An analysis of stock market volatility

Citation for published version:

Digital Object Identifier (DOI):
10.1017/S1748499511000339

Link:
Link to publication record in Edinburgh Research Explorer

Document Version:
Peer reviewed version

Published In:
Annals of Actuarial Science

Publisher Rights Statement:
Copyright © Institute and Faculty of Actuaries 2011

General rights
Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy
The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.
An analysis of stock market volatility

Andrew Adams\textsuperscript{1*}  
Seth Armitage\textsuperscript{2}  
Adrian FitzGerald\textsuperscript{2}  

\textsuperscript{1} Heriot-Watt University, UK  
\textsuperscript{2} University of Edinburgh, UK  

Pre-publication draft, September 2011  

* Corresponding author  
Address:  
Centre for Finance and Investment  
School of Management and Languages  
Heriot-Watt University  
Edinburgh EH14 4AS  
Tel: +44 (0)131 451 8284  
E-mail: A.T.Adams@hw.ac.uk  

Annals of Actuarial Science 6, 2011, pp. 153-70
An analysis of stock market volatility

Abstract
This paper provides a user-friendly approach to explain how variation in fundamental price-determining variables ‘translates into’ variation in the fundamental value of equities, based on the standard dividend-growth model. The analysis is illustrated with UK data using estimates of real interest rate forecasts and real dividend growth rate forecasts in the past. An important application of this approach is that stock market volatility can be analysed in terms of its component parts. Actual market volatility does not appear to be excessive when compared with the notional volatility implied by changes over time in our estimates of forecast real interest rates and forecast real dividend growth rates.

Keywords: Excess volatility; rational valuation; dividend-growth model; equity risk premium

JEL: G14

1. Introduction
The value of a share is determined, in theory, by the expected dividends and other cash payments which the share provides, and by the discount rate or rates at which the expected payments are discounted. The discount rate is given by the risk-free interest rate plus a risk premium. If the view of ‘the market’ changes about one or more of these price-determining variables, the share price should change. The main aim of this paper is to explain how variation in the price-determining variables ‘translates into’ variation in fundamental value.

An important application of our analysis lies in the study of stock market volatility. It is widely believed that there are periods when actual stock market value deviates substantially from its fundamental value, resulting in increased market volatility. In other words, much of the observed market volatility is thought to be a result of ‘irrational’ valuations, i.e. valuations affected by behavioural factors that do not appear in standard finance models of asset value. The claim that prices are excessively volatile can be expressed as a claim that prices vary over time by more than is justified by variation in the price-determining variables. The analysis
will therefore help readers to form a better-grounded view as to whether markets are indeed excessively volatile.

The original debate on volatility was prompted by Shiller’s (1981) finding that stock market value varies over time much more than does the present value of subsequent dividends, assuming perfect foresight for dividends and interest rates. Campbell & Shiller (1988) allow forecasts of the real interest rate and real dividend growth rate to vary over time, and they use vector autoregression (VAR) to arrive at these forecasts. The risk premium, the expected return on equity less the risk-free interest rate, is assumed to be constant. They conclude that changes in the forecasts are insufficient to explain the observed volatility of US market values. Shiller & Beltratti (1992) present similar evidence using UK data. This evidence raised the question as to whether the ‘excess’ volatility thus identified can reasonably be explained by changes in the expected risk premium, or whether the excess volatility is better seen as evidence for changes in investor sentiment that cannot fully be explained by changes in the variables that affect value (Cochrane, 1991).

Subsequent research has questioned whether changes in forecasts of cash flows to equity and of discount rates are too small to explain the observed market volatility. Lettau & Ludvigson (2005) find that ‘changing forecasts of stock market dividend growth do make an important contribution to fluctuations in the post-War U.S. stock market’ (p. 585), though their evidence is consistent with the existence of excess volatility. Ackert & Smith (1993) present evidence that, when share repurchases and cash payments resulting from acquisitions are added to dividends, the volatility of observed market values is not excessive, even assuming a constant discount rate. Larrain and Yogo (2008) compare the variation in dividend yield, in which the cash flows are given by dividends, and payout yield, in which cash flows are given by dividends plus repurchases less cash raised via share issues. Assuming an infinite future horizon, all of the variation in either measure of yield has to be explained by changes in forecast cash flows and discount rates. Using VAR forecasts, they find that 83% of the variation in dividend yield is explained by variation in the discount rate (their Table 9), consistent with excess volatility of market values. But, in contrast, 84% of the variation in payout yield is explained by variation in forecast payout growth, and changes in equity repurchase and issuance are ‘highly predictable’ (p. 220). So there is less support for the excess-volatility view, if yield is measured as payout yield instead of dividend yield. Chen & Zhao (2009) show that the variation in forecast discount rates is very sensitive to the specification of the VAR forecasting model. The conclusion about the relative importance of
variation in discount rates or future cash flows in explaining the variation in equity returns is also very sensitive to the VAR specification.

Actuarial analysis in recent decades has focussed on the use of stochastic modelling techniques. The pioneering work of Wilkie (1986) presents a model in which the predicted natural log of the dividend yield for a given date is given by the mean of the log of the yield, plus 0.6 of the deviation of the observed yield one year ago from the mean value of the yield during the sample period, plus 1.35 of the log of inflation during the previous year, plus a random term which is modelled as an autoregressive process. This model has been subsequently refined and updated, as presented in Wilkie (1995) and Wilkie et al (2010). Other actuarial models for simulating future economic and investment conditions in the UK are compared and discussed in Lee and Wilkie (2000).

For all the debate about the extent of excess volatility, the finance literature leaves readers with little understanding of how much variation in the forecast price-determining variables there has been, and how much variation is required to justify the observed volatility of market values. This is because most of these studies estimate the notional market values justified by price-determining variables from the Campbell-Shiller (1988) version of the dividend-growth model, or some variant thereof, combined with a VAR to estimate the year-by-year forecasts of the discount rates and cash flows. The variation over time in the forecasts of discount rates and cash flows, and their impact on the resulting estimate of rational market volatility, are opaque in such studies.

The current paper explores the market volatility justified by changes in price-determining variables in a more accessible manner. In the interests of simplicity and transparency, decomposition of the factors affecting value is based on the standard dividend-growth model. This means it is assumed that, at a given date, the values of the forecast discount rate and dividend growth rate are the same for each future year, and when the forecast discount rate or growth rate changes, the change applies to the forecast rate for every future year.

