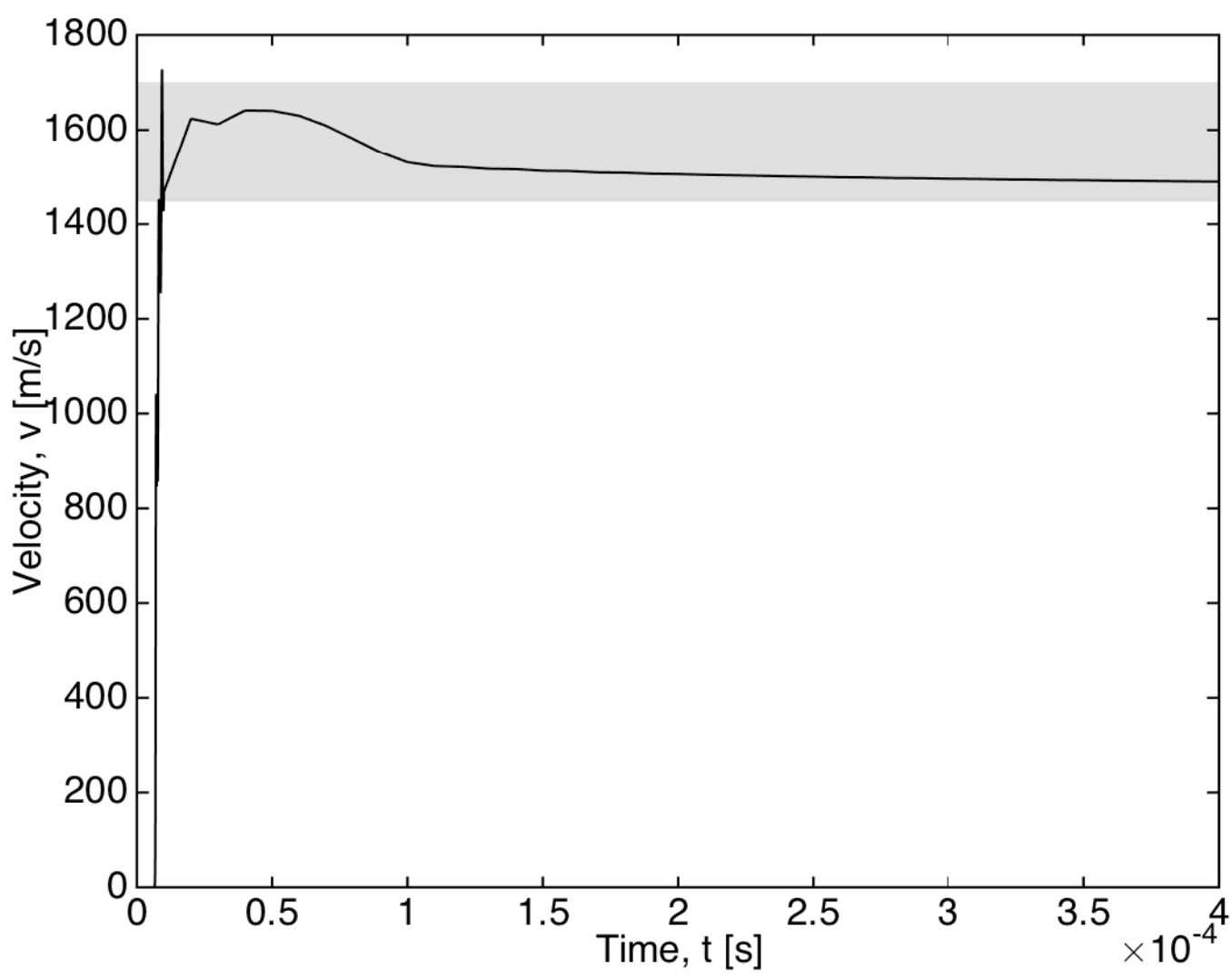


Figure 4a

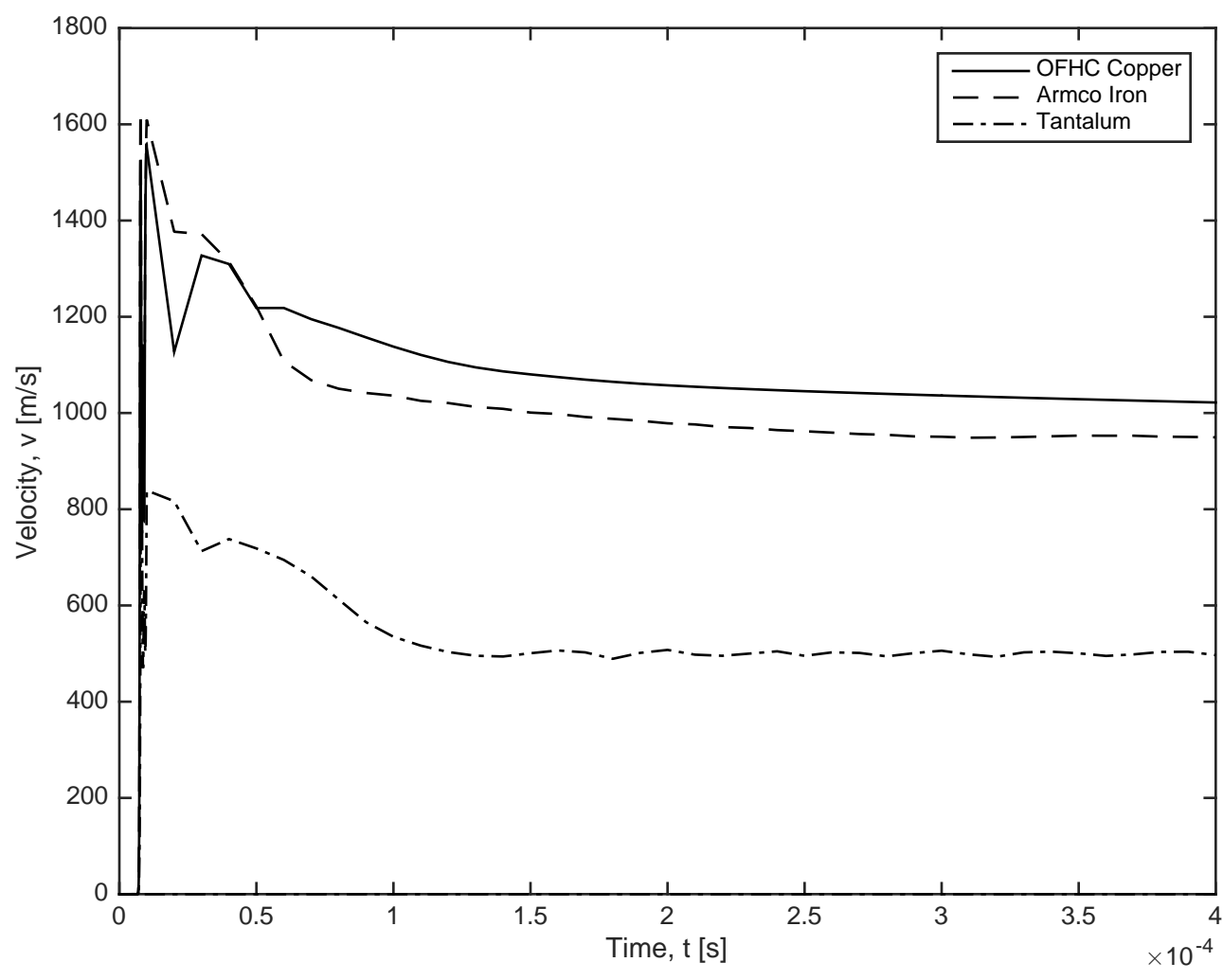
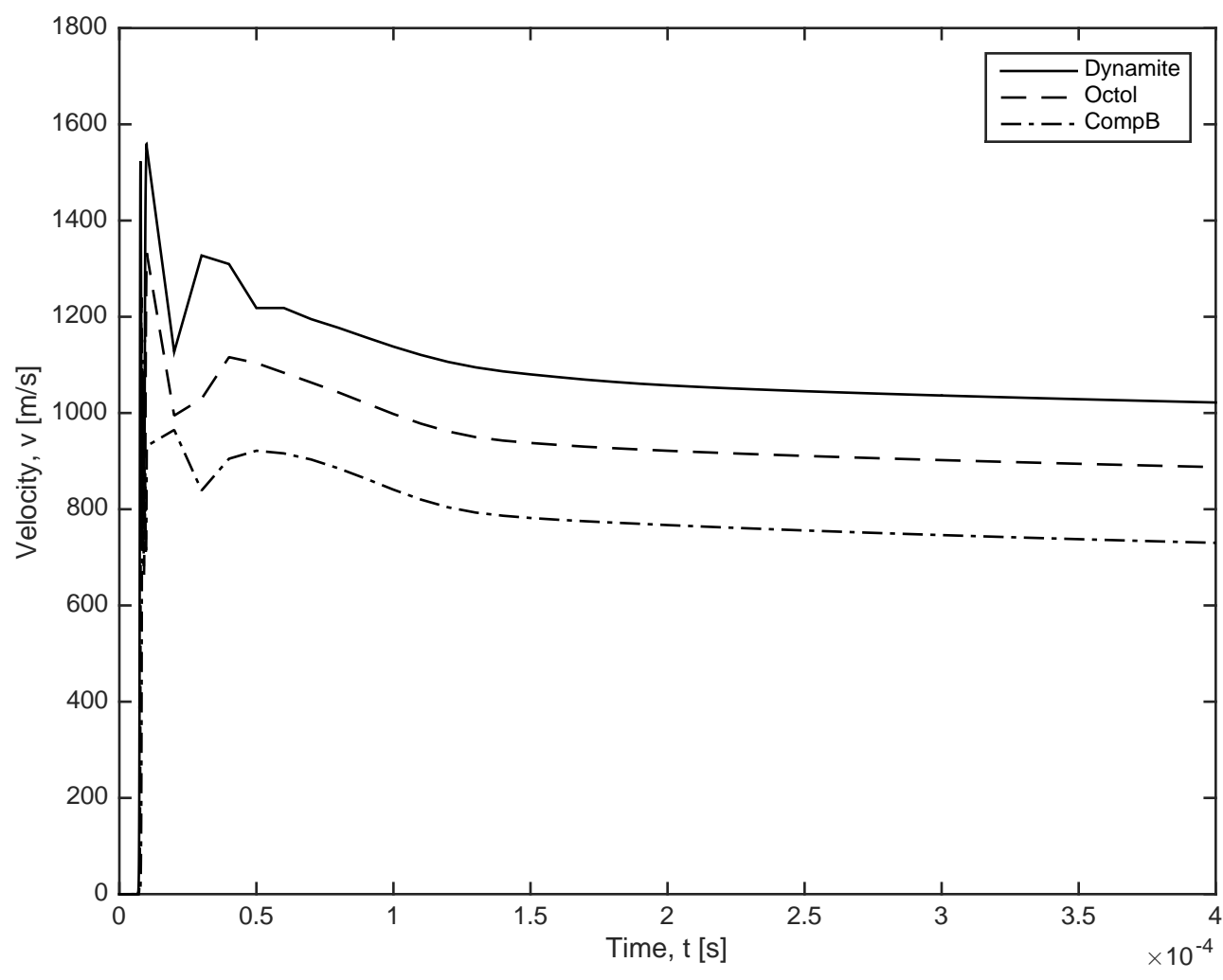