The paper employs UK data for the period 1921-2008. An advantage of using UK data is that cash flows to investors are almost entirely in the form of dividends, even in recent years. The paper presents base-case year-by-year estimates of the expected real interest rate as at date \( t \), \( r_{t,t} \), and estimates of the expected real growth rate of dividends as at date \( t \), \( g_{r,t} \), and shows how altering the assumed variation in these estimated forecasts affects the implied market volatility. The long-term inflation and real growth expectations are assumed to be rational and homogeneous. However, the risk-premium element is a residual that is inferred
given current markets values, dividends, interest rates, and the forecasts of inflation and real
growth. The risk premium in the model can reflect both rational and irrational expectations.

Our approach to forecasting is similar to that of papers which estimate the expected
risk premium in the past (Blanchard, 1993; Jagannathan et al, 2001; Arnott & Bernstein,
2002; Best & Byrne, 2002; Fama & French, 2002; Ilmanen, 2003; Claus & Thomas, 2003;
Vivian, 2007). These papers infer the expected risk premium from some version of the
dividend-growth model, using a variety of relatively simple methods to estimate the forecasts
of investors, none of which involve a VAR.¹ Base-case forecasts in this paper are thought to
be reasonable, assuming that investors forecast a single future $r_{r,t}$ and $g_{r,t}$ at a given date $t$. An
alternative assumption is that investors forecast different values for $r_{r,t+n}$ and $g_{r,t+n}$ for
different future years $t+1$, $t+2$, ..., but that changes in these forecast values over time are
equivalent to changes in single numbers for $r_{r,t}$ and $g_{r,t}$.

The approach adopted in this paper is first used to estimate the expected risk premia
on equity in the past, and to estimate the contribution to market volatility of changes over
time in the expected risk premium. The market values that would have arisen if the expected
risk premia were fixed at their estimated mean are then inferred. This enables a comparison to
be made between market volatility implied under a fixed expected risk premium and actual
volatility. The volatility of the base-case forecasts of $r_{r,t}$ and $g_{r,t}$ are then reduced to show the
impact on implied market volatility.

The rational forecasts that should determine market value at any given time cannot be
known with certainty, whatever method of estimation is used.² This paper joins others,
mentioned above, which argue that estimates of rational volatility are sensitive to the choice
of forecasts.³ However, the main contribution is the transparent framework within which the
forecasts of $r_{r,t}$ and $g_{r,t}$ determine fundamental value. It is hoped that the reader will be left
with a much clearer grasp of the relationship between the volatilities of the forecasts and the
resulting notional market volatility.

¹ Another strand in the literature explores the forecasting of risk premia using lagged explanatory
variables such as dividend yield (for example, Welch & Goyal, 2008).
² The standard test for whether a given forecast is rational is to examine whether the forecast errors are
related to information known at the time the forecast was made. But the relevant horizon for the real
interest rate and real dividend growth rate is infinity, so it is uncertain over what interval to measure
the forecast errors.
³ Estimates of the mean expected risk premium inferred from the dividend-growth model are more
robust. The conclusion that the mean observed risk premium in the UK or USA was higher on average
than the mean expected risk premium during the second half of the twentieth century is not sensitive to
the specific forecasts chosen or methodology used.
The rest of this paper is organised as follows. Section 2 provides a decomposition of equity and bond returns in terms of changes in the underlying fundamental variables. In Section 3, expected dividend growth rates and expected real return rates in the past are estimated. Section 4 gives the results of the empirical analysis and Section 5 concludes.

2. Decomposition of equity and bond returns

This section offers a straightforward analysis of the equity and bond returns for a given year in terms of changes in the variables that should affect equity and bond values.

2.1 Equity

The expected nominal equity return as at date \( t \), \( r_t \), is estimated by

\[
r_t = \frac{D_t (1 + g_t)}{P_t} + g_t
\]

where \( D_t \) is the total dividends paid by listed companies in a given index during the year ending at date \( t \), \( P_t \) is the total market capitalisation of the ordinary shares in the index at date \( t \), and \( g_t \) is the expected value of the annual growth rate of dividends, as at date \( t \). Dividends are assumed to be paid at the end of the calendar year, for simplicity. Our notation uses capitals for actual observable values, and small letters for expected values; a date \( t \) is always at the end of a calendar year. For example, for \( t = 31 \) December 1989, investors are assumed to know the market capitalisation on that day and the value of dividends paid during 1989, and to have an expectation of the growth rate of dividends in 1990 and each subsequent year.

Return due to unexpected dividend growth in first year

The effect on the equity return of unexpected dividend growth during the next twelve months (i.e. the notional return for the year assuming no change by the end of the year in \( r_t \) or \( g_t \), less the expected return as at date \( t \)) is first isolated. It follows from equation (1) that the prospective dividend yield remains the same from one year to the next, so that

\[
D_t (1 + g_t)/P_t = D_t (1 + G_{t+1})(1 + g_{t+1})/P_{t+1}
\]

and with \( g_{t+1} = g_t \),

\[
D_t/P_t = D_t (1 + G_{t+1})/P_{t+1}
\]

where \( G_{t+1} \) is the actual nominal dividend growth rate for the year ending at date \( t+1 \). Thus, to maintain the same yield at \( t+1 \) as at \( t \), the following must hold:

\[
P_{t+1} = P_t (1 + G_{t+1})
\]

(2)

So the actual equity return with \( r_t \) and \( g_t \) fixed, \( R^*_{t+1} \), is

\[
R^*_{t+1} = \frac{(D_{t+1} + P_{t+1})/P_t - 1}{\frac{D_t (1 + g_t)}{P_t} + g_t}
\]
\[
\begin{align*}
&= \{D_t(1 + G_{t+1}) + P_t(1 + G_{t+1}) - P_t\}/P_t \\
&= D_t(1 + G_{t+1})/P_t + G_t \\
&= G_{t+1}(1 + D_t/P_t) + D_t/P_t
\end{align*}
\]
of which the expected return from re-arranging (1) is given by
\[
r_t = g_t(1 + D_t/P_t) + D_t/P_t
\]
and the effect on return of unexpected dividend growth during the year starting at date \( t \), \( R(\Delta D)_{t+1} \), is given by
\[
R(\Delta D)_{t+1} = R^*_{t+1} - r_t \\
= (G_{t+1} - g_t)(1 + D_t/P_t)
\]

Return due to changes in expected return or expected dividend growth

Consider now the return that is due to a change in \( r_t \) or \( g_t \). Re-arranging (1) again,
\[
D_t/P_t = (r_t - g_t)/(1 + g_t)
\]
So a change in \( r_t \) or \( g_t \), implies a change in yield, and the change in yield can be written as:
\[
\Delta[(r - g)/(1 + g)]_{t+1} = (r_{t+1} - g_{t+1})/(1 + g_{t+1}) - (r_t - g_t)/(1 + g_t)
\]
From (2), the price at \( t+1 \) with no change in yield must be \( P_t(1 + G_{t+1}) \). So the return due to a change in yield, or in \( r_t \) or \( g_t \), \( R\{\Delta[(r - g)/(1 + g)]\}_{t+1} \), can be written as
\[
R\{\Delta[(r - g)/(1 + g)]\}_{t+1} = [P_{t+1} - P_t(1 + G_{t+1})]/P_t
\]
It follows that (see Appendix 1 for proof):
\[
R\{\Delta[(r - g)/(1 + g)]\}_{t+1} = \left[\frac{D_t/P_t - D_{t+1}/P_{t+1}}{D_{t+1}/P_{t+1}}\right](1 + G_{t+1})
\]
(6)
The return due to a change in \( r_t \) or \( g_t \), can also be analysed as the sum of the returns due to changes in the components of \( r_t \) and \( g_t \). Thus,
\[
r_t = r_{Fr,t} + i_t + \theta_t + \pi_t
\]
and
\[
g_t = g_{Fr,t} + i_t
\]
where \( r_{Fr,t} \) is the expected real interest rate, \( i_t \) is the expected rate of inflation, \( \theta_t \) is the inflation risk premium, \( \pi_t \) is the expected (equity) risk premium, and \( g_{Fr,t} \) is the expected real growth rate of dividends. The approximate, additive, formula for nominal rates is used for simplicity. Thus,
\[
(r_t - g_t)/(1 + g_t) = [(r_{Fr,t} + i_t + \theta_t + \pi_t) - (g_{Fr,t} + i_t)] / (1 + g_t)
\]
(8)
Using (5), (6) and (8) to express the return due to a change in \( r_t \) or \( g_t \) as the sum of the returns due to changes in the components of \( r_t \) and \( g_t \):
\[
R\{\Delta[(r - g)/(1 + g)]\}_{t+1} = R(\Delta r_{Fr})_{t+1} + R(\Delta \theta)_{t+1} + R(\Delta \pi)_{t+1} - R(\Delta g_{Fr})_{t+1}
\]
(9)
The return due to a change in $r_{Fr,t}$, $R(\Delta r_{Fr})$, for example, can be derived by taking (6) as the starting point. The $D/P$ terms in (6) can be re-expressed in terms of $r$ and $g$, using (5). Since $r_{Fr,t}$ is a component of $r_t$, as shown in (7), it then follows that

$$R(\Delta r_{Fr})_{t+1} = \frac{r_{Fr,t}/(1+g_t) - r_{Fr,t+1}/(1+g_{t+1})}{(r_{t+1} - g_{t+1})/(1+g_{t+1})}$$

(10)

The other expressions on the right-hand side of (9) are defined analogously.

**Risk premium**

All the variables are estimated directly except the expected risk premium, $\pi_t$. This is calculated as the residual expected return:

$$\pi_t = r_t - r_{F,t}$$

where $r_{F,t}$ is the expected return on the risk-free asset

$$r_t = r_t - (r_{Fr,t} + i_t + \theta_t)$$

$r_t$ is estimated via the re-arranged dividend-growth formula in (1), and $r_{F,t}$ is proxied by the yield on undated government bonds. Our methods of estimating $r_{Fr,t}$, $i_t$ and $\theta_t$, explained below, ensure that these components sum to give $r_{F,t}$. Because $\pi_t$ is calculated as the residual expected return, decomposition of the return for a given year is exact: the component returns on the right hand side of (9), which include $R(\Delta \pi)_t$, sum exactly to give the return due to a change in dividend yield in (6), and therefore

Actual return, $R_{t+1} = $ Expected return, $r_t$, +

Return due to unexpected dividend growth, $R(\Delta D)_{t+1}$, +

Return due to a change in dividend yield, $R\{\Delta[(r - g)/(1 + g)]\}_{t+1}$

Note that a change in the expected rate of inflation, $i_t$, does not affect the notional return on equity due to a change in $r_t$ or $g_t$. This is because $i_t$ is included additively in both $r_t$ and $g_t$, and therefore cancels out (see eq. (8)). The inflation risk premium, however, is a component of the discount rate but not of the expected rate of dividend growth, and so a change in its value affects the notional return for the relevant year. Another point to notice is that the absolute size of the return arising from a given percentage change in one of the variables is negatively related to the dividend yield at date $t+1$. That is, the impact on return of a given percentage change in one of the variables is greater when the yield is low.4

---

4 Small changes in forecasts that affect all future periods can have a surprisingly large impact on the volatility of the implied market values, especially at low yields. For example, suppose that $r_t = 5\%$ and $g_t = 3\%$, and so the yield at date $t$ is $(5\% - 3\%)/(1.03) = 1.94\%$. A 10% fall in $r_t$ gives a yield at date $t+1$ of 1.46%, which implies a capital gain of 32.9%.
2.2 Bonds

The return on bonds can be decomposed in a similar manner. The yield on 2.5% consols (undated government bonds) is used as a proxy for \( r_{F,t} \). With undated bonds, the price is given by

\[
P_t = \frac{Y}{r_{F,t}}
\]  

(11)

where \( Y \) is the annual interest payment, which is fixed in nominal terms. A change in price is caused by a change in the discount rate. It follows from (11) that the return due to a change in the discount rate, \( R_F(\Delta r_F)_{t+1} \), is given by

\[
R_F(\Delta r_F)_{t+1} = \frac{P_{t+1}}{P_t} - 1 = \frac{r_{F,t} - r_{F,t+1}}{r_{F,t+1}}
\]

The return due to a change in the discount rate can be decomposed as follows:

\[
R_F(\Delta r_F)_{t+1} = R_F(\Delta r_{Fr})_{t+1} + R_F(\Delta \bar{i})_{t+1} + R_F(\Delta \theta)_{t+1}
\]  

(12)

where \( R_F(\Delta r_{Fr})_{t+1} = (r_{Fr,t} - r_{Fr,t+1})/r_{F,t+1} \), and analogously for \( R_F(\Delta \bar{i})_{t+1} \) and \( R_F(\Delta \theta)_{t+1} \).