Figure 4b



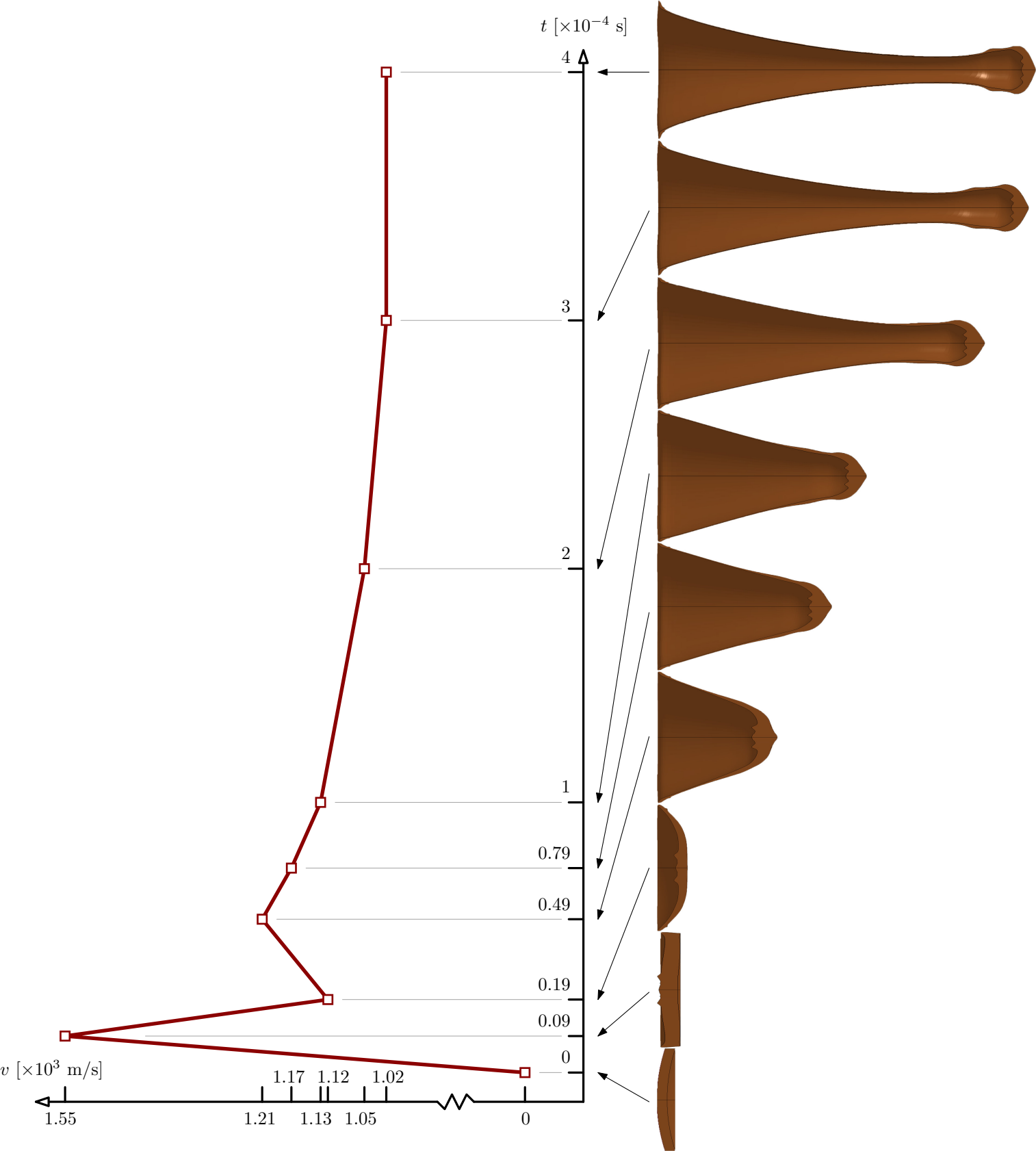


Figure 6a

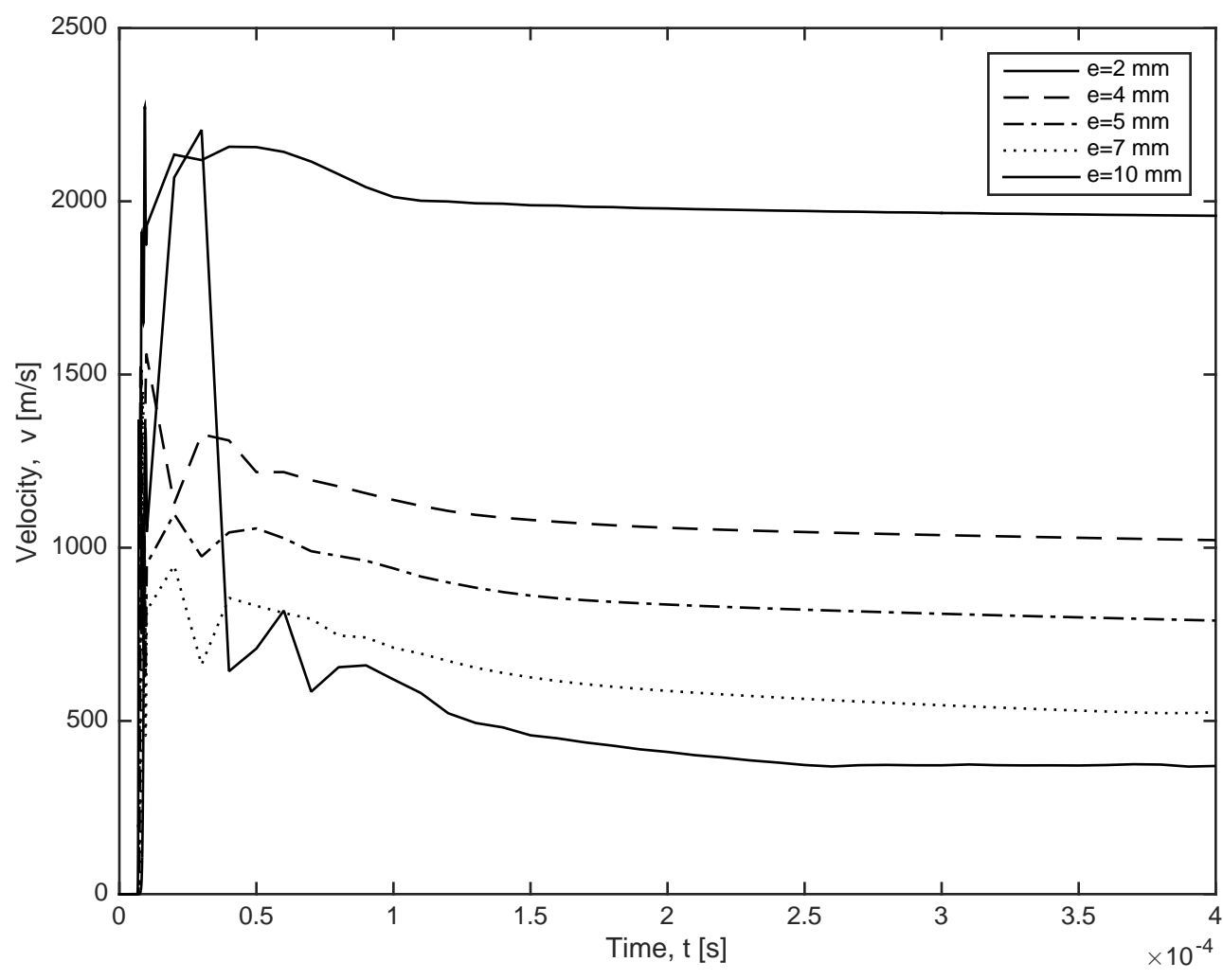
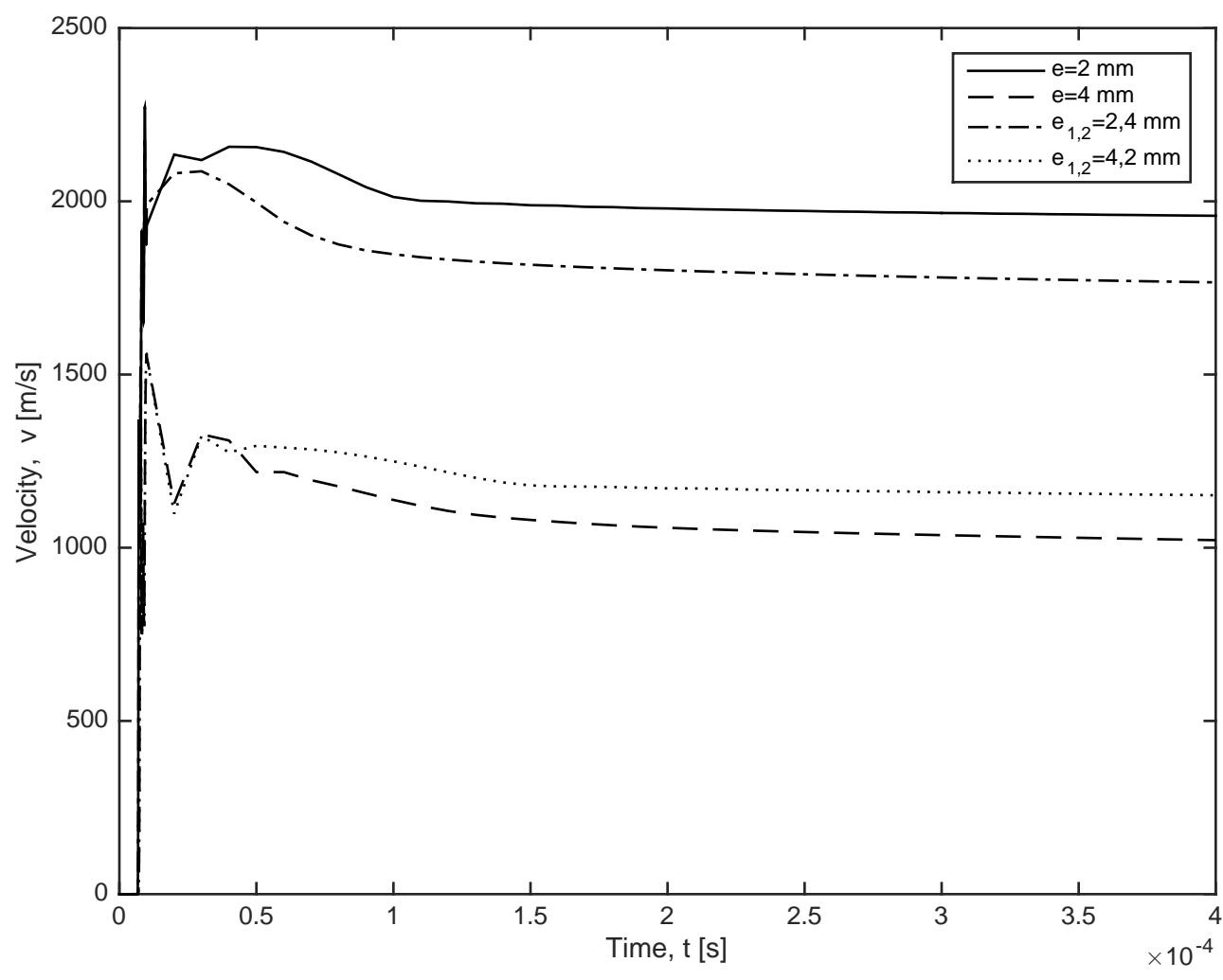


Figure 6b



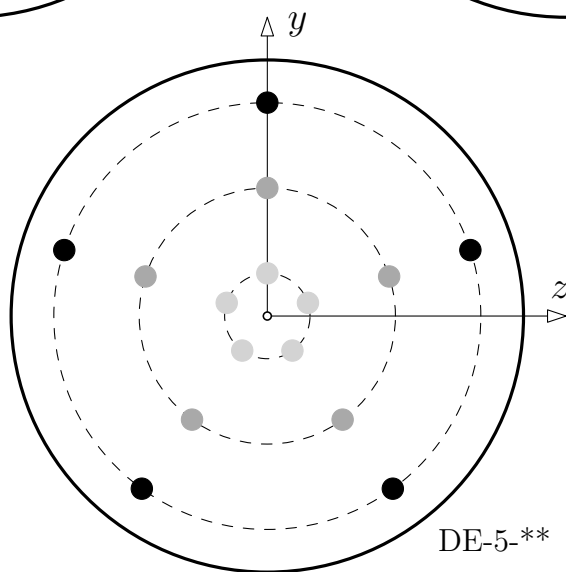
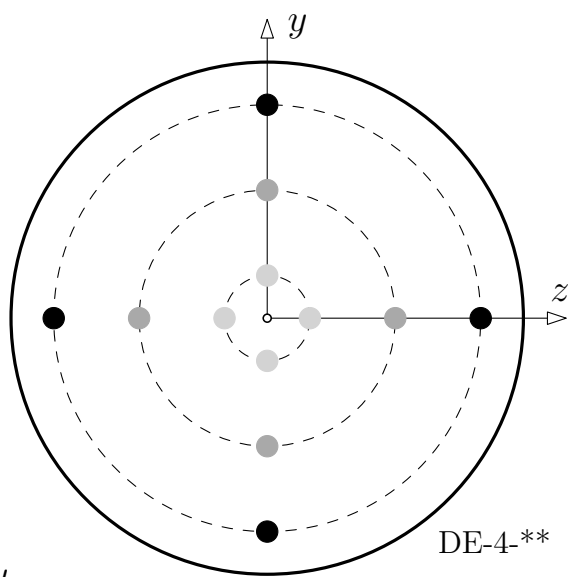
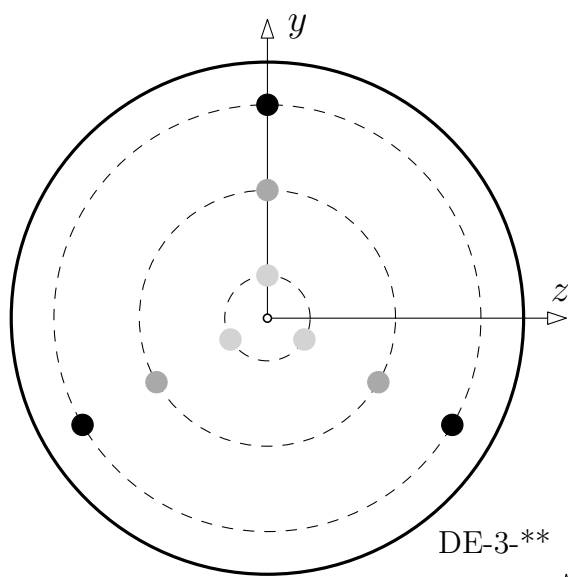
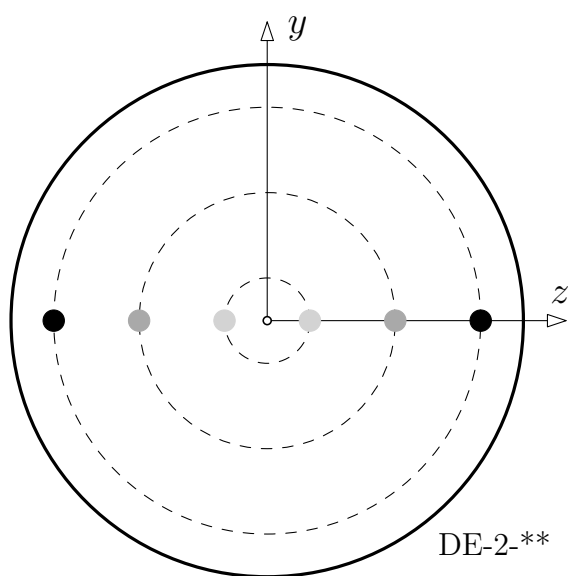
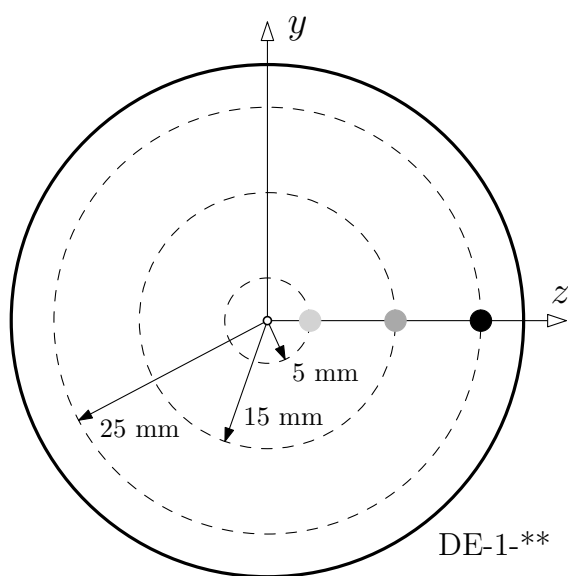