3. Estimation of expected dividend growth rates and real interest rates in the past

UK data are used and the sample period is 1921-2008. Requisite data are available for 1900 onwards, but 1921 is used as the starting point to avoid the period during and shortly after the 1914-18 war, when dividends were extremely volatile, and to ensure that we have at least 15 years of past dividend growth. The data are mostly from the Equity-Gilt Study, produced annually by Barclays Capital, and from Datastream. Details of the data sources and of the returns calculations are shown in Table 1. The forecasts and their volatilities are intended to be plausible and easy to understand.

Table 1 around here

Expected real dividend growth rate

A number of variables and combinations of variables were assembled and analysed for their ability to reflect long-term real growth expectations, utilising the fact that a negative correlation between the equity market yield and such expectations should be anticipated. The following proved to be statistically the most significant:

\[
g_{r,t} = \bar{G}_r (t-15, t+10)
\]  

(13)
where $\bar{G}_r(t-15, t+10)$ is the geometric mean real growth rate of dividends during the 25-year period that starts at date $t-15$ and ends at date $t+10$. The real growth for a single year is

$$G_{r,t} = \frac{(1 + G_t)/(1 + I_t) - 1}{(1 + G_t)/(1 + I_t) - 1}$$

where $G_t$ is the percentage growth in dividends for year $t$ and $I_t$ is inflation. The estimate in (13) is a moving average measured over a long period, and so it is normally slow-moving. The combination of 15 years of past growth data, known as at date $t$, and ten years of forward data, unknown at date $t$, is meant to capture the idea that investors base their expectations primarily on observed growth in recent years, but with some ability to adjust for changing economic circumstances. The estimates of $g_{r,t}$ in Arnott & Bernstein (2002) and Ilmanen (2003) are also moving averages. Repurchases and other cash payments to shareholders are ignored.6

The above method results in estimates of negative expected real growth for several years in the 1920s, 1940s and 1970s. An expectation of negative real growth indefinitely is thought to be implausible, and an expected real growth rate of 0% pa is therefore set as a minimum. The estimates are below 3.0% pa except for one outlier of 4.3% pa in 1935. This estimate is capped at 3.0% pa. These constraints reduce the variation in $g_{r,t}$, which reduces the variation in returns that can be ‘explained’ by changes in this variable. The estimates used are shown in Figure 1. The mean of $g_{r,t}$ is 0.99%, the standard deviation is 0.81%, and the mean of the absolute values of the changes is 0.32%.

Figure 1 around here

**Expected real interest rate**

For the period 1982-2008, the expected real rate of interest, $r_{Fr,t}$, is given by the yield on 20-year index-linked government bonds, which were introduced in 1981. The index-linked yield provides a good estimate of the expected long-term real interest rate at a given date, although the market was somewhat illiquid in its early years.

The expected rate of inflation, $i_t$, is estimated for 1982-2008 as follows. The inflation gap, $z_t$, is calculated as:

Yield on 2.5% consols – Yield on 20-year index-linked gilts

---

5 For 2000 onwards there are fewer than ten future years between date $t$ and the end of 2008. For these years the growth rates for all available future years are used.

6 Annual repurchases in the UK were below 0.1% of market value until 1995, and had risen to 0.9% by 2004 (Vivian, 2007). Results regarding volatility are almost the same if Vivian’s estimated repurchases are added to dividends.
The expected rate of inflation is given by $z_t - \theta_t$. The inflation risk premium $\theta_t$ is estimated as $0.2z_t$. This assumes that there is a positive relation between the inflation risk premium and expected inflation, and there is evidence that such a relation exists (Breedon & Chadha, 2003). Evidence to justify an inflation risk premium of up to 20% of the inflation gap is in Shen (1998) and Garcia & Werner (2010). The expected rate of inflation in the period 1982-2008 is then given by:

$$i_t = z_t - 0.2z_t = 0.8z_t$$

Calculations with no inflation risk premium are also carried out.

For the period 1921-81, expected inflation is estimated from the yield on 2.5% consols. A regression of the yield $Y_t$ on future inflation shows that the yield provides quite a good forecast, at least for inflation during the subsequent decade:

$$\bar{I}(t, t+9) = 0.323\% + 0.616Y_t$$  \hspace{1cm} (14)

$$\begin{align*}
(0.40) & \hspace{1cm} (5.69)
\end{align*}$$

where $\bar{I}(t, t+10)$ is the geometric mean rate of inflation for the ten years between $t = 0$ and $t+10$ and the numbers are OLS regression coefficients with $t$-statistics in brackets beneath. The $R^2$ is 0.30.

The expected real interest rate for the period 1921-81 is then given by:

$$r_{Fr,t} = r_{F,t} - z_t$$

where $r_{F,t}$ is the prevailing yield on 2.5% Consols, as above, and $z_t$ is taken to be $i_t/0.8$, as for the period 1982-2008.

The estimates of the expected real interest rate are shown in Figure 2. The rate varies between 0.2% and 4.4% pa. As this seems a reasonable range within which the expected rate could vary, no adjustments are made. The mean of $r_{Fr,t}$ is 1.56%, the standard deviation is 1.26%, and the mean of the absolute values of the changes is 0.19%. If it is accepted that the yield on index-linked gilts provides a fairly precise estimate of the expected real interest rate at a given time, the evidence from the index-linked market shows that the expected real rate does vary year-by-year. In fact the mean of the absolute values of the changes is 0.30% for 1982-08 from the index-linked market, compared with 0.15% for 1921-81 from the alternative estimates.
4. Results

This section presents the analysis for the period 1921-2008, first with an inferred (variable) expected risk premium and then with a fixed expected risk premium. Simulated volatilities under a range of alternative assumptions are then calculated. In particular, estimates of standard deviations of the main real variables are altered. Implications for the standard deviation of fixed-premium returns are assessed, and comparisons made with the standard deviation of actual returns.

4.1 Results with variable expected risk premium

Table 2 shows the results for the case in which the expected risk premium is inferred and varies from year to year, as described above. The results regarding the risk premium are first briefly discussed. The arithmetic mean expected risk premium for 1921-2008 is 3.3%, whereas the ex post risk premium is 4.9%. Taking the 50 years 1950-99, the mean expected risk premium is 3.0%, compared with an ex post risk premium of 9.1% (not shown in the table). Thus the results agree with those of other UK and US studies, cited in the Introduction, that estimate the expected risk premium in the past and find that the historic risk premium in the second half of the twentieth century provides an upwardly biased estimate of the expected risk premium.