Figure 8a

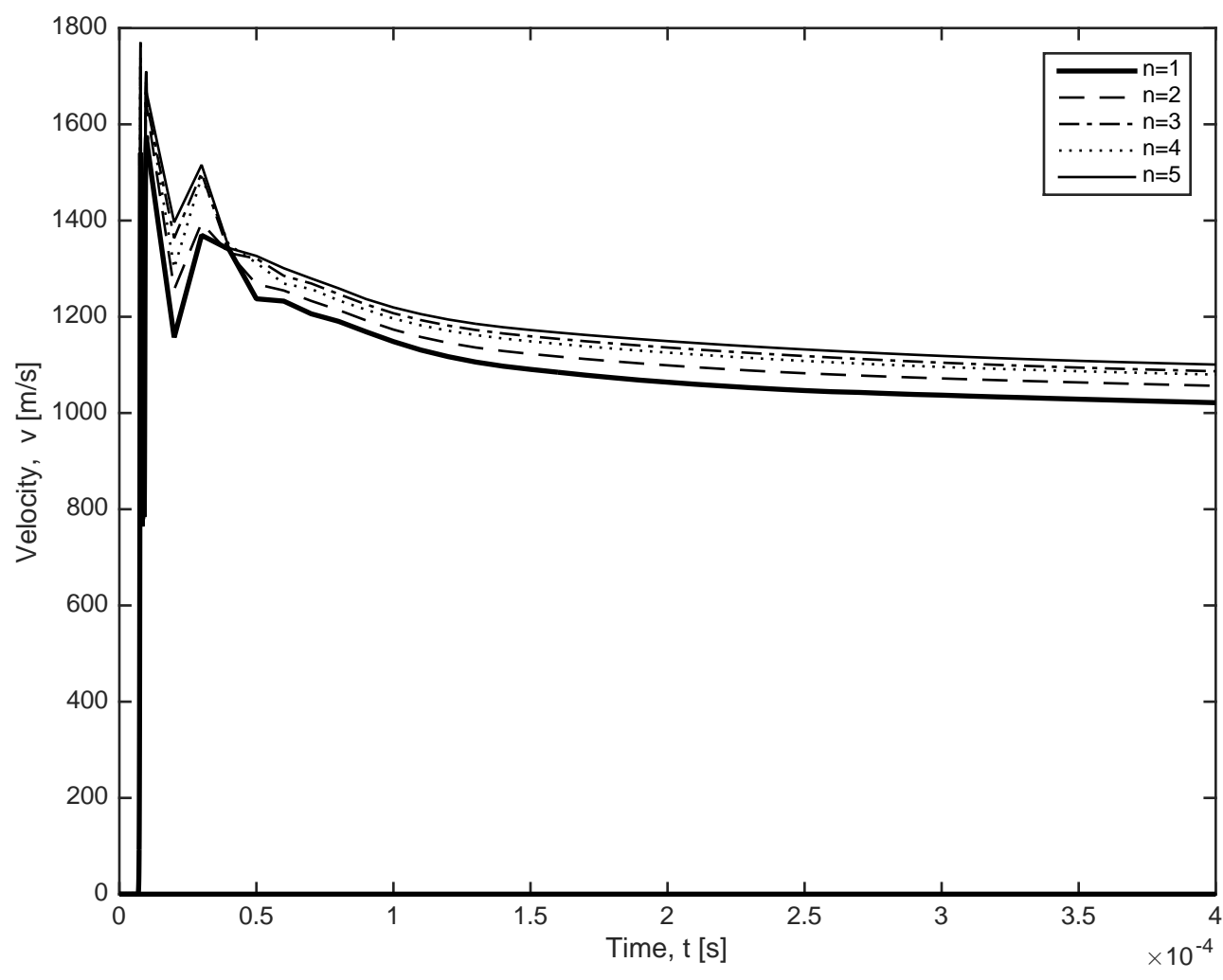




Figure 8b

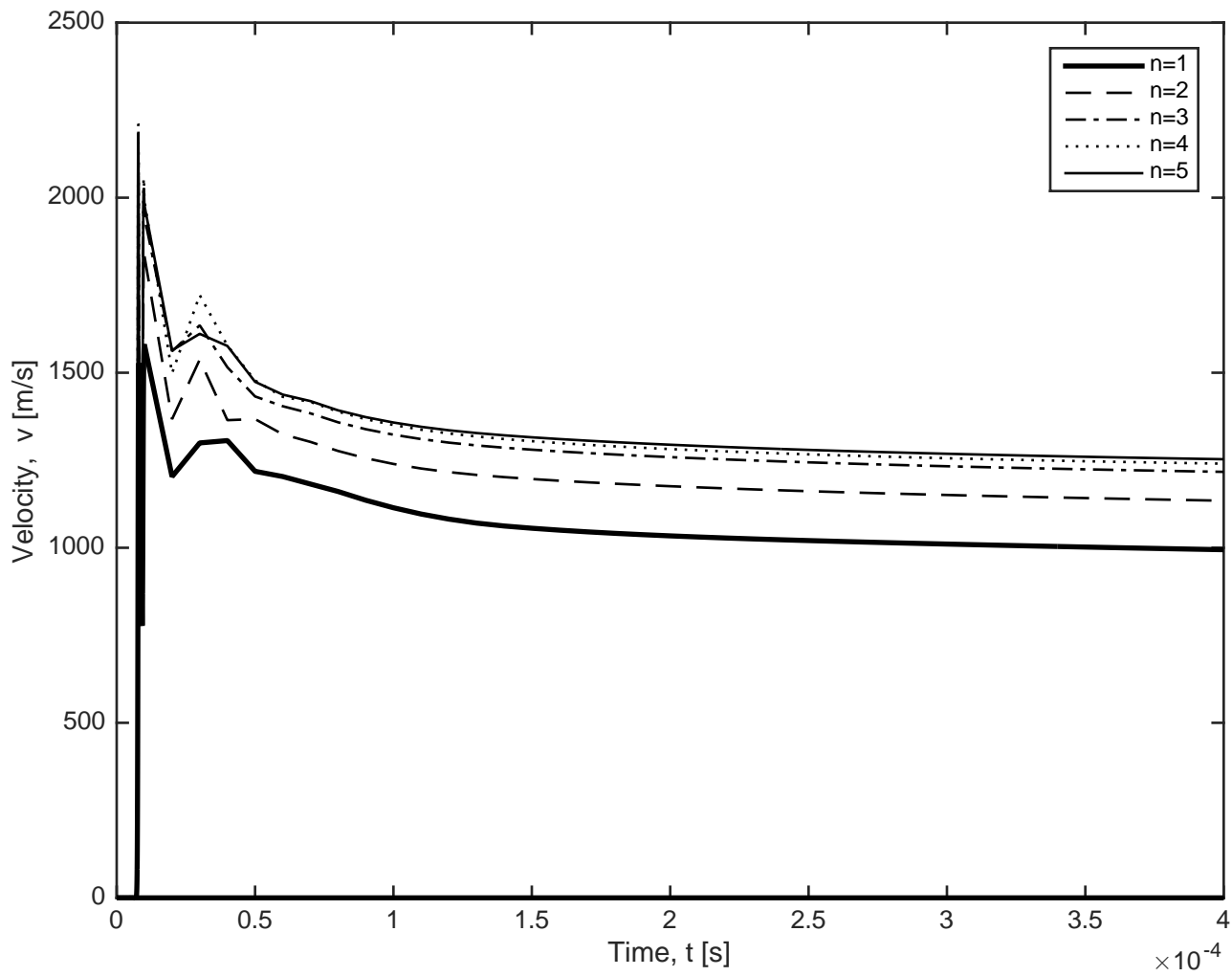


Figure 8c

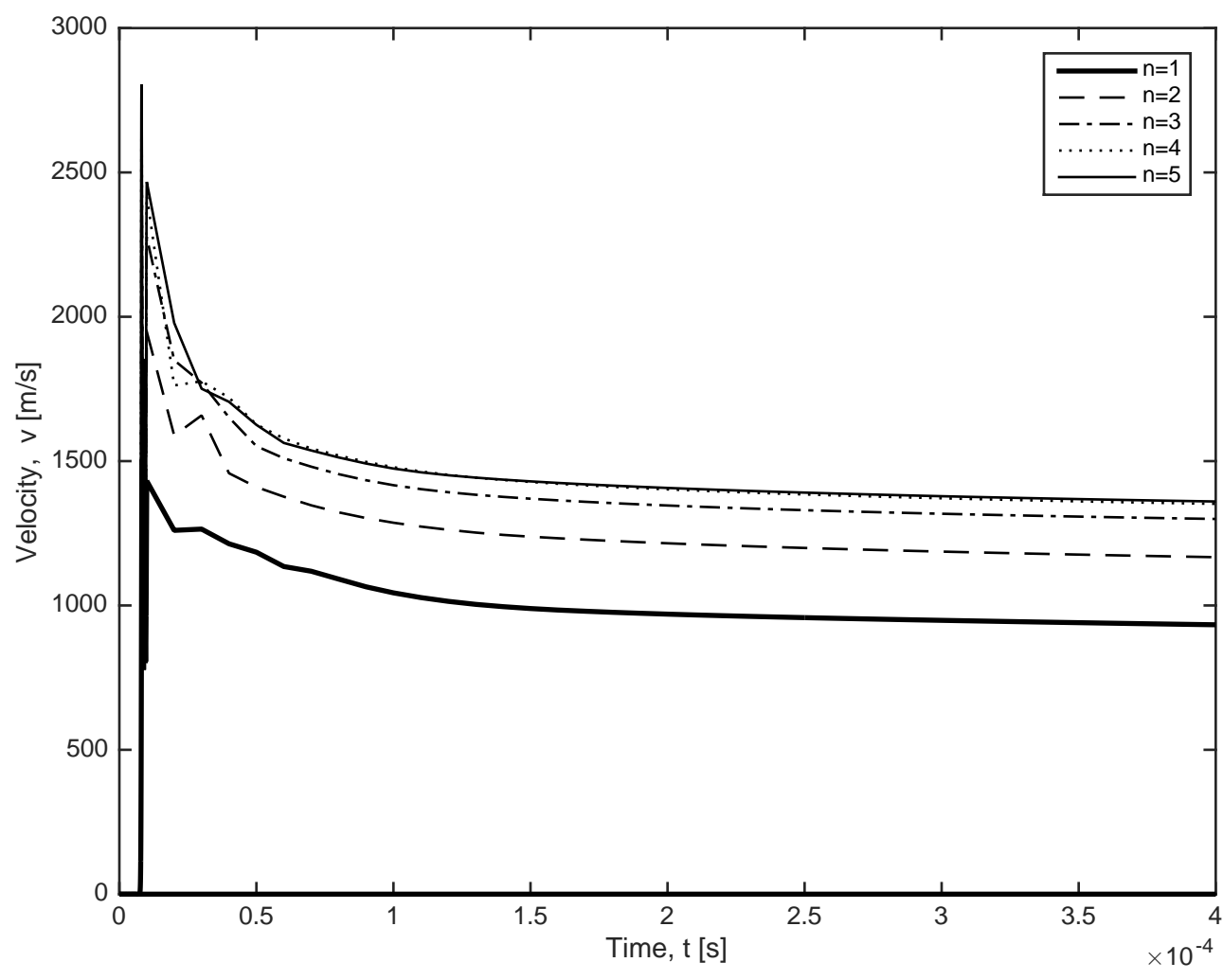


Figure 9

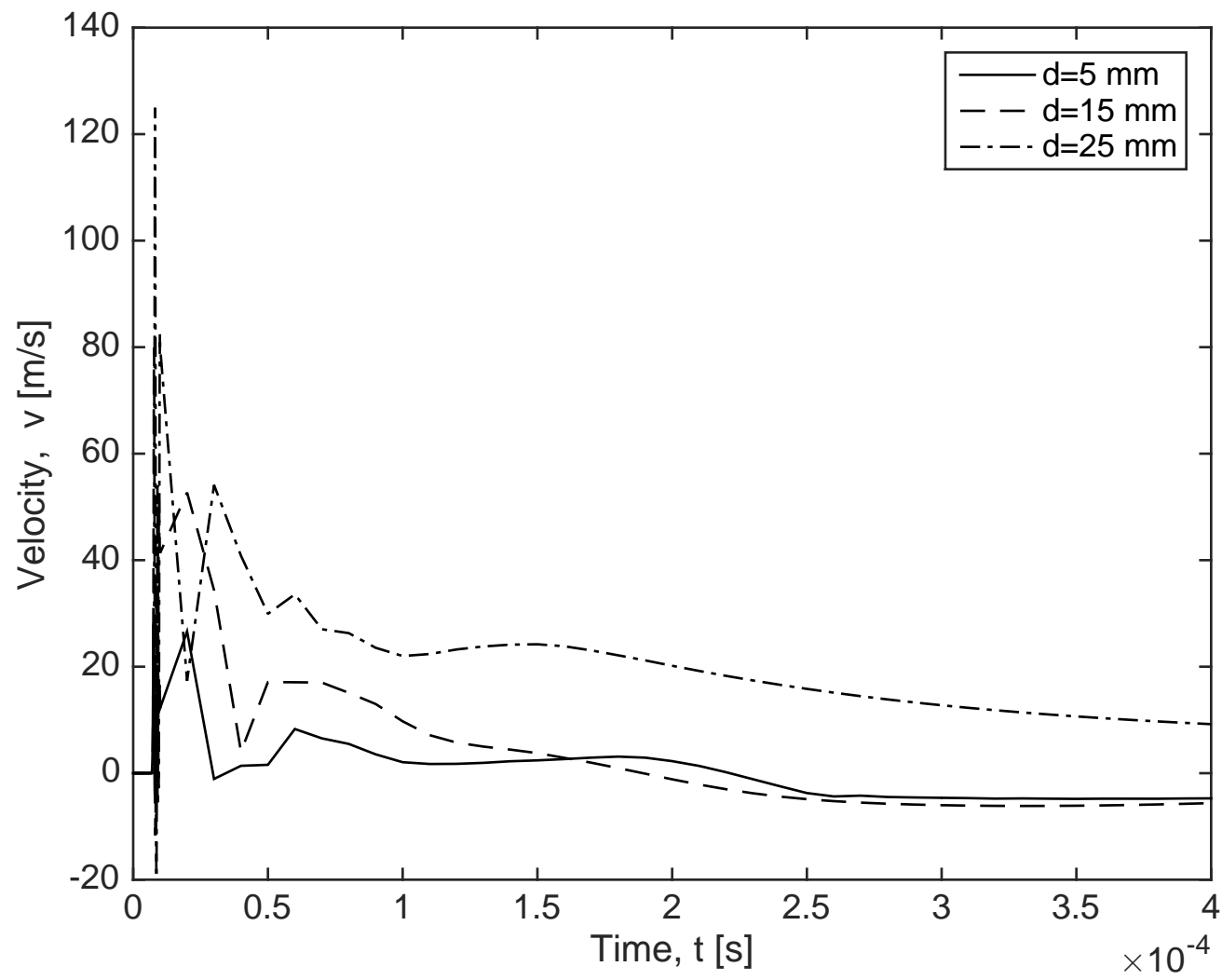


Figure 10

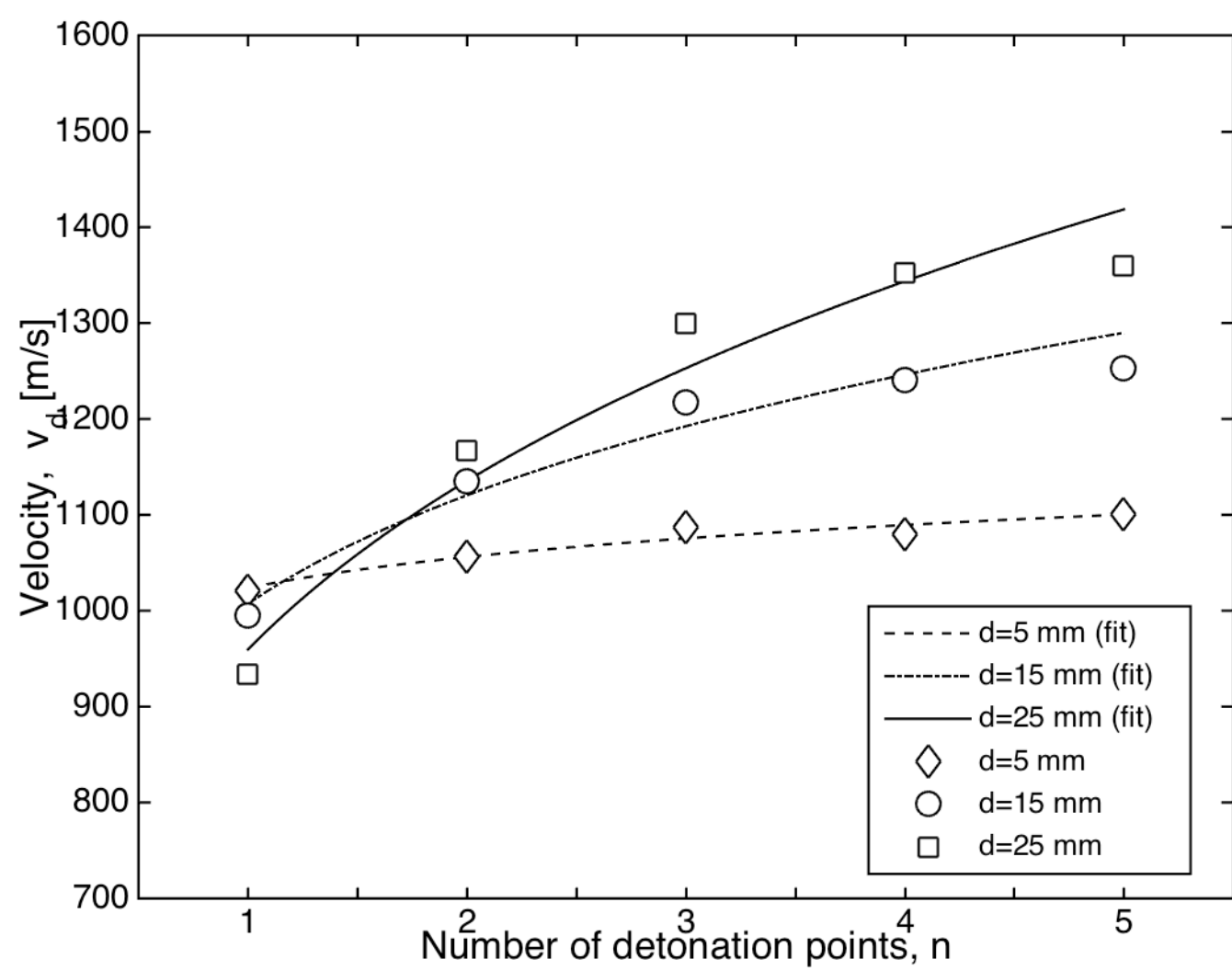
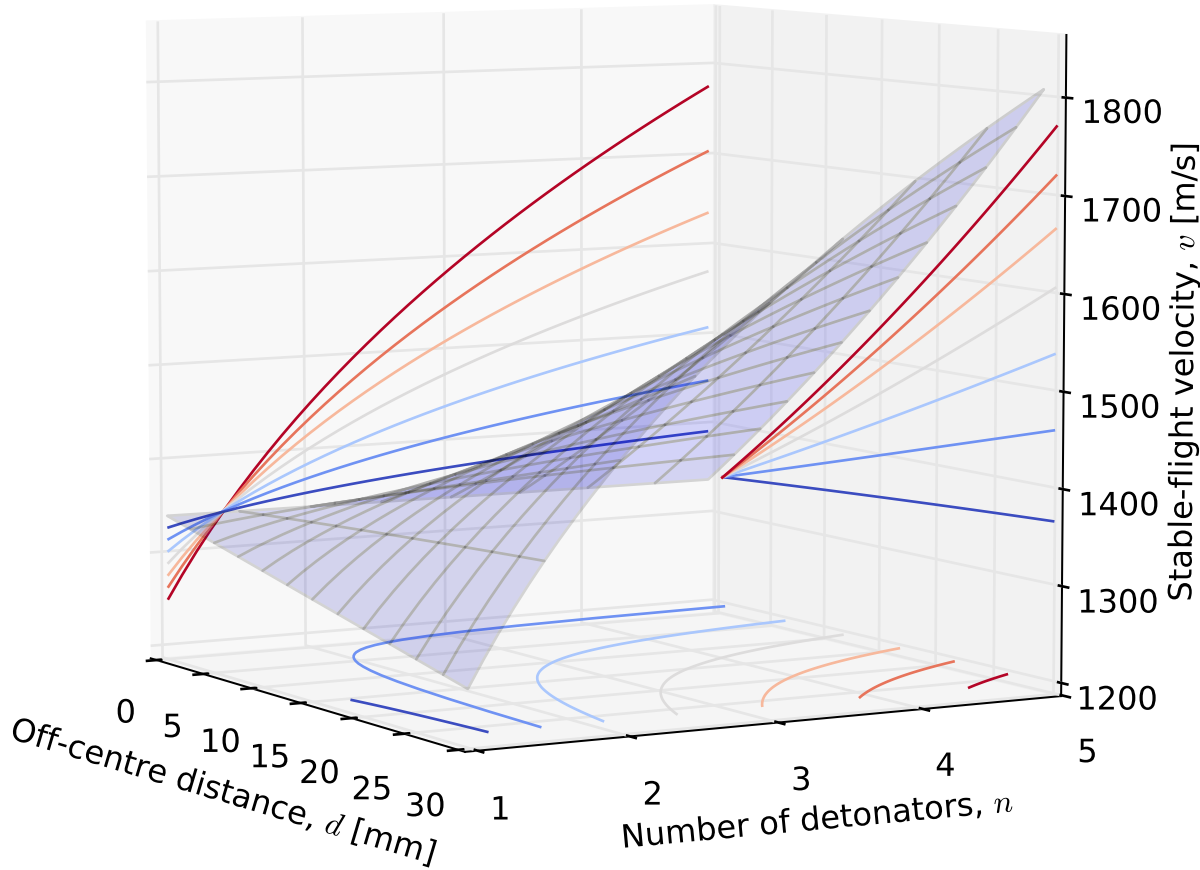


Figure 11



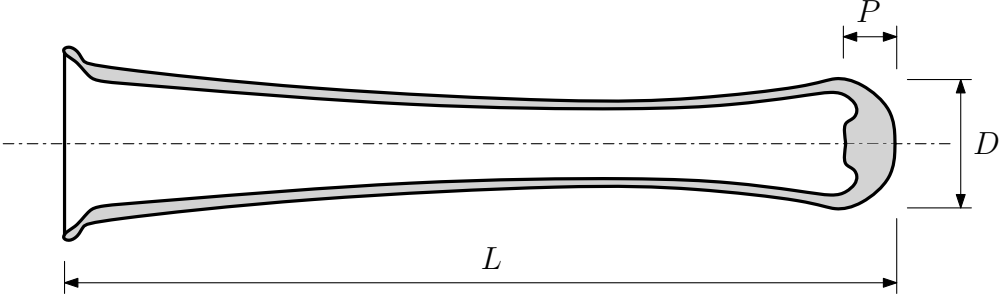


Figure 13

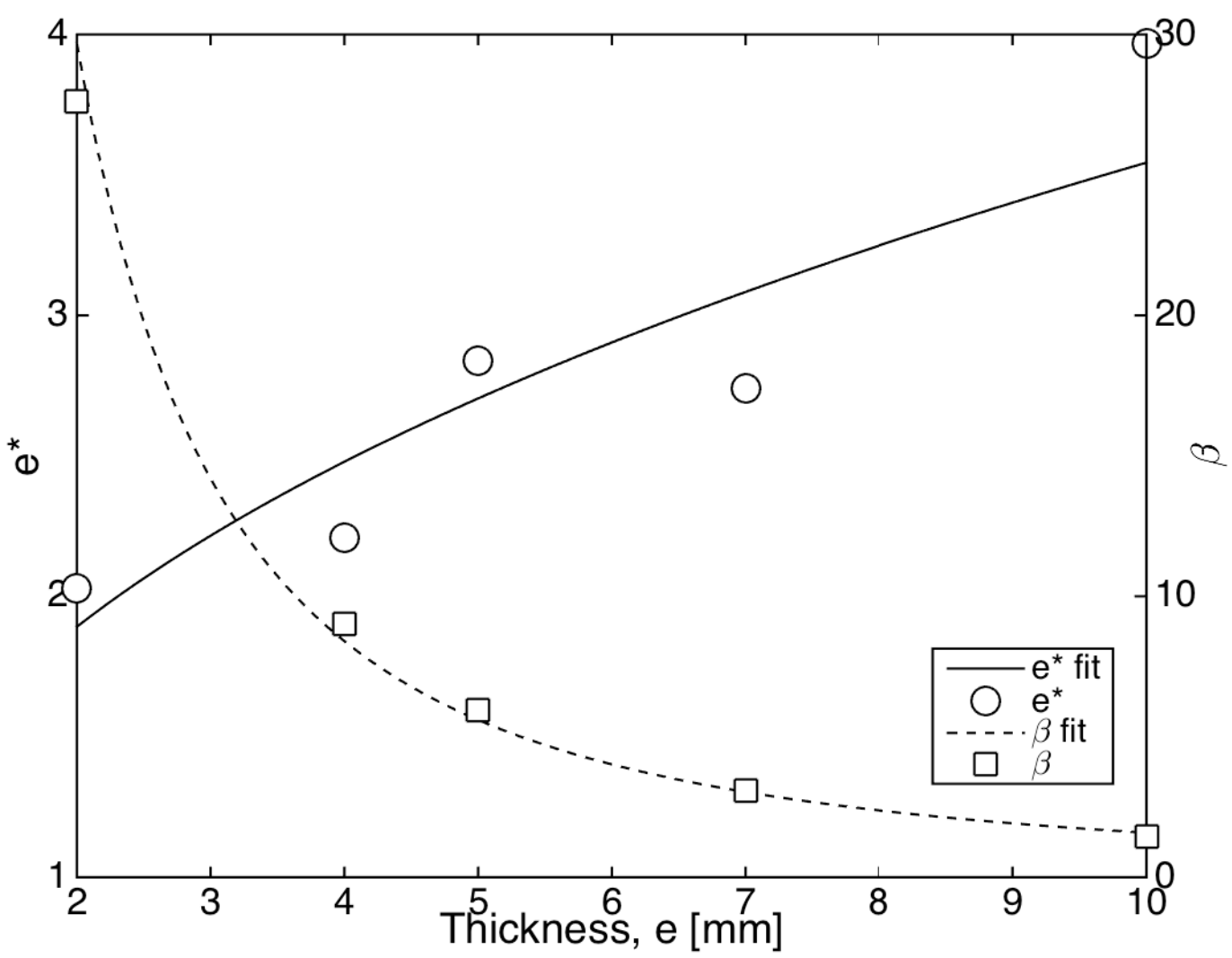


Figure 14a

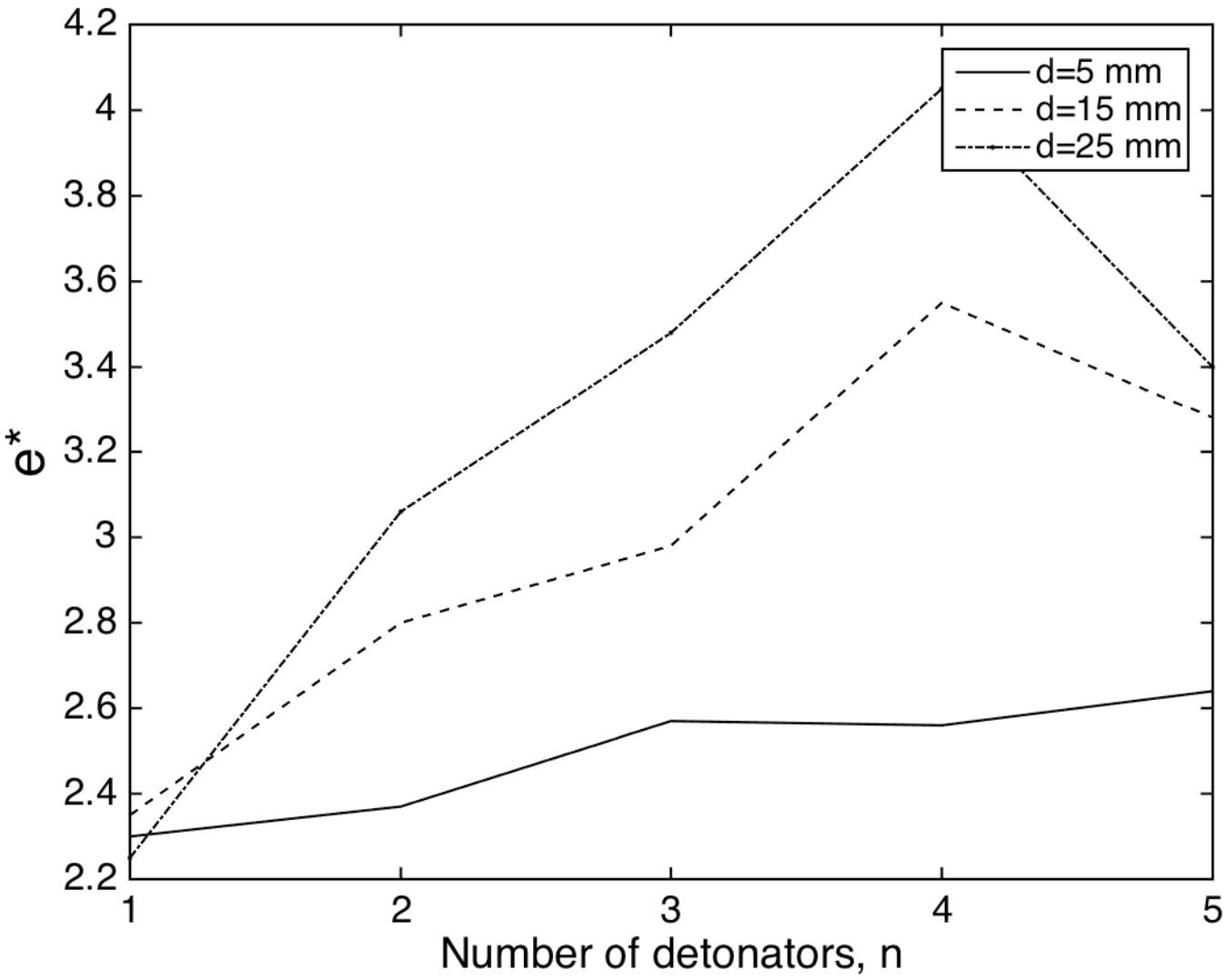




Figure 14b

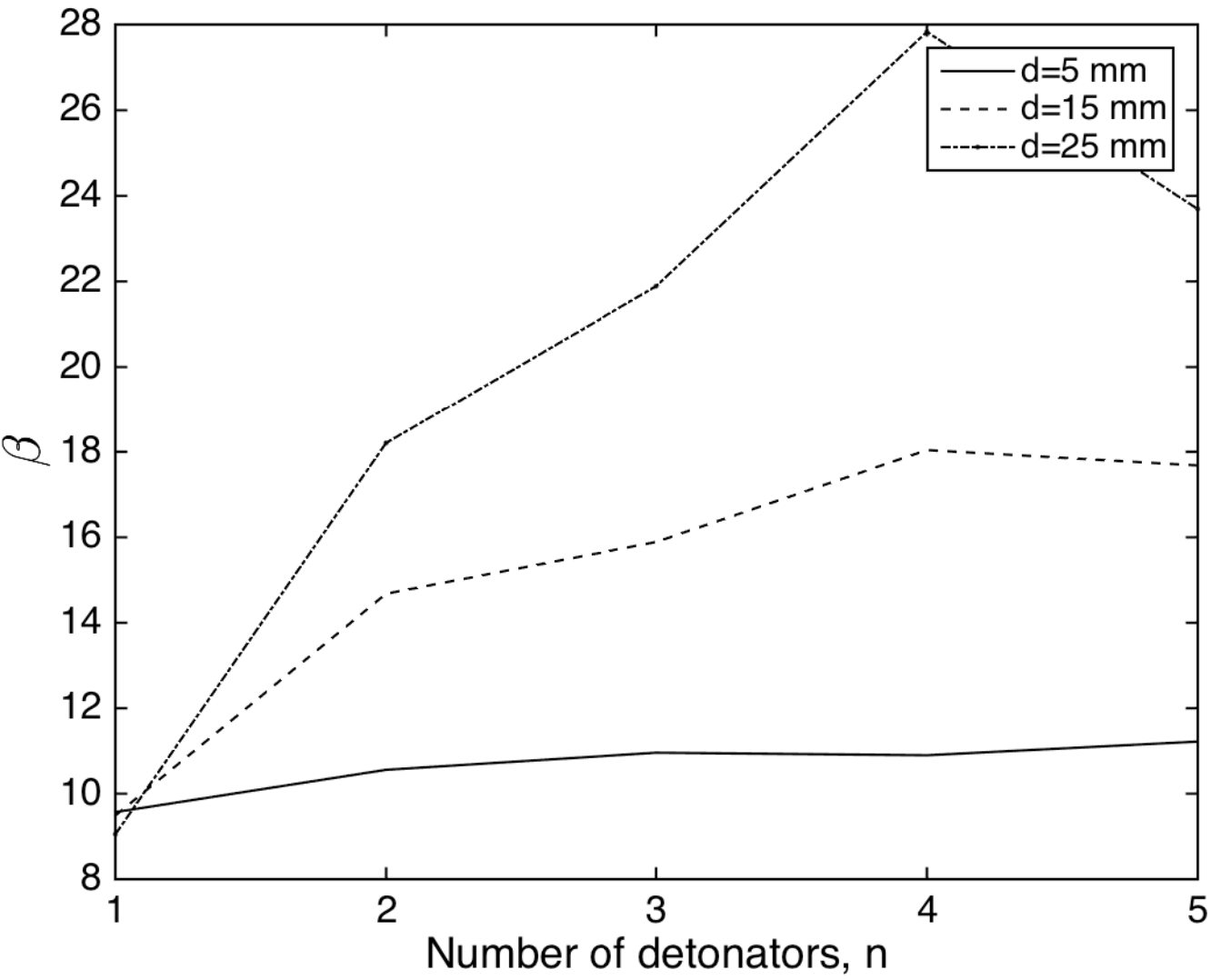


Figure 15a