Table 2 around here

The difference of 1.7 percentage points between the ex post (actual) and expected risk premium for 1921-2008 is explained by an actual mean return on equity that is 2.9 percentage points higher than the expected return, partly offset by a return of 1.2% due to change in yield ($r_{F,t}$). According to the decomposition in this paper, the reasons for the higher-than-expected ex post risk premium are changes in the expected equity premium (+1.2 percentage point contribution to the ex post premium, so the expected premium tended to decline), and unexpected dividend growth (+1.0 point). These factors that increased the ex post premium are partly offset by changes in expected inflation that increased the return on bonds (−0.4 point contribution to the risk premium). The inference of a declining expected risk premium echoes that of previous studies, especially Fama & French (2002). But unexpectedly high dividend growth is an important contributor to the unexpectedly high ex post risk premium.

Turning to the results relating to volatility, the expected risk premium for each year has a mean of 3.3% and a standard deviation of 1.8%; the mean of the absolute values of the
changes is 0.8%. So it exhibits substantial variation over time. The standard deviation of the returns due to changes in the expected risk premium is 22.7%, which is close to the standard deviation of 23.9% for the actual returns. However, the changes in the expected risk premium contribute nothing to the volatility of the observed returns, because they often dampen down the return that would have arisen had the risk premium not changed. One way of showing this is in Figure 3. There are two bars for each year. The first bar is the actual return on equity less the return arising from the change in the expected risk premium: $R_t - R(\Delta\pi)_t$. This difference is the return for the year that would have arisen, had the expected risk premium not changed from its value in the previous year (it is not the same as the return assuming a constant expected risk premium every year). The second bar shows the return that is ascribed to the change in the expected risk premium, $R(\Delta\pi)_t$. The two returns (bars) combined give the actual return, $R_t$. For clarity, Figure 3 shows these results for 1960-2008 only.

Figure 3 around here

Figure 3 shows that for the majority of years (61% during 1960-2008; 65% during the full sample period), the return due to a change in the expected risk premium has the opposite sign from the return due to the other variables. Consistent with the visual impression, the correlation coefficient for the series $R_t - R(\Delta\pi)_t$ and $R(\Delta\pi)_t$ is –0.32. During the four years 1995-98, for example, the equity returns would have been even higher had the expected risk premium not been rising. The major exceptions are the extreme years of 1974 and 1975, when the returns due to changes in the expected risk premia greatly augmented the returns ascribed to other factors.

The reader might feel that a mean of the absolute changes in the inferred risk premium of 0.8% implies implausibly large jumps from one year to the next. The consensus in other research is that, while the expected risk premium probably does change over time, it does so gradually. However, estimates of the changes in expected risk premia in this paper should not be taken too literally. $\Delta\pi_t$ is calculated as a residual: it is the change in the expected equity return (discount rate) that must have arisen given the actual equity return for the year starting at date $t$, and given the changes in the other variables that determine the notional return with no change in the risk premium. One possible explanation for the variation in the expected risk premium is that the estimates of $r_{r,t}$ and $g_{r,t}$ are not variable enough: investor expectations regarding these variables change through time by more than have been estimated, causing the
inferred risk premium to overstate the actual changes in the expected risk premium. For example, during the extreme year of 1975, the expected risk premium falls from 6.5% at the start of 1975 to 0.6% at the start of 1976. The estimated real interest rate falls from 3.7% to 3.0%. There is no change in the estimated forecast real dividend growth rate, which is zero for both years. The actual risk premium for 1975 is +111.0%, most of which is ‘explained’ by a fall in the expected risk premium. But if the actual fall in the expected real interest rate was greater, or if investors became more optimistic about real dividend growth during 1975, the estimated change in the expected risk premium is exaggerated.

Alternatively, for some years the return ascribed to a change in the expected risk premium could be viewed as having an irrational component, and the apparent changes in the expected risk premium would then be seen as a symptom of irrational pricing, as discussed in the Introduction. Whatever the interpretation of the changes in the expected risk premium, the observed volatility for the sample period can be explained without assuming that there were changes in the expected risk premium. This is now shown more directly.

### 4.2 Results with fixed expected risk premium

This section presents the volatility that would have arisen had the expected risk premium been fixed. The expected risk premium is set at 3.3% every year, which is the arithmetic mean over the sample period that has already been inferred. The values of \( r_{Fr,t}, i_t, \theta_t \) and \( g_{r,t} \) are unchanged. Using a similar approach to that in Section 2.1, the simulated expected return with a fixed premium, \( Simr_t \), and the return due to unexpected dividend growth, \( R(Sim\Delta D)_{t+1} \), are calculated as follows:

\[
Simr_t = r_{Fr,t} + i_t + \theta_t + 3.3\%
\]

\[
Simr_t = g_t[1 + Sim(D_t/P_t)] + Sim(D_t/P_t)
\]

(15)

\[
R(Sim\Delta D)_{t+1} = (G_{t+1} - g_t)[1 + Sim(D_t/P_t)]
\]

(16)

where the simulated dividend yield is given by

\[
Sim(D_t/P_t) = (Simr_t - g_t)/(1 + g_t)
\]

(17)

Note that equations (15), (16) and (17) are similar in form to equations (3), (4) and (5).