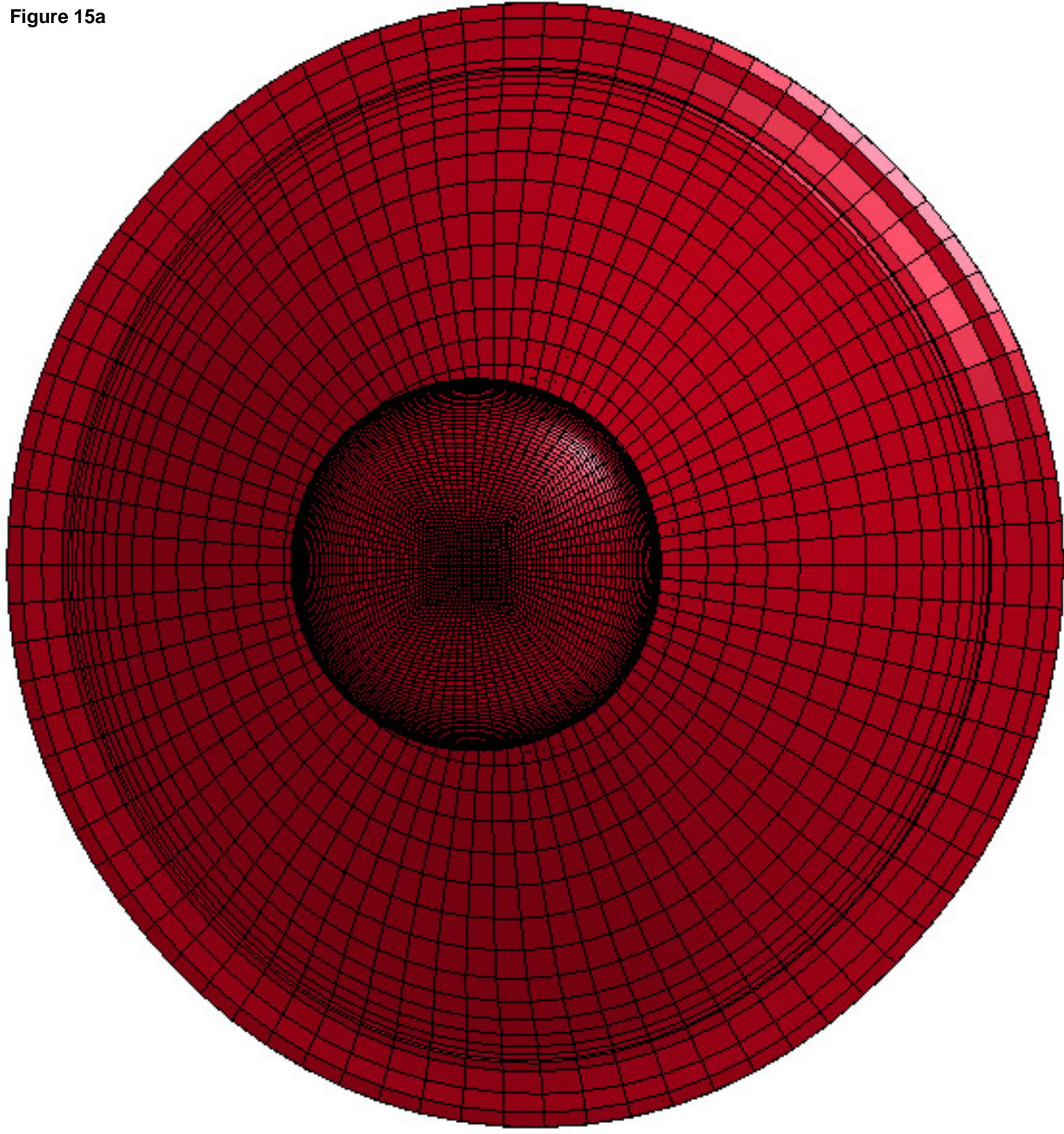




Figure 15b

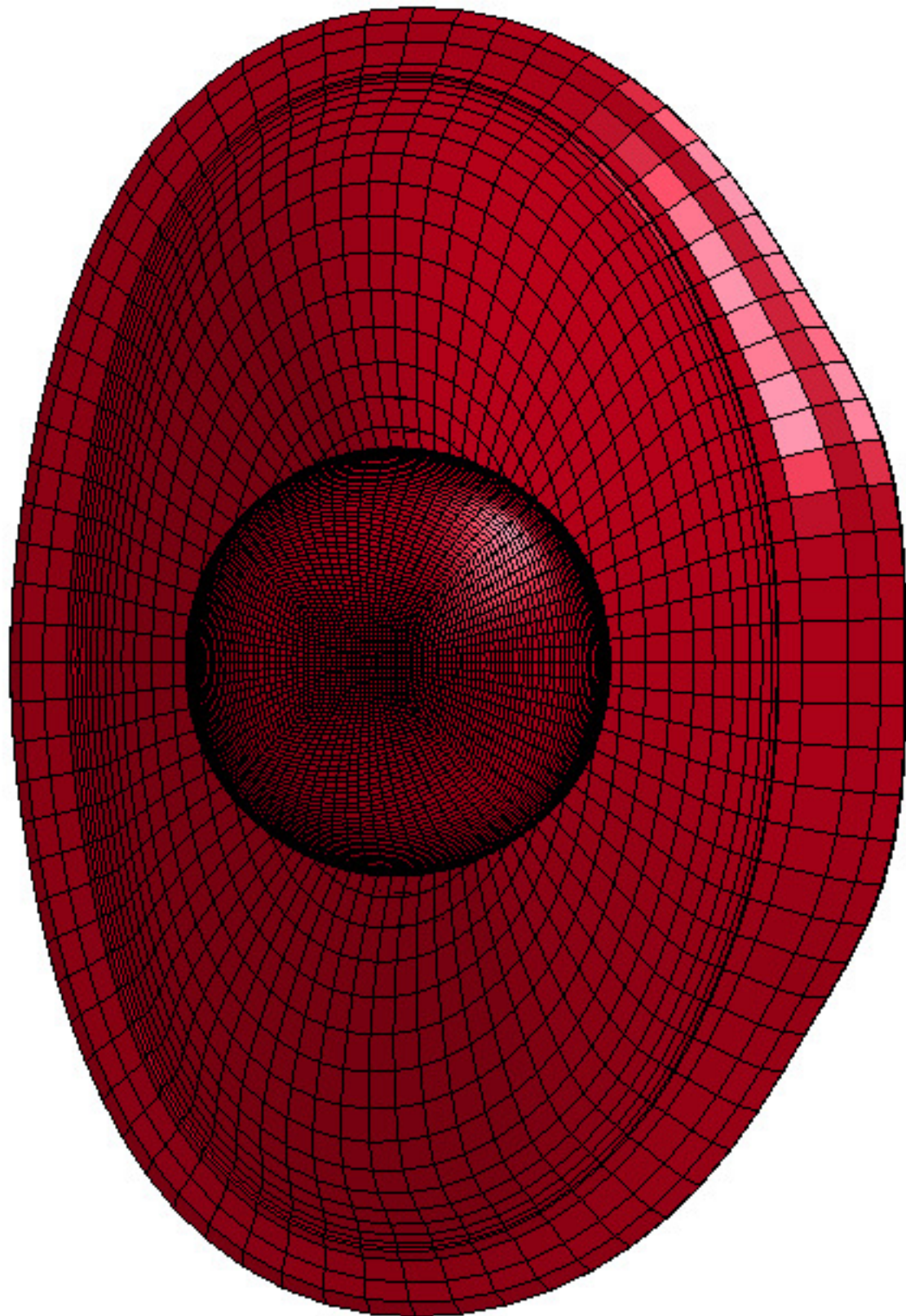


Figure 15c

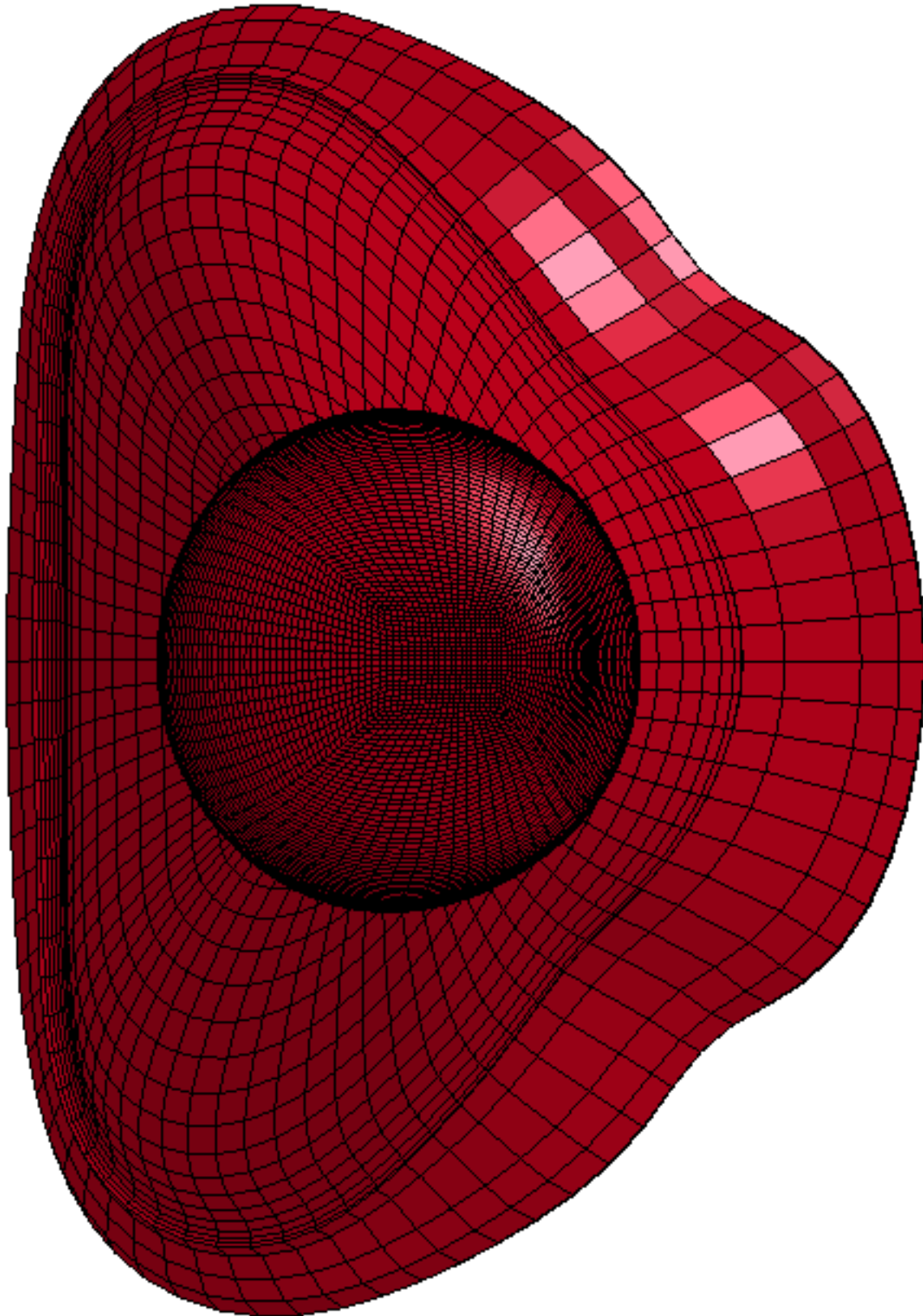




Figure 15d

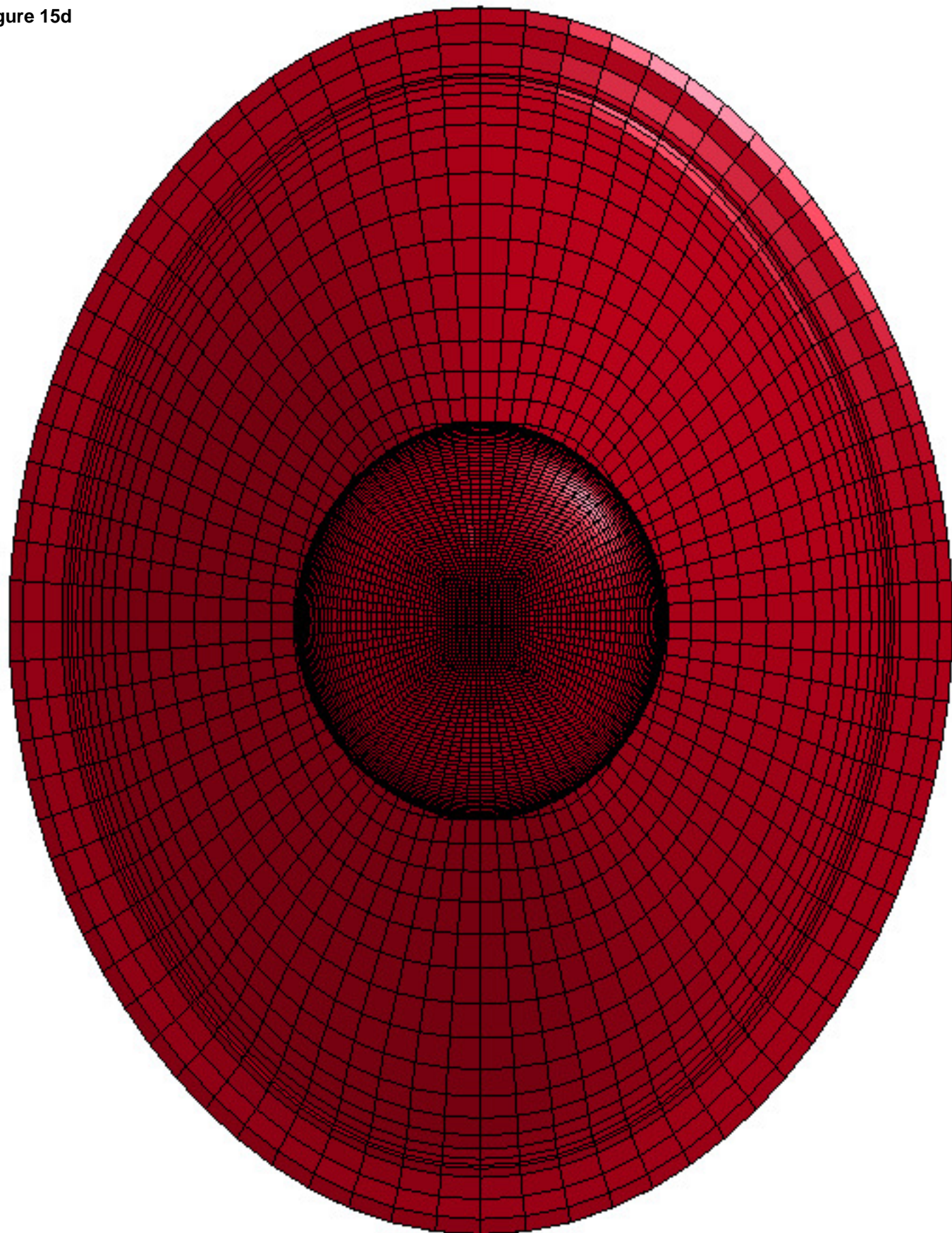


Figure 15e

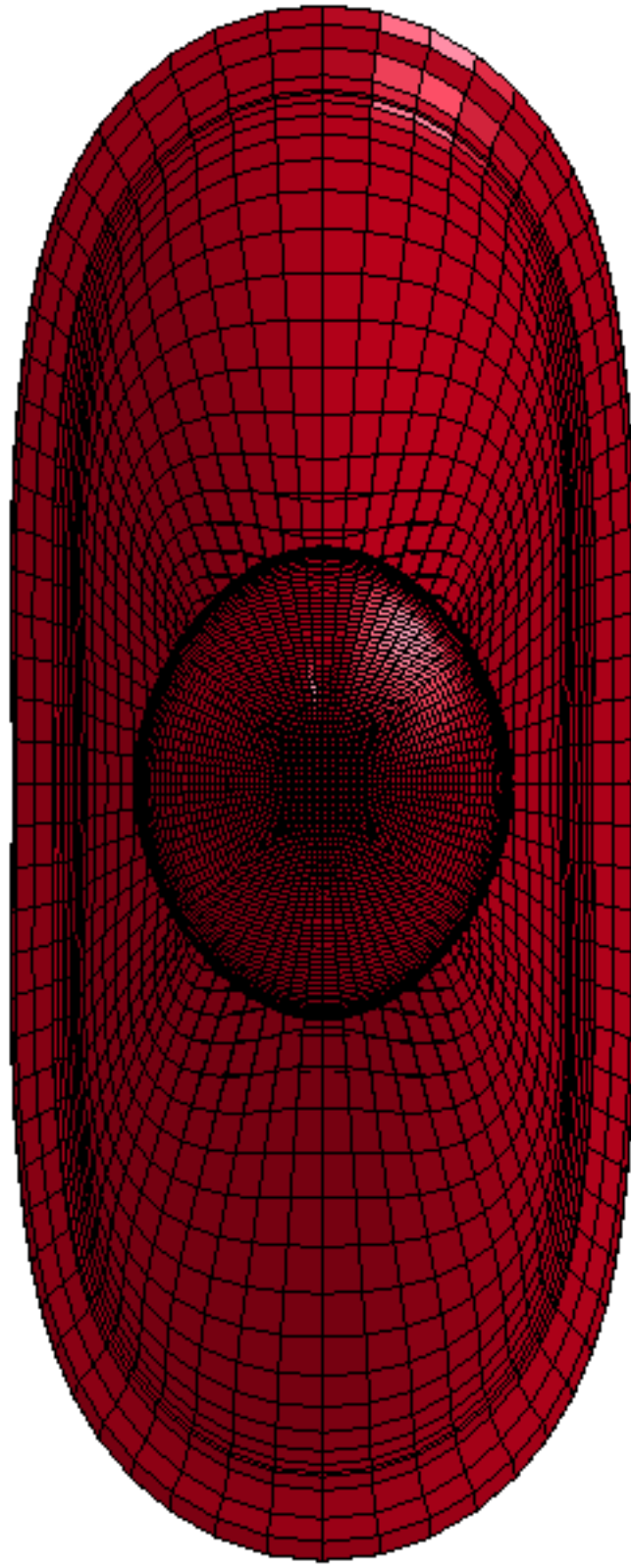


Figure 15f

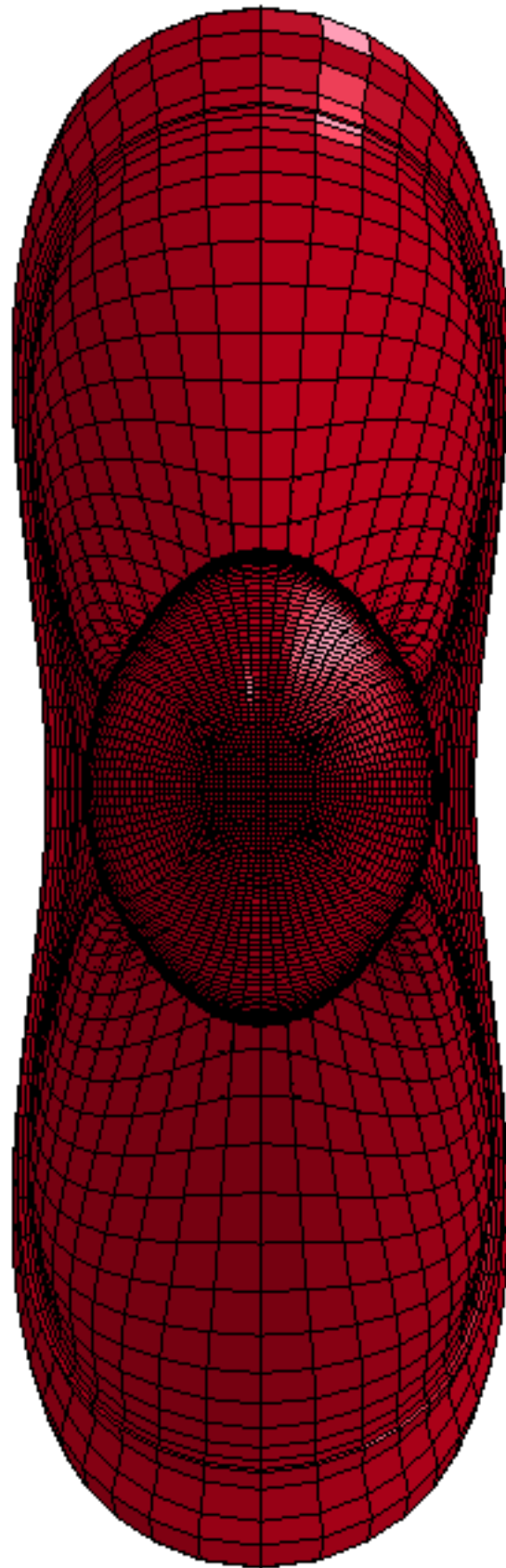




Figure 15g

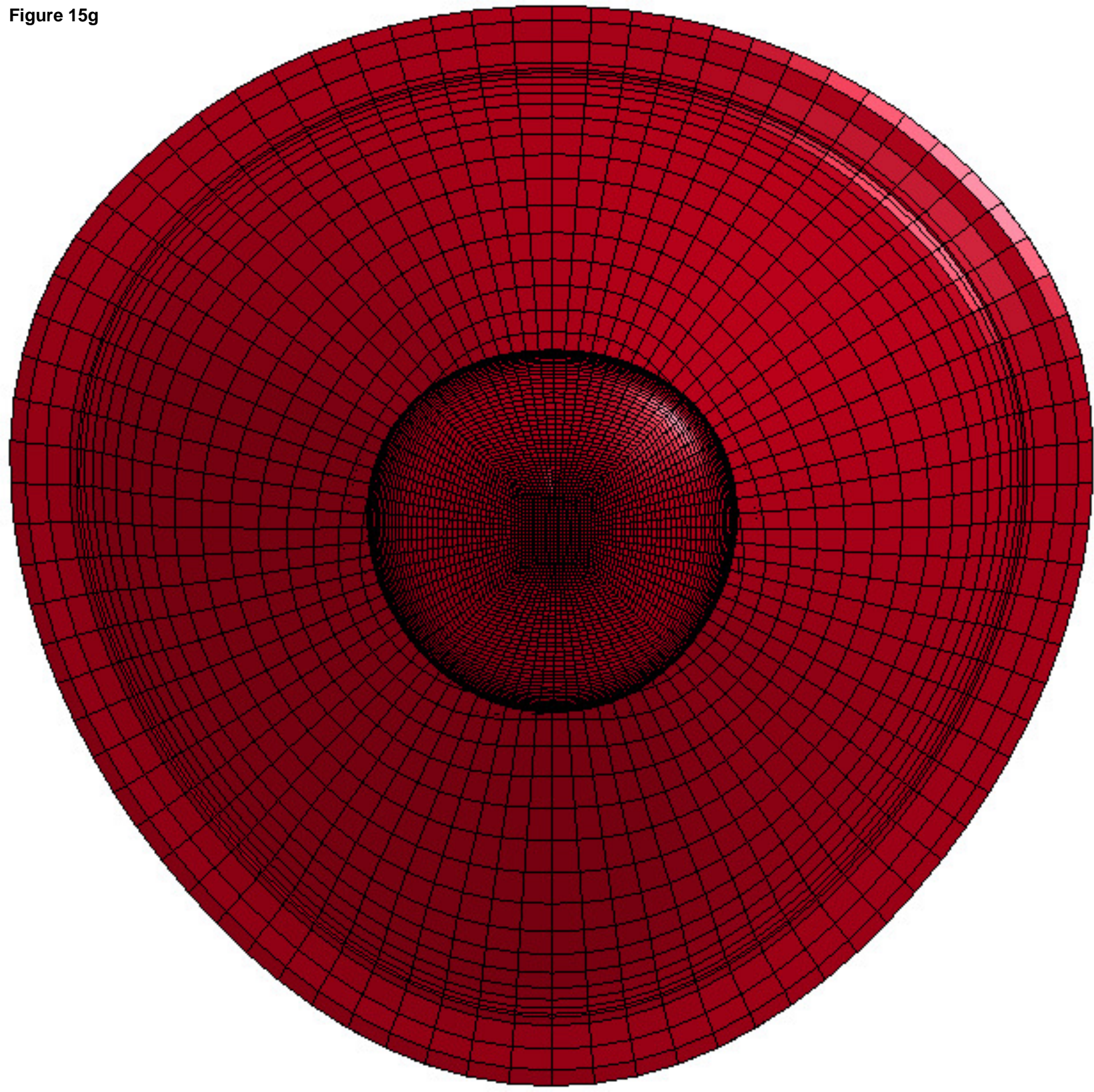




Figure 15h

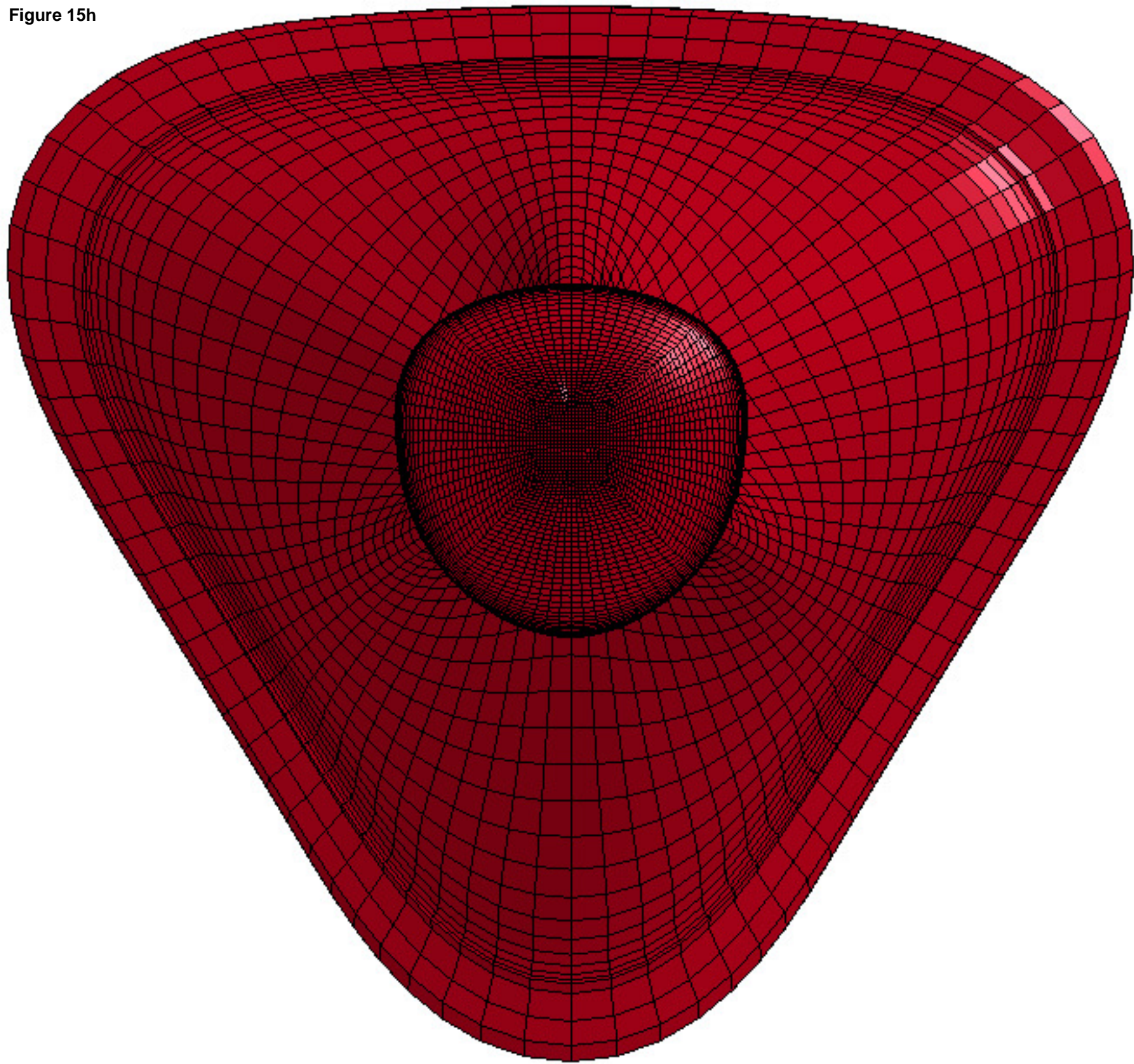




Figure 15i

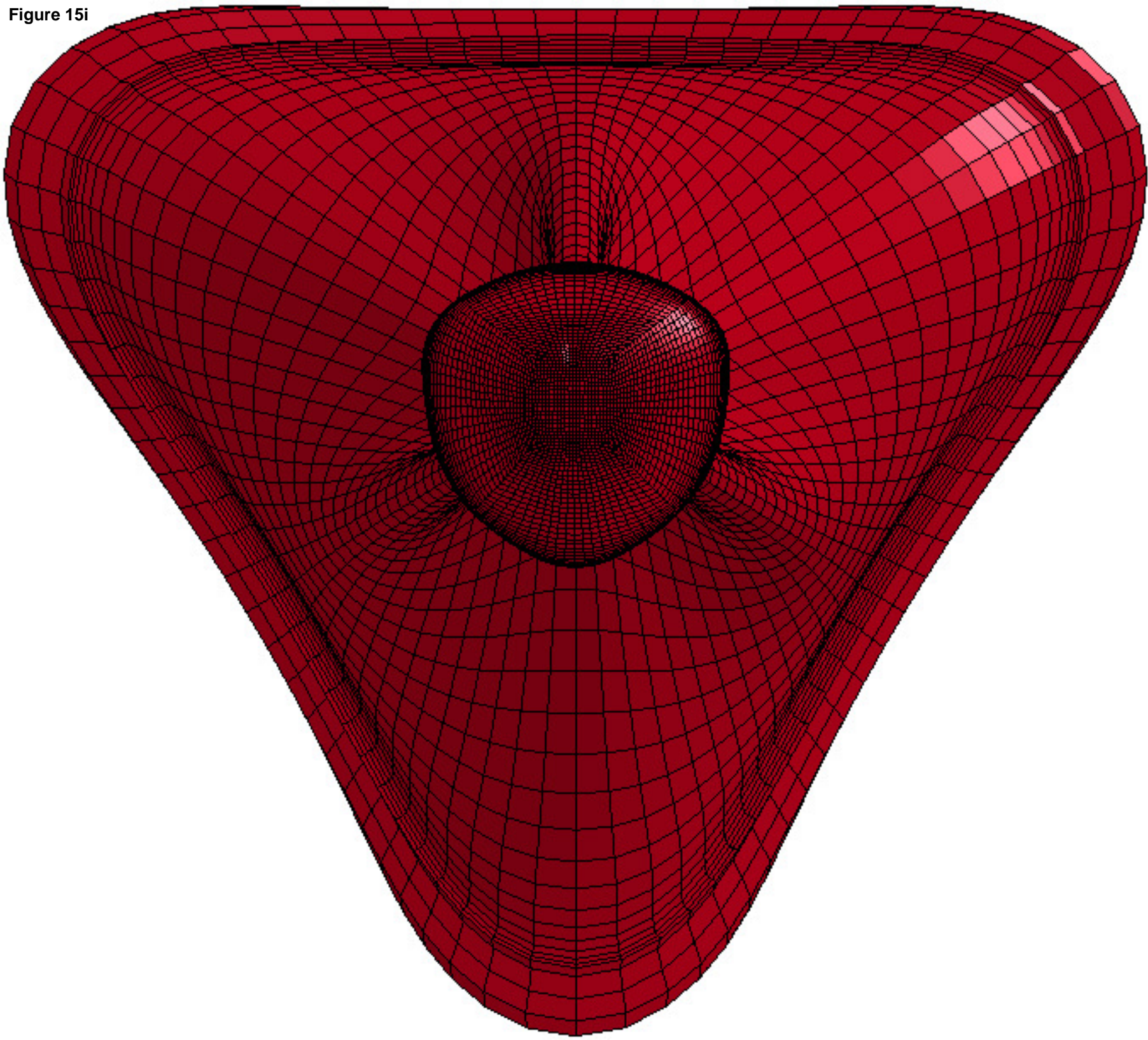




Figure 15j