The simulated return due to a change in \( Simr_t \) or \( g_t \) is given by:

\[
R\{\Delta[(Simr - g)/(1 + g)]\}_{t+1} = SimR(\Delta r_{Fr})_t + SimR(\Delta \theta)_t + SimR(\Delta g_r)_t + \text{balancing term}
\]

(18)

where

\[
SimR(\Delta r_{Fr})_{t+1} = [r_{Fr,t}/(1 + g_t) - r_{Fr,t+1}/(1 + g_{t+1})] (1 + G_{t+1})/[(Simr_{t+1} - g_{t+1})/(1 + g_{t+1})]
\]

(19)
and SimR(Δθ)_{t+1} and SimR(Δg,\textsuperscript{r})_{t+1} are defined analogously. Although the expected risk premium is fixed at 3.3%, so there is no return due to a change in the risk premium, a small balancing term is needed, defined as

\[
\text{balancing term} = \frac{3.3%/(1 + g_t) - 3.3%/(1 + g_{t+1})}{(1 + G_{t+1})/[(Simr_{t+1} - g_{t+1})/(1 + g_{t+1})]}
\]

The total simulated return is the sum of (15), (16) and (18):

\[
SimR_{t+1} = Simr_t + R(Sim\Delta D)_{t+1} + R\{\Delta[(Simr - g)/(1 + g)]\}_{t+1}
\]

The results are shown in Table 3. The key finding is that the simulated returns with the expected risk premium fixed at 3.3% are at least as volatile as the actual returns.\(^7\) The standard deviation of the fixed-premium returns is 28.1%, compared with the standard deviation of the actual returns of 23.9%. The standard deviation of the fixed-premium returns would have to be below 16.5% for the fixed-premium returns to be significantly less volatile than the actual returns at the 1% level, using a one-tailed F-test on the ratio of the variances. Table 3 also shows that changes in \(g_{r,t}\) are the most important cause of variation in the fixed-premium returns in the full sample.

Table 3 around here

The period 1982-2008 is examined separately (although the results are not reported in detail). Estimates of the expected real interest rate are more reliable for this period, and the expected real dividend growth rate is less variable than in earlier years; the mean of the absolute values of Δ\(g_{r,\text{t}}\) is 0.24 for 1982-08, compared with 0.35 for 1921-81. The average expected risk premium for 1982-08 is 1.6%, so 1.6% is the fixed risk premium used to calculate the fixed-premium returns. The standard deviation of the actual returns on equity during 1982-2008 is 17.0%; the standard deviation of the fixed-premium returns is 21.0%. So, as for the full sample, the fixed-premium returns are at least as volatile as the actual returns. For 1982-2008 changes in the expected real interest rate are the most important source of variation in the fixed-premium returns.

The fixed-premium returns are related to the actual returns. In 70% of the years in the full sample the two returns have the same sign, and the correlation coefficient for the two series is 0.24 (\(t = 2.25\)). These results indicate that the fundamentals that are supposed to

\(^7\) Although the expected risk premium is fixed at its sample mean, the simulated returns differ from the actual returns, and their means differ. This is because the impact on returns of changes in Simr, which incorporates the fixed risk premium, differs from the impact of changes in \(r,\) which incorporates a variable risk premium. It is the presence of Simr\(_{t+1}\) in the denominator of (19) that causes the simulated returns arising from changes in \(r_{fr,t}\), for example, to differ from the unsimulated returns, given by (10).
affect value in the fixed-premium dividend-discount model do have significant explanatory power. Figure 4 shows the two returns for each year, for 1960-2008.

Figure 4 around here

4.3 Simulated volatilities under alternative assumptions

First assume that there is no inflation risk premium. This assumption is made in a number of previous studies such as Blanchard (1993) and Ilmanen (2003). For 1921-81, the expected real interest rate is estimated by subtracting the estimate of expected inflation, with no added premium, from the consols yield. For 1982-08 it is assumed that the entire inflation gap measured via equation (14) represents expected inflation. These adjustments result in a standard deviation of the fixed-premium returns of 22.9%, less than the 28.1% of the base-case fixed-premium returns, but little different from the standard deviation of the actual returns of 23.9%.

An advantage of the analysis in this paper is that the forecasts that determine the predicted changes in equity values are explicit. For predicted volatility of fixed-premium returns to be less than actual volatility, the estimated values of $r_{Fr,t}$ and $g_{r,t}$ would have to be less variable than they are in Figures 1 and 2. Table 4 shows the volatilities of the fixed-premium returns, with an inflation risk premium, under various assumptions about the volatilities of $r_{Fr,t}$ and $g_{r,t}$. It shows directly how changing the volatilities of the price-determining variables changes the volatility of the resulting notional market returns. Each cell reports the standard deviation of the fixed-premium returns resulting from applying differing values of $x$ in the following formula

$$\Delta r_{Fr,t}^* = \text{av}(r_{Fr,t}) + x[\Delta r_{Fr,t} - \text{av}(r_{Fr,t})]$$

where $\Delta r_{Fr,t}^*$ is the adjusted change in the expected real interest rate for year $t$ used to calculate the fixed-premium returns, $\text{av}(r_{Fr,t})$ is the arithmetic mean of $r_{Fr,t}$ for the sample period, and a value for $x$ is selected between 1.0 and 0.0. $x = 1$ means that the year-by-year changes in $r_{Fr,t}$ are unaltered; $x = 0$ means that there is no variation in $r_{Fr,t}$. The same formula is used to vary the volatility of $g_{r,t}$. The formula results in smaller year-by-year changes in the relevant variable, while preserving its mean value.

Table 4 around here
Table 4 shows the combinations of adjustments needed for the standard deviation of the fixed-premium returns to be less than 16.5%, i.e. significantly less than the standard deviation of the actual returns. For example, if the volatility of $g_{r,t}$ were 0.8 times its actual level, the volatility of $r_{Fr,t}$ would need to drop to 0.4 times its actual level for the fixed-premium volatility to fall below 16.5%. If both $g_{r,t}$ and $r_{Fr,t}$ were constant, the fixed-premium volatility would be 8.9%. This is the volatility of the returns with a constant yield, most of which is volatility attributed to ‘unexpected’ year-by-year changes in actual dividends paid (see equation 4). Table 4 also shows that the fixed-premium volatility is more sensitive to the volatility of $g_{r,t}$ than of $r_{Fr,t}$. This arises because the year-by-year changes are larger for $g_{r,t}$ than for $r_{Fr,t}$ in the full sample. Of course, if the base-case variation in $g_{r,t}$ or $r_{Fr,t}$ were felt to be too low, $x$ in equation (20) would exceed one and the fixed-premium volatility would be higher than in the base case.

5. Conclusion

The paper presents a transparent analysis of the impact on fundamental values of year-by-year changes in estimates of the expected real interest rate and the expected real growth rate of dividends. An important application of the analysis is that it helps the reader to appreciate the relationships between the volatility of price-determining variables and the volatility of fundamental values. It is possible to see how variable over time the expected real interest rate and real dividend growth rate need to be in order for the observed market volatility to be justified. It is impossible to gain an understanding of this from previous research, which employs the Campbell-Shiller logarithmic version of the dividend-growth model combined with forecasts of the real interest rate and real dividend growth rate derived from vector autoregression. Risk premia expected in the past can also be inferred, using our analysis.