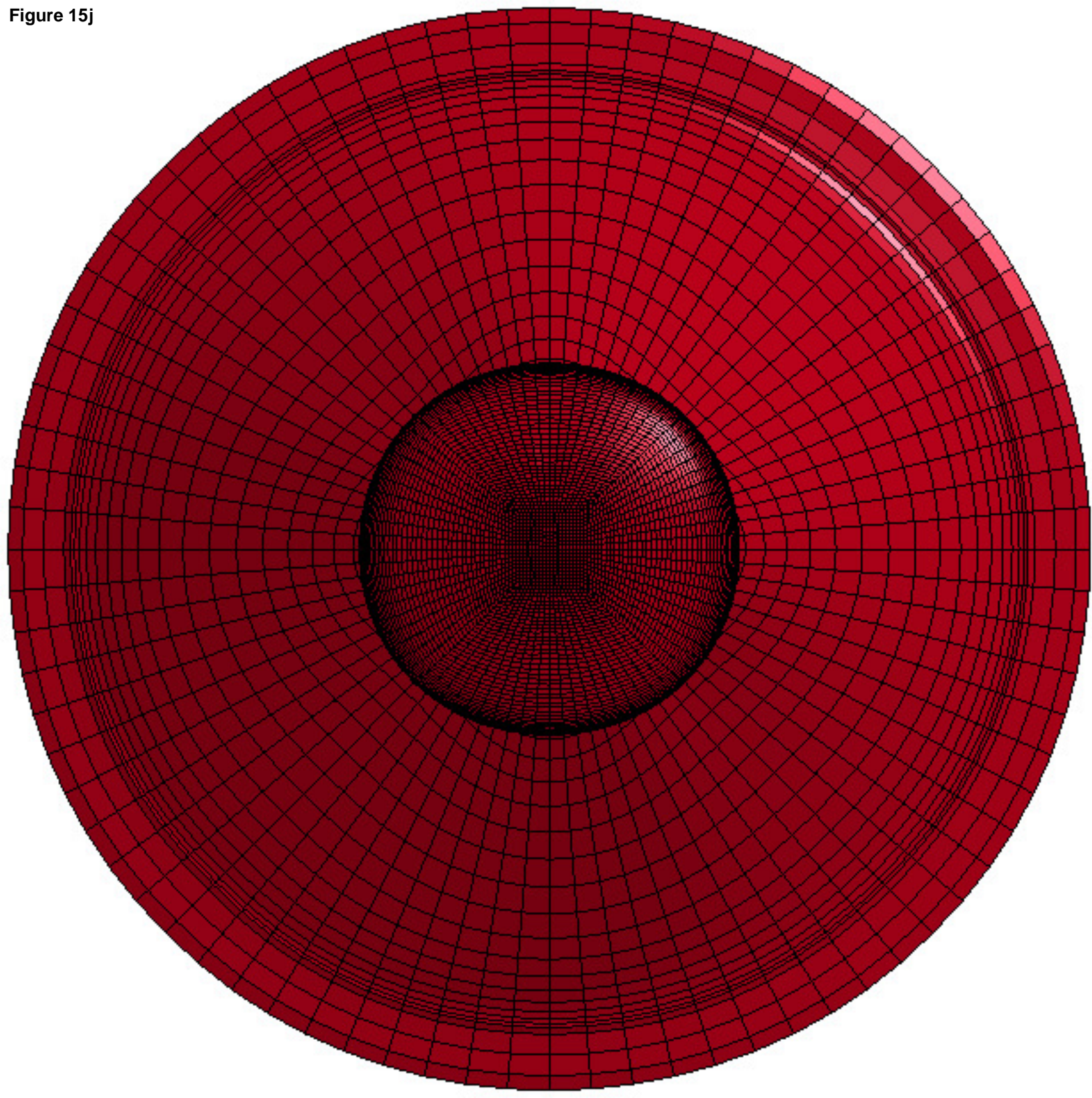




Figure 15k

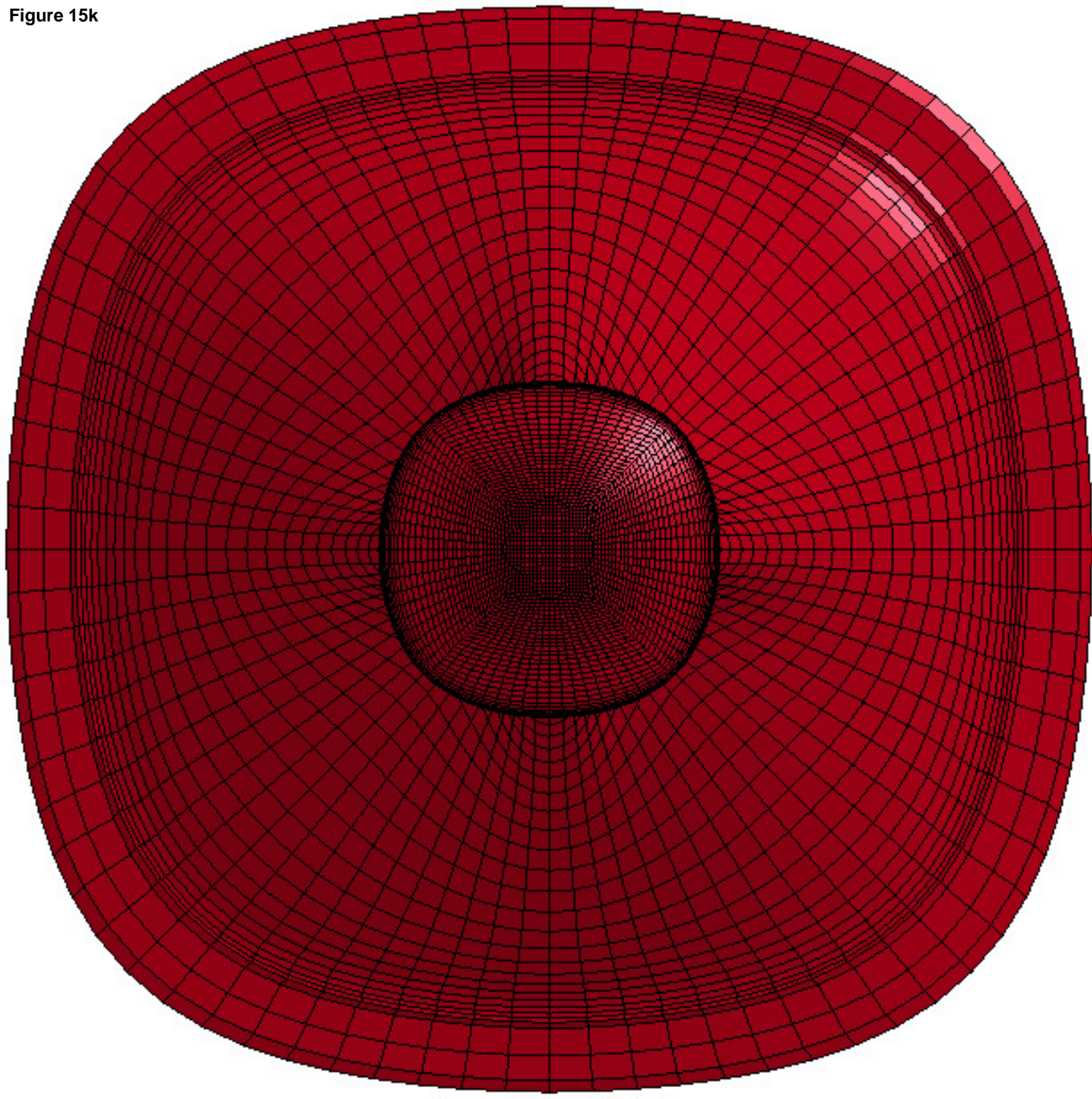




Figure 15I

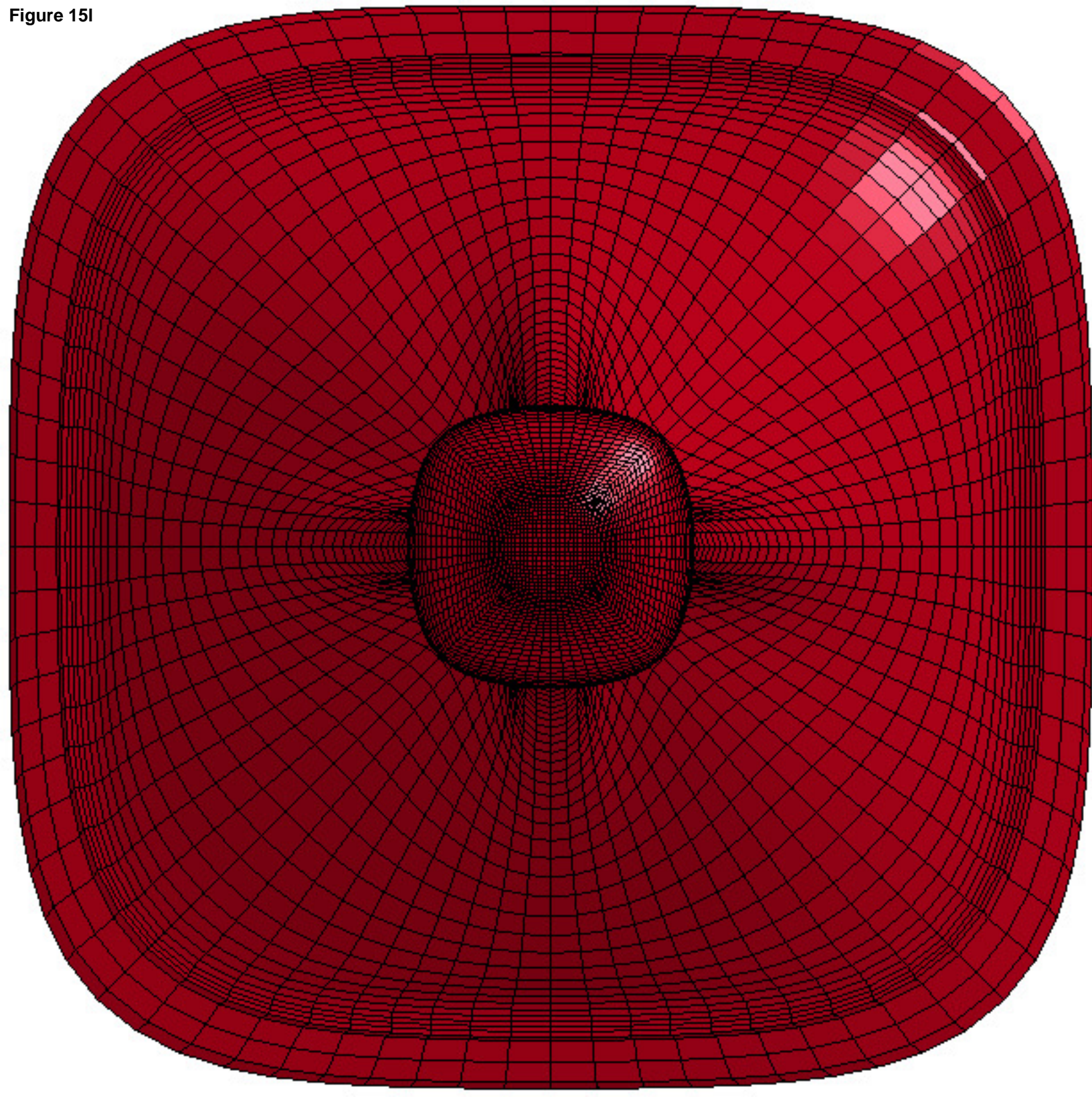




Figure 15m

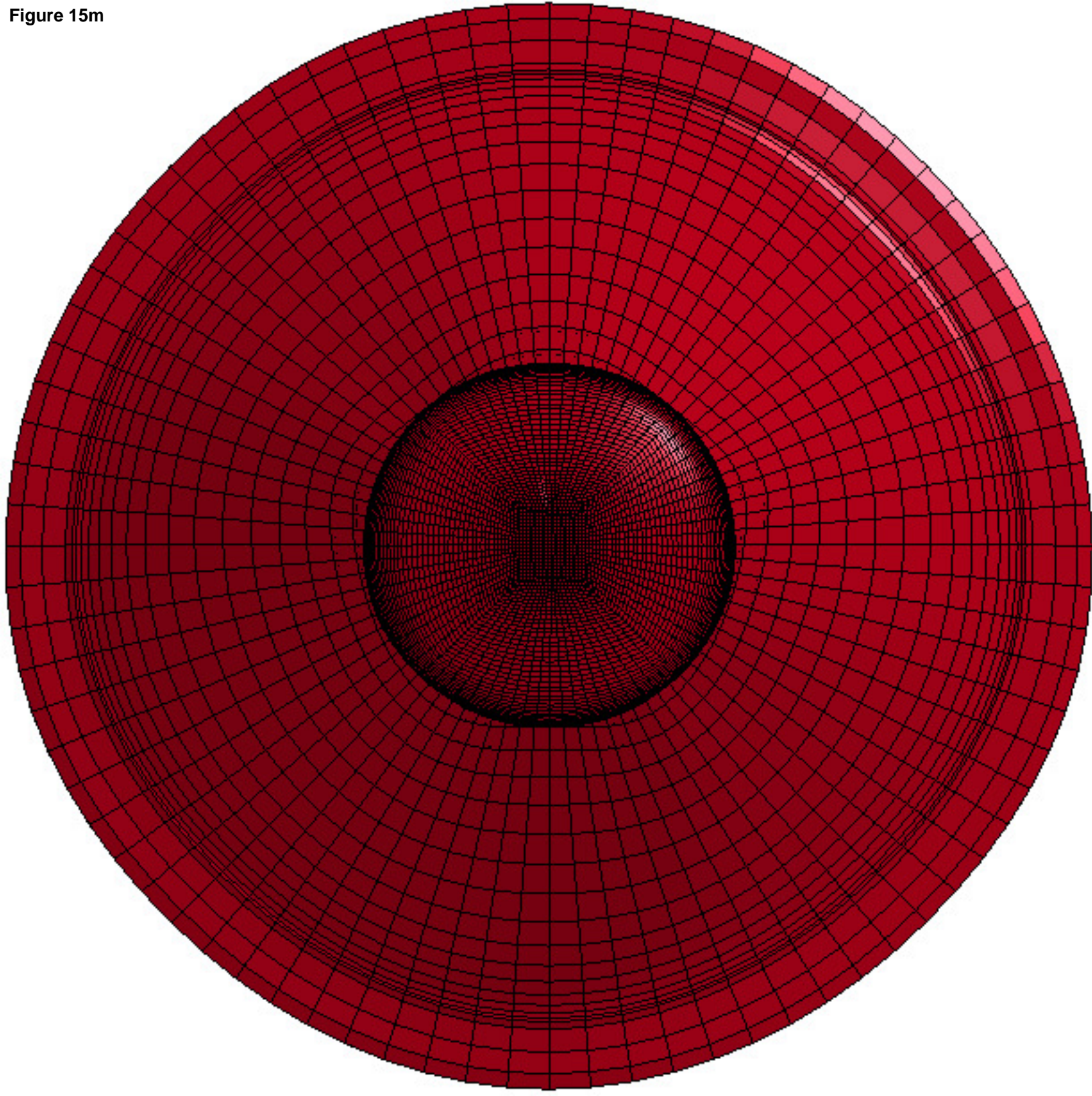




Figure 15n

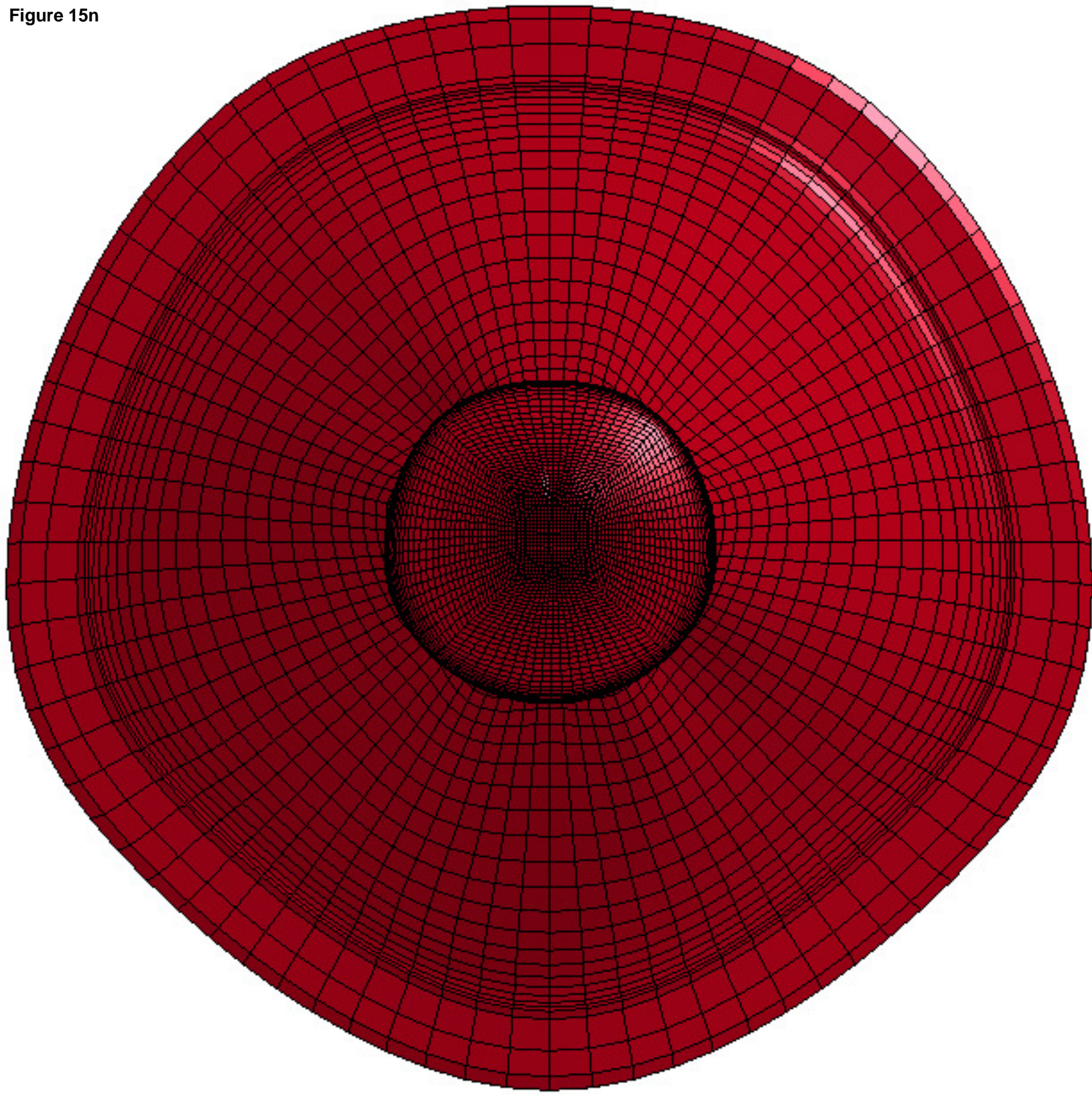