Estimates of forecasts for $r_{r,t}$ and $g_{r,t}$ in the past are believed to be reasonable. They are derived from simple methods, of the type used by authors who have inferred the risk premium expected in the past. The average of the estimated expected risk premium during the sample period is 3.3%, which is in line with the estimates in previous studies. Changes in expected real interest rate forecasts and expected dividend growth rate forecasts are sufficient to explain the observed volatility of the UK stock market during 1921-2008. This is the case whether the expected risk premium is allowed to vary, or whether market returns which would have arisen had the expected risk premium been fixed are estimated. Readers can, literally, see what the forecasts look like (Figures 1 and 2) that produce the results, and judge
for themselves whether the forecasts are too volatile. The standard deviation of both the forecasts of $r_{r,t}$ and of $g_{r,t}$ would have to drop by about one third for the notional market volatility with a fixed risk premium to be the same as actual market volatility (Table 4).

Any forecasting method that produces year-by-year variation in $g_{r,t}$ and $r_{Fr,t}$ that is similar to the variation in the estimates in this paper is likely to give similar results regarding volatility. For example, a study that has similar implications regarding volatility is Blanchard (1993). His estimates of $r_{Fr,t}$ and $g_{r,t}$ appear to fluctuate year-by-year at least as much, although the range of Blanchard’s estimates is somewhat greater for the expected real interest rate, and somewhat less for the expected real growth rate. In the light of our UK results in this paper, it is almost certain that Blanchard’s estimates of $r_{Fr,t}$ and $g_{r,t}$ would be more than sufficient to explain the observed US market volatility.

Using the analysis in this paper, readers can readily calculate the expected risk premium, or the notional volatility of market returns, by inserting their own year-by-year forecasts of $r_{r,t}$ and $g_{r,t}$.
Appendix 1: Proof of Equation (6)

\[ R\{\Delta[(r - g)/(1 + g)]\}_{t+1} = \frac{[P_{t+1} - P_t(1 + G_{t+1})]}{P_t} \]

\[ = \left[ \frac{P_{t+1}}{(1 + G_{t+1})P_t} - 1 \right] (1 + G_{t+1}) \]

\[ = \left( \left[ \frac{P_{t+1}D_{t+1}}{(1 + G_{t+1})P_tP_{t+1}} - \frac{D_{t+1}}{P_{t+1}} \right] \frac{P_{t+1}}{D_{t+1}} \right) (1 + G_{t+1}) \]

\[ = \left( \frac{D_t - D_{t+1}}{P_tP_{t+1}} \right) (1 + G_{t+1}) \text{ because } D_t = \frac{D_{t+1}}{(1 + G_{t+1})} \]

\[ = \frac{D_t - D_{t+1}}{P_tP_{t+1}} (1 + G_{t+1}) \]

\[ (6) \]
<table>
<thead>
<tr>
<th>Data item</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Equity yield and index value</td>
<td>1921-34: index constructed by Barclays Capital, in <em>Equity-Gilt Study 2009 (EGS)</em></td>
</tr>
<tr>
<td></td>
<td>1935-62: FT 30 index, from <em>EGS</em></td>
</tr>
<tr>
<td></td>
<td>1963-08: FT All-Share index, from Thomson Datastream</td>
</tr>
<tr>
<td>2.5% consols yield and price</td>
<td>1921-68: Capie &amp; Webber (2005)</td>
</tr>
<tr>
<td></td>
<td>1969-08: Thomson Datastream</td>
</tr>
<tr>
<td>Index-linked gilts</td>
<td>Thomson Datastream</td>
</tr>
<tr>
<td>Annual change in nominal dividend</td>
<td>Inferred from index value and yield¹</td>
</tr>
<tr>
<td>Annual inflation</td>
<td>From <em>EGS</em></td>
</tr>
</tbody>
</table>

### Calculation of returns

The equity return is given by $R_t = P_t(1 + Y_t)/P_{t-1} - 1$, where the yield $Y_t = D_t/P_t$. The return on consols is given by $R_{F,t} = (P_t + 2.5)/P_{t-1} - 1$. $P_t$ for equity is given by the index value and $P_t$ for bonds by the consol price, at the close of 31 December year $t-1$. There are discontinuities in the equity yield figures between 1962 and 1963, because of the switch from the FT30 index to the FTAll-Share index in 1963, and between 1997 and 1998, because of a change in the taxation of dividends in 1997. Adjustments to the yields are made in order that the change in yield, used in the decomposition of the return, is consistent with the correct return on equity.

¹The formula is $G_t = [(Y_t I_t)/(I_{t-1} I_{t-1}) - 1]$ where $I_t$ is the share price index at time $t$. 

---

Table 1

Data sources and calculation of returns
The returns and risk premia are arithmetic means of annual returns and risk premia for the period 1921-2008. The formulae are explained in Section 2.2. The expected return for a year ending at date $t$ is a return expected one year earlier, at date $t-1$.

<table>
<thead>
<tr>
<th>Return or premium</th>
<th>Return or premium</th>
<th>Standard deviation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Equity return</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Actual return, $R_t$</td>
<td>12.6</td>
<td>23.9</td>
</tr>
<tr>
<td>Of which, return due to</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Expected return, $r_{t-1}$</td>
<td>9.7</td>
<td>3.0</td>
</tr>
<tr>
<td>Unexpected dividend growth, $R(\Delta D)_t$</td>
<td>1.0</td>
<td>7.6</td>
</tr>
<tr>
<td>Change in $r_t - g_t$, $R{\Delta[(r - g)/(1 + g)]}_t$</td>
<td>1.9</td>
<td>22.9</td>
</tr>
<tr>
<td>Of which, return due to</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Change in expected real rate of interest, $R(\Delta r_{F,t})_t$</td>
<td>0.7</td>
<td>7.6</td>
</tr>
<tr>
<td>Change in inflation risk premium, $R(\Delta \theta)_t$</td>
<td>0.1</td>
<td>3.7</td>
</tr>
<tr>
<td>Change in risk premium, $R(\Delta \pi)_t$</td>
<td>1.2</td>
<td>22.7</td>
</tr>
<tr>
<td>Change in expected real growth rate of dividends, $R(\Delta g_r)_t$</td>
<td>-0.1</td>
<td>11.4</td>
</tr>
</tbody>
</table>