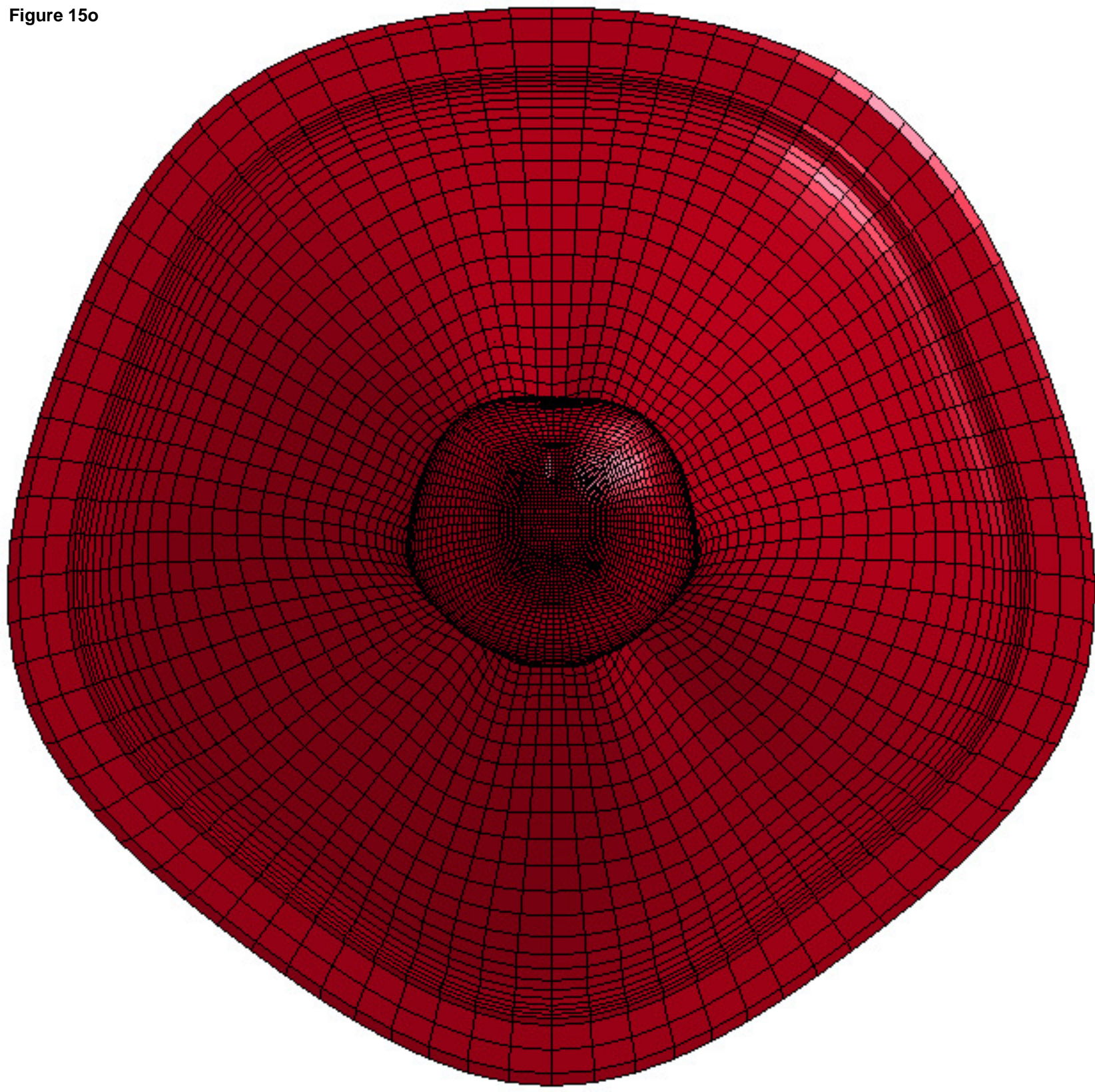
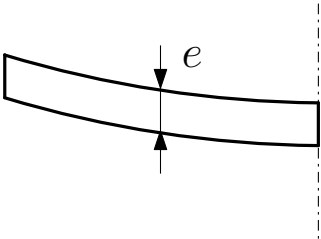


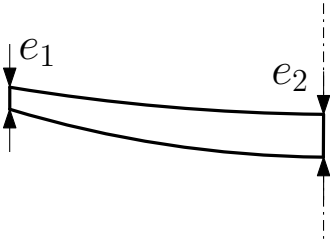


Figure 15o









**LaTeX Source Files**

[Click here to download LaTeX Source Files: 20150601\\_DC-FTD\\_IJIE\\_LaTeX.zip](#)