| Return on consols |                   |                    |
| Actual return, $R_{F,t}$ | 7.6             | 14.2               |
| Of which, return due to |                 |                    |
| Yield on consols (= expected return, $r_{F,t-1}$) | 6.4              | 3.4                |
| Change in $r_{F,t}, R_F(\Delta r_{F,t})_t$ | 1.2              | 13.3               |
| Of which, return due to |                 |                    |
| Change in expected real rate of interest, $R_F(\Delta r_{F,t})_t$ | 0.7              | 5.6                |
| Change in expected rate of inflation, $R_F(\Delta i)_t$ | 0.4              | 8.7                |
| Change in inflation risk premium, $R_F(\Delta \theta)_t$ | 0.1              | 2.2                |

| Risk premium |                   |                    |
| Ex post risk premium, $R_t - R_{F,t}$ | 4.9              | 21.5               |
| Of which |                 |                    |
| Expected risk premium, $r_{t-1} - r_{F,t-1}$ | 3.3              | 1.8                |
| Unexpected risk premium, $R_t - R_{F,t} - (r_{t-1} - r_{F,t-1})$ | 1.7              | 21.0               |
| Of which, risk premium due to |                 |                    |
| Unexpected dividend growth, $R(\Delta D)_t$ | 1.0              | 7.6                |
| Change in expected real rate of interest, $R(\Delta r_{F,t})_t - R_F(\Delta r_{F,t})_t$ | -0.1             | 3.3                |
| Change in expected rate of inflation, $R(\Delta i)_t - R_F(\Delta i)_t$ | -0.4             | 8.7                |
| Change in inflation risk premium, $R(\Delta \theta)_t - R_F(\Delta \theta)_t$ | 0.0              | 1.8                |
| Change in risk premium, $R(\Delta \pi)_t$ | 1.2              | 22.7               |
| Change in expected real growth rate of dividends, $R(\Delta g_r)_t$ | -0.1             | 11.4               |
Table 3  
**Results with expected risk premium fixed at 3.3%**

The returns are arithmetic means of annual returns for the period 1921-2008. The equity returns are simulated using a fixed expected risk premium of 3.3% and the returns implied by the actual values of the other variables that affect equity value. The balancing term arises because of the use of a fixed expected premium, and is defined in Section 4.2.

<table>
<thead>
<tr>
<th>Fixed-premium equity return</th>
<th>Return %</th>
<th>Standard deviation %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Simulated return, $\text{Sim}R_t$</td>
<td>13.4</td>
<td>28.1</td>
</tr>
<tr>
<td>Of which, return due to</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Expected return, $\text{Sim}r_{t-1}$</td>
<td>9.7</td>
<td>3.4</td>
</tr>
<tr>
<td>Unexpected dividend growth, $R(\text{Sim}D)_t$</td>
<td>1.0</td>
<td>7.5</td>
</tr>
<tr>
<td>Change in $\text{Sim}r_t - \text{g}_t$, $R{\Delta[(\text{Sim}r - \text{g})/(1 + \text{g})]}$</td>
<td>2.7</td>
<td>26.6</td>
</tr>
<tr>
<td>Of which, return due to</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Change in expected real rate of interest, $\text{Sim}R(\Delta r_{Fr})_t$</td>
<td>0.7</td>
<td>7.1</td>
</tr>
<tr>
<td>Change in inflation risk premium, $\text{Sim}R(\Delta \theta)_t$</td>
<td>0.1</td>
<td>3.3</td>
</tr>
<tr>
<td>Change in expected real growth rate of dividends, $\text{Sim}R(\Delta g_r)_t$</td>
<td>1.9</td>
<td>22.3</td>
</tr>
<tr>
<td>Balancing term</td>
<td>0.1</td>
<td>0.7</td>
</tr>
</tbody>
</table>
Table 4
Volatilities of simulated fixed-premium equity returns
under forecasts of differing variability

The table shows standard deviations of simulated fixed-premium equity returns, estimated under a range of assumptions about the volatilities of the expected real interest rate, $r_{Fr,t}$, and the expected real growth rate of dividends, $g_{r,t}$. The assumed changes in $r_{Fr,t}$, $\Delta(r_{Fr})^*$, are calculated from the formula $\Delta(r_{Fr})^* = \text{av}(r_{Fr,t}) + x[\Delta(r_{Fr,t}) - \text{av}(r_{Fr,t})]$, where $\text{av}(r_{Fr,t})$ is the arithmetic mean value of $r_{Fr,t}$ during the sample period, and $x$ is set at a value between 1 and 0 for each case. The same applies for $g_{r,t}$. The values of the two variables with $x = 1$ for each is the base case, reported in detail in Table 3. The values with $x = 0$ is the case with constant dividend yield.

<table>
<thead>
<tr>
<th>standard deviation of $g_{r,t}$ times</th>
<th>1.0</th>
<th>0.8</th>
<th>0.6</th>
<th>0.4</th>
<th>0.2</th>
<th>0.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0</td>
<td>28.1</td>
<td>24.7</td>
<td>23.5</td>
<td>20.6</td>
<td>19.3</td>
<td>18.2</td>
</tr>
<tr>
<td>0.8</td>
<td>20.5</td>
<td>18.9</td>
<td>17.6</td>
<td>16.5</td>
<td>15.6</td>
<td>14.9</td>
</tr>
<tr>
<td>0.6</td>
<td>16.2</td>
<td>15.2</td>
<td>14.3</td>
<td>13.5</td>
<td>12.9</td>
<td>12.4</td>
</tr>
<tr>
<td>0.4</td>
<td>13.5</td>
<td>12.7</td>
<td>12.1</td>
<td>11.5</td>
<td>11.0</td>
<td>10.6</td>
</tr>
<tr>
<td>0.2</td>
<td>11.9</td>
<td>11.3</td>
<td>10.7</td>
<td>10.2</td>
<td>9.8</td>
<td>9.4</td>
</tr>
<tr>
<td>0.0</td>
<td>11.3</td>
<td>10.7</td>
<td>10.2</td>
<td>9.7</td>
<td>9.3</td>
<td>8.9</td>
</tr>
</tbody>
</table>
Figure 3

Actual equity return less return due to change in expected risk premium (first bar), and return due to change in expected risk premium (second bar) (%), 1960-2008

Figure 4
Actual equity return (first bar) and simulated return with expected risk premium fixed at 3.3% (second bar) (%), 1960-2008
References


Barclays Capital (2009), *Equity-Gilt Study*.


